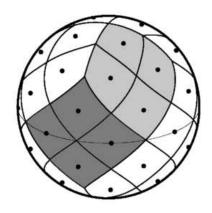
# **HEALPix** Fortran90 Subroutines Overview



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Abstract: This document is an overview of the **HEALPix** For-

tran90 subroutines.

# Contents

Conventions
Changes between release 2.13 and 2.14
Changes between release 2.0 and 2.13
Changes between release 1.2 and 2.0
Changes between release 1.1 and 1.2
$\mathrm{add\_card}\ .\ .\ .\ .\ .\ .\ .\ .\ .\ .\ .\ .\ .\$
$add\_dipole^* \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
$alm2cl^* \dots \dots$
$\mathrm{alm2map}^*\ \ldots\ldots\ldots\ldots\ldots\ldots\ldots\ldots$
$alm2map\_der^* \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
$alm2map\_spin^* \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
alms2fits*
$\mathrm{alter\_alm^*} \ \ldots \ $
ang2vec
angdist
$assert\_alloc,  assert\_directory\_present,  assert\_not\_present,  assert\_present  .$
brag_openmp
complex_fft
compute_statistics*
concatnl
convert_inplace*
convert_nest2ring*
$convert\_ring2nest^*  .  .  .  .  .  .  .  .  .  $
coordsys2euler_zyz
create_alm*
$\operatorname{del\_card} \ \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
$\mathrm{dump\_alms^*} \ . \ . \ . \ . \ . \ . \ . \ . \ . \ $
fits2alms*
$\mathrm{fits}2\mathrm{cl}^*\ \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
gaussbeam
$generate\_beam  .  .  .  .  .  .  .  .  .  $
get_card

CONTENTS 3

$get\_healpix\_data\_dir, \ get\_healpix\_main\_dir, \ get\_healpix\_test\_dir \ \dots \dots \dots \dots \dots$
getArgument
getEnvironment
$\operatorname{getdisc\_ring}$
getnumext_fits
getsize_fits
healpix_modules module
healpix_types module
in_ring
$input\_map^*$
$input\_tod^* \ldots \ldots$
$map2alm^* \dots \dots$
$map2alm\_iterative^* \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$
$map2alm\_spin^* \dots \dots$
$\mathrm{medfiltmap}^* \ldots \ldots$
median*
merge_headers
mpi_alm_tools*
mpi_alm2map*
mpi_alm2map_simple*
mpi_alm2map_slave
mpi_cleanup_alm_tools
mpi_initialize_alm_tools
mpi_map2alm*
mpi_map2alm_simple*
mpi_map2alm_slave
nArguments
neighbours_nest
npix2nside
nside2npix
nside2ntemplates
number_of_alms
output_map*
parse xxx

pixel_window
pix2xxx,ang2xxx,vec2xxx, nest2ring,ring2nest
planck_rng derived type
plm_gen
query_disc
query_polygon
query_strip
query_triangle
rand_gauss
rand_init
rand_uni
read_asctab*
read_bintab*
read_conbintab*
read_dbintab
read_fits_cut4
read_par
real_fft
remove_dipole*
ring_analysis
ring_num
ring_synthesis
rotate_alm*
same_shape_pixels_nest, same_shape_pixels_ring
scan_directories
string, strlowcase, strupcase
surface_triangle
template_pixel_nest, template_pixel_ring
udgrade_nest*
udgrade_ring*
vec2ang
vect_prod
write_asctab*
write_bintab*

CONTENTS 5

write_bintabh	209
write_dbintab	212
write_fits_cut4	213
write_minimal_header	216
write_plm	219
xcc_v_convert	221

#### Conventions

Here we list some conventions which are used in this document.

*	Fortran90 allows generic names which refer to several specific subroutines. Which one of the specific routines is called depends on the type and rank of the arguments supplied in the call. We tag generic names with a $\ast$ in this document.
$ m N_{side}$	$\mathbf{HEALPix}$ resolution parameter — see the $\mathbf{HEALPix}$ Primer.
map	We use the word "map" referring to a function, defined on the set of all <b>HEALPix</b> pixels.
$\theta$	The polar angle or colatitude on the sphere, ranging from 0 at the North Pole to $\pi$ at the South Pole.
$\phi$	The azimuthal angle on the sphere, $\phi \in [0, 2\pi[$ .

## Changes between release 2.13 and 2.14

• In alm2map\_der routine, a numerical bug affecting the accuracy of the Stokes parameter derivatives  $\partial X/\partial\theta$ ,  $\partial^2 X/(\partial\theta\partial\phi\sin\theta)$ ,  $\partial^2 X/\partial\theta^2$ , for X=Q,U has been corrected. See "Fortran Facilities" Appendix for details.

# Changes between release 2.0 and 2.13

- New functions in version 2.13:
  - get\_healpix\_data\_dir, get\_healpix\_main\_dir, get\_healpix\_test\_dir return full path to HEALPix directories.
- New routines in version 2.10:
  - alm2map\_spin: synthesis of maps of arbitrary spin
  - map2alm\_iterative: iterative analysis of map
  - map2alm\_spin: analysis of maps of arbitrary spin
  - healpix\_modules: meta-module
  - write\_minimal\_header: routine to write minimal FITS header

 parse\_check\_unused: prints out parameters present in parameter file but not used by the code.

#### • Improved routines:

- query\_strip: the inclusive option now returns *all* (and only) the pixels overlapping, even partially, with the strip
- query\_disc: when the disc center is on one of the poles, *only* the pixels overlapping with the disc are now returned.
- remove\_dipole: can now deal with non-uniform pixel weights.
- parse\_init: silent mode
- parse\_string: can expand environment variables (\${XXX}) and leading ~/

# Changes between release 1.2 and 2.0

Some new features have been added

- Most routines dealing with maps and  $a_{\ell m}$  (eg, create\_alm, map2alm, alm2map, convert\_inplace, convert\_nest2ring, udgrade\_nest, udgrade\_ring) or inputting or outputting data (read\_\*, write\_\*) now accept both single and double precision arguments.
- The routines map2alm and remove\_dipole can now deal with non-symmetric azimuthal cut sky. For backward compatibility, the former calling sequence is still accepted.
- most routines are now parallelized with OpenMP (for shared memory architecture), and some of them are also parallelized with MPI (for distributed memory architecture)

Some new routines have been introduced since version 1.2, as listed below.

- New routines in version 2.0
  - add\_dipole
  - alm2cl
  - alm2map\_der
  - fits2cl (replaces read\_asctab)
  - nside2ntemplates
  - plm\_gen
  - rand\_gauss, rand\_init, rand\_uni

- same\_shape\_pixels\_nest, same\_shape\_pixels\_ring
- template\_pixel\_nest, template\_pixel\_ring
- write\_plm (replaces write\_dbintab)
- New modules or modules with new name
  - misc\_utils: fatal\_error, assert\_assert\_present, assert\_not\_present, assert\_alloc, file\_present, assert\_directory\_present, string strupcase strlowcase, upcase, low-case, wall\_clock\_time, brag\_openmp
  - rngmod: rand\_gauss, rand\_init, rand\_uni
- The following routines are superseded.
  - read\_asctab (replaced by fits2cl)
  - write\_dbintab (replaced by write\_plm)

# Changes between release 1.1 and 1.2

Some new routines have been introduced since version 1.1, as listed below.

- New routines in version 1.2
  - angdist
  - complex\_fft
  - concatnl
  - del\_card
  - get\_card
  - getargument
  - getenvironment
  - $input\_tod*$
  - nArguments
  - parse\_double, parse\_init, parse\_lgt, parse\_long, parse\_real, parse\_string (see parse\_xxx)
  - query\_disc (replaces getdisc\_ring)
  - query\_polygon
  - query\_strip
  - query\_triangle

- read\_fits\_cut4
- real\_fft
- scan\_directories
- surface\_triangle
- vect\_prod
- write\_bintabh
- write\_fits\_cut4
- New modules or modules with new name
  - the modules extension (C extensions), healpix\_fft (FFT operations), paramfile\_io (parameter parsing) have been introduced,
  - the module wrap\_fits has been renamed head\_fits to reflect its extended capabilities in manipulating FITS headers.
- The following routines are superseded. They have been moved to the obsolete module.
  - ask\_inputmap, ask\_outputmap, ask\_lrange (initially in fitstools module)
  - setpar, getpar, anafast\_parser, anafast\_setpar, anafast\_getpar, hotspots\_parser, hotspots\_setpar, hotspots\_getpar, udgrade\_parser, udgrade\_setpar, udgrade\_getpar, smoothing\_parser, smoothing\_setpar, smoothing\_getpar (initially in utilities module).

# add\_card

#### Location in HEALPix directory tree: src/f90/mod/head\_fits.F90

This routine writes a keyword of any kind into a FITS header. It is a wrapper to other routines that write keywords of different kinds.

## $\mathbf{FORMAT}$

call add\_card(header, kwd, value [, comment, update])

Arguments appearing in *italic* are optional.

name & dimensionality	kind	in/out	description
header(LEN=80) DIMENSION(:)	CHR	INOUT	The header to write the keyword to.
kwd(LEN=*)	CHR	IN	the FITS keyword to write. Should be shorter or equal to 8 characters.
value	any	IN	the value to give to the keyword.
comment(LEN=*)	CHR	IN	comment to the keyword.
update	LGT	IN	if set to .true., the first occurence of the keyword kwd in header will be updated (and all other occurences removed); otherwise, the keyword will be appended at the end (and any previous occurence removed). If the keyword is either 'HISTORY' or 'COMMENT', update is ignored and the keyword is peacefully appended at the end of the header.

add\_card 11

#### **EXAMPLE:**

```
character(len=80), dimension(1:120) :: header
header = '' ! very important
call add_card(header,'NSIDE',256,'the nside of the map')
```

Gives the keyword 'NSIDE' the value 256 in the given headerstring. It is important to make sure that the header string array is empty before attempting to write anything in it.

#### MODULES & ROUTINES

This section lists the modules and routines used by add\_card.

 $write_hl$ more general routine for adding a keyword to a

header.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to add\_card.

write_minimal_header	routine to write <b>HEALPix</b> compliant baseline
	FITS header

general purpose routine to read any keywords get\_card

from a header in a FITS file.

routine to discard a keyword from a FITS header del\_card read\_par, number\_of\_alms

routines to read specific keywords from a header

in a FITS file.

getsize\_fits function returning the size of the data set in a fits

file and reading some other useful FITS keywords

merge\_headers routine to merge two FITS headers

# add\_dipole\*

Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

This routine provides a means to add a monopole and dipole to a **HEALPix** map.

FORMAT call add\_dipole\*(nside, map, ordering, degree, multipoles [, fmissval])

name & dimensionality	kind	in/out	description
nside	I4B	IN	value of $N_{\text{side}}$ resolution parameter for input map
map(0:12*nside*nside-1)	SP/ DP	INOUT	<b>HEALPix</b> map to which the monopole and dipole will be added. Those are added to all unflagged pixels.
ordering	I4B	IN	<b>HEALPix</b> scheme 1:RING, 2: NESTED
degree	I4B	IN	multipoles to add. It is either 0 (nothing done), 1 (monopole only) or 2 (monopole and dipole)
multipoles(0:degree*degree-1)	DP	IN	values of monopole and dipole to add. The monopole is described as a scalar in the same units as the input map, the dipole as a 3D cartesian vector, in the same units.
fmissval (OPTIONAL)	SP/ DP	IN	value used to flag bad pixel on input ( <b>default:</b> -1.6375e30). Pixels with that value are left unchanged.

add\_dipole\*

#### **EXAMPLE:**

call add\_dipole\*(128, map, 1, 2, (\ 10.0\_dp, 0.0\_dp, 1.2\_dp, 0.0\_dp \))

map is a **HEALPix** map of resolution  $N_{\text{side}} = 128$ , with the RING ordering scheme. A monopole of amplitude 10 and a dipole of amplitude 1.2 and directed along the y axis will be added to it.

#### MODULES & ROUTINES

This section lists the modules and routines used by add\_dipole\*.

pix\_tools module, containing:

#### RELATED ROUTINES

This section lists the routines related to add\_dipole\*.

remove\_dipole routine to remove the best fit monopole and

monopole from a map.

# alm2cl\*

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine computes the auto (or cross) power spectra of a one (or two) sets of spherical harmonics coefficients  $a_{\ell m}$ .  $C_{12}(\ell) = \sum_{m=-\ell}^{\ell} a_{1,\ell m} a_{2,\ell m}^* / (2\ell+1)$ 

### **FORMAT**

call alm2cl\*(nlmax, nmmax, alm1, [alm2,] cl)

name & dimensionality	kind	in/out	description
nlmax	I4B	IN	the maximum $\ell$ value used for the
nmmax	I4B	IN	$a_{lm}$ . the maximum $m$ value used for the
alm1(1:p, 0:nlmax, 0:nmmax)	SPC/ DPC	IN	$a_{lm}$ . First set of $a_{lm}$ values. $p$ is 3 or 1 depending on wether polarisation is included or not. In the former case, the first index runs from 1 to 3 corresponding to $(T,E,B)$ .
alm2(1:p, 0:nlmax, 0:nmmax) (OPTIONAL)	SPC/ DPC	IN	Second set of $a_{lm}$ values.
cl(0:nlmax,1:d)	SP/ DP	OUT	resulting auto or cross power spectra. If both alm1 and alm2 are present, c1 will be their cross power spectrum. If only alm1 is present, c1 will be its power spectrum. If $d=1$ , only the temperature spectrum $C_l^T$ will be output. If $d=4$ and $p=3$ , the output will be $C_l^T$ , $C_l^E$ , $C_l^B$ , $C_l^{T\times E}$ , and if $d\geq 6$ and $p=3$ , $C_l^{T\times B}$ $C_l^{E\times B}$ will also be output.

 $alm2cl^*$ 

#### **EXAMPLE:**

```
lmax = 128 ; mmax = lmax
call alm2cl(lmax, mmax, alm1, cl_auto)
call alm2cl(lmax, mmax, alm1, alm2, cl_cross)
```

cl\_auto will contain the (auto) power spectrum of the  $a_{\ell m}$  coefficients alm1 up to  $\ell=128$ , while cl\_cross will be the cross power spectra of the two sets of  $a_{\ell m}$  coefficients alm1 and alm2.

#### MODULES & ROUTINES

This section lists the modules and routines used by alm2cl\*.

none

#### RELATED ROUTINES

This section lists the routines related to alm2cl\*.

map2alm routine extracting the  $a_{\ell m}$  coefficients from a

**HEALPix** map

create\_alm routine to generate randomly distributed  $a_{\ell m}$  co-

efficients according to a given power spectrum

# alm2map\*

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine is a wrapper to 10 other routines: alm2map\_sc\_X, alm2map\_sc\_pre\_X, alm2map\_pol\_x, alm2map\_pol\_pre1\_X, alm2map\_pol\_pre2\_X, where X stands for either s or d. These routines synthesize a **HEALPix** RING ordered temperature map (and if specified, polarisation maps) from input  $a_{lm}^T$  (and if specified  $a_{lm}^E$  and  $a_{lm}^B$ ) values. The different routines are called dependent on what parameters are passed. Some routines synthesize maps with or without precomputed harmonics and some with or without polarisation. The routines accept both single and double precision arrays for alm\_TGC and map\_TQU. The precision of these arrays should match.

FORMAT	call	alm2map*(nsmax,	nlmax,	nmmax,
	$alm_{-}$	TGC, map_TQU [, pln	n])	

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	the $N_{side}$ value of the map to synthesize.
nlmax	I4B	IN	the maximum $\ell$ value used for
nmmax	I4B	IN	the $a_{lm}$ . the maximum $m$ value used for the $a_{lm}$ .
alm_TGC(1:p, 0:nlmax, 0:nmmax)	SPC or DPC	IN	The $a_{lm}$ values to make the map from. $p$ is 3 or 1 depending on wether polarisation is respec- tively included or not. In the former case, the first index runs from 1 to 3 corresponding to (T,E,B).

 $alm2map^*$ 

$map_TQU(0:12*nsmax**2-1)$	SP	OUT	if only a temperature map is to
	or		be synthesized, the map-array
	DP		should be passed with this rank.
$map_TQU(0:12*nsmax**2-1, 1:3)$	SP	OUT	if both temperature an polar-
	or		isation maps are to be syn-
	DP		thesized, the map array should
			have this rank, where the sec-
			ond index is $(1,2,3)$ correspond-
			ing to $(T,Q,U)$ .
$plm(0:n_plm-1),$	DP	IN	If this optional matrix is
OPTIONAL			passed with this rank, pre-
			computed $P_{lm}(\theta)$ are used
			instead of recursion. ( $n_{-}plm =$
			nsmax*(nmmax+1)*(2*nlmax-
			nmmax+2)
$plm(0:n_plm-1,1:3),$	DP	IN	If this optional matrix is passed
OPTIONAL			with this rank, precomputed
			$P_{lm}(\theta)$ AND precomputed
			tensor harmonics are used
			instead of recursion. $(n_plm =$
			nsmax*(nmmax+1)*(2*nlmax-1)*
			nmmax+2)
			nmmax+2)

#### **EXAMPLE:**

```
use healpix_types
use pix_tools, only : nside2npix
use alm_tools, only : alm2map
integer(I4B) :: nside, lmax, mmax, npix, n_plm
real(SP), dimension(:,:), allocatable :: map
complex(SPC), dimension(:,:), allocatable :: alm
real(DP), dimension(:,:), allocatable :: plm
...
nside=256; lmax=512; mmax=lmax
npix=nside2npix(nside)
n_plm=nside*(mmax+1)*(2*lmax-mmax+2)
allocate(alm(1:3,0:lmax,0:mmax))
allocate(map(0:npix-1,1:3))
allocate(plm(0:n_plm-1,1:3))
...
call alm2map(nside, lmax, mmax, alm, map, plm)
```

Make temperature and polarisation maps from the scalar and tensor  $a_{lm}$  passed in alm. The maps have  $N_{side}$  of 256, and are constructed from  $a_{lm}$  values up to 512 in  $\ell$  and m. Since the optional plm array is passed with both precomputed  $P_{lm}(\theta)$  AND tensor harmonics, there will be no recursions in the routine and execution will be faster.

#### MODULES & ROUTINES

This section lists the modules and routines used by alm2map\*.

ring\_synthesis Performs FFT over m for synthesis of the rings.

compute\_lam\_mm, get\_pixel\_layout, gen\_lamfac,gen\_mfac, gen\_normpol, gen\_recfac, init\_rescale, l\_min\_ylm

it\_rescale, l\_min\_ylm Ancillary routines used for  $Y_{\ell m}$  recursion

misc\_utils module, containing:

assert\_alloc routine to print error message, when an array can

not be allocated properly

#### RELATED ROUTINES

This section lists the routines related to alm2map\*.

alm2map\_der routine generating a map and its derivatives from

its  $a_{\ell m}$ 

alm2map\_spin routine generating maps of arbitrary spin from

their  $_sa_{\ell m}$ 

smoothing executable using alm2map\* to smooth maps

synfast executable using alm2map\* to synthesize maps.

map2alm routine performing the inverse transform of

alm2map\*.

create\_alm routine to generate randomly distributed  $a_{\ell m}$  co-

efficients according to a given power spectrum

pixel\_window, generate\_beam return the l-space **HEALPix** -pixel and beam

window function respectively

alter\_alm modifies  $a_{lm}$  to emulate effect of real space filtering

alm2map\_der\*

# $alm2map_der*$

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine is a wrapper to four other routines that synthesize a **HEALPix** temperature (and polarisation) map(s), its (their) first derivatives, and optionally its (their) second derivatives. The routines accept both single and double precision arrays for alm, map, der1 and der2. The precision of these arrays should match. All maps produced are RING ordered.

See "Fortran Facilities" Appendix for a note on a bug affecting the calculation of polarisation derivatives on past versions of this routine.

# FORMAT call alm2map\_der\*(nsmax, nlmax, nmmax, alm, map, der1 [, der2])

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	the $N_{side}$ value of the map to synthesize.
nlmax	I4B	IN	the maximum $\ell$ value used for the
nmmax	I4B	IN	$a_{lm}$ . the maximum $m$ value used for the
alm(1:p, 0:nlmax, 0:nmmax)	SPC/ DPC	IN	$a_{lm}$ . The $a_{lm}$ values to make the map from. p is either 1 (temperature+polarisation).
map(0:12*nsmax**2-1) or $(0:12*nsmax**2-1,1:3)$	SP/ DP	OUT	temperature map $T(p)$ or temperature + polarisation maps $T(p)$ , $Q(p)$ , $U(p)$ to be synthesized.
der1(0:12*nsmax**2-1, 1:2*p)	SP/ DP	OUT	contains on output the first derivatives of T: $(\partial T/\partial \theta, \partial T/\partial \phi/\sin \theta)$ or the interleaved derivatives of T, Q, and U: $(\partial T/\partial \theta, \partial Q/\partial \theta, \partial U/\partial \theta; \partial T/\partial \phi/\sin \theta,)$
der2(0:12*nsmax**2-1,1:3*p), OPTIONAL	SP/ DP	OUT	If this optional matrix is passed with this rank, it will contain on output the second derivatives $(\partial^2 T/\partial \theta^2, \partial^2 T/\partial \theta \partial \phi/\sin \theta, \partial^2 T/\partial \phi^2/\sin^2 \theta)$ or $(\partial^2 T/\partial \theta^2, \partial^2 Q/\partial \theta^2, \partial^2 Q/\partial \theta^2, \ldots)$

#### **EXAMPLE:**

```
use healpix_types
use pix_tools, only : nside2npix
use alm_tools, only : alm2map_der
integer(I4B) :: nside, lmax, mmax, npix, n_plm
real(SP), dimension(:), allocatable :: map
real(SP), dimension(:,:), allocatable :: der1, der2
complex(SPC), dimension(:,:,:), allocatable :: alm
...
nside=256; lmax=512; mmax=lmax
npix=nside2npix(nside)
allocate(alm(1:1,0:lmax,0:mmax))
allocate(map(0:npix-1))
```

alm2map\_der\*

```
allocate(der1(0:npix-1,1:2), der2(0:npix-1,1:3))
...
call alm2map_der(nside, lmax, mmax, alm, map, der1, der2)
```

Make temperature maps and its derivatives from the  $a_{lm}$  passed in alm. The maps have  $N_{side}$  of 256, and are constructed from  $a_{lm}$  values up to 512 in  $\ell$  and m.

#### MODULES & ROUTINES

This section lists the modules and routines used by alm2map\_der\*.

routine to print error message, when an array can not be allocated properly

#### RELATED ROUTINES

This section lists the routines related to alm2map\_der\*.

alm2map routine generating maps of temperature and po-

larisation from their  $a_{\ell m}$ 

alm2map\_spin routine generating maps of arbitrary spin from

their  $sa_{\ell m}$ 

synfast executable using alm2map\_der\* to synthesize

maps.

create\_alm routine to generate randomly distributed  $a_{\ell m}$  co-

efficients according to a given power spectrum

# alm2map\_spin\*

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine produces the maps of arbitrary spin s and -s given their alm coefficients. A (complex) map S of spin s is a linear combination of the spin weighted harmonics  $_sY_{lm}$ 

$${}_{s}S(p) = \sum_{lm} {}_{s}a_{lm} \quad {}_{s}Y_{lm}(p) \tag{1}$$

for  $l \ge |m|, l \ge |s|$ , and is such that  ${}_sS^* = {}_{-s}S$ . alm2map\_spin\* expects the alm coefficients to be provided as

$$|s|a_{lm}^{+} = -(|s|a_{lm} + (-1)^{s} - |s|a_{lm})/2$$
 (2)

$$a_{|s|}a_{lm}^- = -(a_{|s|}a_{lm} - (-1)^s - a_{|s|}a_{lm})/(2i)$$
 (3)

for  $m \ge 0$ , knowing that, just as for spin 0 maps, the coefficients for m < 0 are given by

$$|s|a_{l-m}^+ = (-1)^m |s|a_{lm}^{+*},$$
 (4)

$$a_{ls}^{-}a_{l-m}^{-} = (-1)^{m}{}_{|s|}a_{lm}^{-*}.$$
 (5)

The two (real) maps produced by alm2map\_spin\* are defined respectively as

$$|s|S^{+} = (|s|S + -|s|S)/2$$
 (6)

$$|s|S^- = (|s|S - -|s|S)/(2i).$$
 (7)

With these definitions,  ${}_2a^+, {}_2a^-, {}_2S^+$  and  ${}_2S^-$  match **HEALPix** polarization  $a^E, a^B, Q$  and U respectively. However, for  $s=0, {}_0a^+_{lm}=-a^T_{lm}, {}_0a^-_{lm}=0, {}_0S^+=T, {}_0S^-=0.$ 

# **FORMAT**

call alm2map\_spin\*(nsmax, nlmax, nmmax, spin, alm, map)

alm2map\_spin\*

name & dimensionality	kind in/out	description
nsmax	I4B IN	the $N_{side}$ value of the map to synthesize.
nlmax	I4B IN	the maximum $\ell$ value used for the
nmmax	I4B IN	$a_{lm}$ . the maximum $m$ value used for the
spin	I4B IN	$a_{lm}$ . spin s of the maps to be generated (only its absolute value is relevant).
alm(1:2, 0:nlmax, 0:nmmax)	SPC/ IN	The $_{ s }a_{lm}^{+}$ and $_{ s }a_{lm}^{-}$ values to make
map(0:12*nsmax**2-1, 1:2)	DPC SP/ OUT DP	the map from. $ s S^+$ and $ s S^-$ output maps

#### **EXAMPLE:**

```
use healpix_types
use pix_tools, only : nside2npix
use alm_tools, only : alm2map_spin
integer(I4B) :: nside, lmax, mmax, npix, spin
real(SP), dimension(:,:), allocatable :: map
complex(SPC), dimension(:,:,:), allocatable :: alm
...
nside=256 ; lmax=512 ; mmax=lmax ; spin=4
npix=nside2npix(nside)
allocate(alm(1:2,0:lmax,0:mmax))
allocate(map(0:npix-1,1:2))
...
call alm2map_spin(nside, lmax, mmax, spin, alm, map)
```

Make spin-4 maps from the  $a_{lm}$  passed in alm. The maps have  $N_{side}$  of 256, and are constructed from  $a_{lm}$  values up to 512 in  $\ell$  and m.

#### MODULES & ROUTINES

This section lists the modules and routines used by alm2map\_spin\*.

ring\_synthesis Performs FFT over m for synthesis of the rings. compute\_lam\_mm, get\_pixel\_layout,

gen\_lamfac\_der, gen\_mfac\_spin, do\_lam\_lm\_spin,

gen\_recfac\_spin, init\_rescale, l\_min\_ylm Ancillary routines used for

 $Y_{\ell m}$  recursion

misc\_utils module, containing:

assert\_alloc routine to print error message, when an array can

not be allocated properly

#### RELATED ROUTINES

This section lists the routines related to alm2map\_spin\*.

alm2map routine generating maps of temperature and po-

larisation from their  $a_{\ell m}$ 

alm2map\_der routine generating maps of temperature and po-

larisation, and their spatial derivatives, from their

 $a_{\ell m}$ 

map2alm\_spin routine performing the inverse transform of

alm2map.

create\_alm routine to generate randomly distributed  $a_{\ell m}$  co-

efficients according to a given power spectrum

alms2fits\*

# alms2fits\*

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine stores  $a_{lm}$  values in a binary FITS file. Each FITS file extension created will contain one integer column with  $index = \ell^2 + \ell + m + 1$ , and 2 or 4 single (or double) precision columns with real/imaginary  $a_{lm}$  values and real/imaginary standard deviation. One can store temperature  $a_{lm}$  or temperature and polarisation,  $a_{lm}^T$ ,  $a_{lm}^E$  and  $a_{lm}^B$ . If temperature is specified, a FITS file with one extension is created. If polarisation is specified, a FITS file with 3 extensions one for each set of  $a_{lm}$ ,  $a_{lm}^T$ ,  $a_{lm}^E$  and  $a_{lm}^B$  is created.

# FORMAT call alms2fits\*(filename, nalms, alms, ncl, header, nlheader, next)

name & dimensionality	kind	in/oı	utdescription
filename(LEN=filenamelen)	CHR	IN	filename for the FITS file to store
,			the $a_{lm}$ in.
nalms	I4B	IN	number of $a_{lm}$ to store.
ncl	I4B	IN	number of columns in the FITS file.
			If an standard deviation is given,
			this number is 5, otherwise it is 3.
next	I4B	IN	the number of extensions. 1 for tem-
			perature only, 3 for temperature and
			polarisation.

name & dimension	ality	kind	in/o	utdescription
alms(1:nalms,1:ncl+1	,1:next)	SP/ DP	IN	the $a_{lm}$ to write to the file. alms(i,1,j) and alms(i,2,j) contain the $\ell$ and $m$ values for the ith $a_{lm}$ (j=1,2,3 for (T,E,B)). alms(i,3,j) and alms(i,4,j) contain the real and imaginary value of the ith $a_{lm}$ . Finally, the standard deviation for the ith $a_{lm}$ is contained in alms(i,5,j) (real) and alms(i,6,j) (imaginary).
nlheader		I4B	IN	number of header lines to write to
header(LEN=80) 1:next)	(1:nlheader,	CHR	IN	the file. the header to the FITS file.

### **EXAMPLE:**

call alms2fits ('alms.fits', 65\*66/2, alms, 3, header, 80, 3)

Creates a FITS file with the  $a_{lm}^T$ ,  $a_{lm}^E$  and  $a_{lm}^B$  values given in alms(1:65\*66/2,1:4,1:3). The last index specifies (T,E,B). The second index gives l, m, real( $a_{lm}$ ), imaginary( $a_{lm}$ ) for each of the  $a_{lm}$ . The number 65\*66/2 is the number of  $a_{lm}$  values up to an  $\ell$  value of 64. 80 lines from header(1:80,1:3) is written to each extension.

#### MODULES & ROUTINES

This section lists the modules and routines used by alms2fits\*.

write_alms	routine called by alms2fits* for each extension.
fitstools	module, containing:
printerror	routine for printing FITS error messages.
${f cfitsio}$	library for FITS file handling.

alms2fits\* 27

### RELATED ROUTINES

This section lists the routines related to alms2fits\*.

fits 2<br/>alms, read\_conbintab <br/> routines to read  $a_{lm}$  from a FITS file

dump\_alms has the same function as alms2fits\* but with pa-

rameters passed differently.

# alter\_alm\*

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine modifies scalar (and tensor)  $a_{\ell m}$  by multiplying them by a beam window function described by a FWHM (in the case of a gaussian beam) or read from an external file (in the more general case of a circular beam)  $a_{\ell m} \longrightarrow a_{\ell m} b(\ell)$ . It can also be used to multiply the  $a_{\ell m}$  by an arbitray function of  $\ell$ .

# FORMAT

call alter\_alm\*(nsmax, nlmax, nmmax, fwhm\_arcmin, alm\_TGC [, beam\_file, window])

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	$N_{\text{side}}$ resolution parameter of the map associated with the $a_{lm}$ considered. Currently has no effect on the routine.
nlmax nmmax	I4B I4B	IN IN	maximum $\ell$ value for the $a_{\ell m}$ . maximum $m$ value for the $a_{\ell m}$ .
$fwhm_arcmin$	SP/ DP	IN	fwhm size of the gaussian beam in arcminutes.
alm_TGC(1:p,0:nlmax,0:nmmax)	SPC/ DPC	INOUT	complex $a_{\ell m}$ values to be altered. The first index here runs from 1:1 for temperature only, and 1:3 for polarisation. In the latter case, 1=T, 2=E, 3=B.

alter\_alm\*

beam_file(LEN=filenamelen) (OPTIONAL)	CHR	IN	name of the file containing the (non necessarily gaussian) window function $B_{\ell}$ of a circular beam. If present, it will override the argument fwhm arcmin.
window(0:nlw,1:d) (OPTIONAL)	SP/ DP	IN	arbitrary window by which to multiply the $a_{\ell m}$ . If present, it overrides both fwhm_arcmin and beam_file. If nlw < nlmax, the $a_{\ell m}$ with $\ell \in \{\text{nlw+1,nlmax}\}$ are set to 0, and a warning is issued. If $d < p$ the window for temperature is replicated for polarisation.

### **EXAMPLE:**

call alter\_alm(64, 128, 128, 1, 5.0, alm\_TGC)

Alters scalar and tensor  $a_{lm}$  of a map with  $N_{\rm side} = 64$ ,  $\ell_{\rm max} = m_{\rm max} = 128$  by multiplying them by the beam window function of a gaussian beam with FWHM = 5 arcmin.

### MODULES & ROUTINES

This section lists the modules and routines used by alter\_alm\*.

${ m alm\_tools}$	module, containing:
$generate\_beam$	routine to generate beam window function
$pixel\_window$	routine to generate pixel window function

#### RELATED ROUTINES

This section lists the routines related to alter\_alm\*.

$create\_alm$	Routine to create $a_{\ell m}$ coefficients.
$rotate\_alm$	Routine to rotate $a_{\ell m}$ coefficients between 2 different arbitrary coordinate systems.
map2alm	Routines to analyze a <b>HEALPix</b> sky map into its $a_{\ell m}$ coefficients.

alm2map Routines to synthetize a **HEALPix** sky map from

its  $a_{\ell m}$  coefficients.

ang2vec 31

# ang2vec

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to convert the position angles  $(\theta, \phi)$  of a point on the sphere into its 3D position vector (x, y, z) with  $x = \sin \theta \cos \phi$ ,  $y = \sin \theta \sin \phi$ ,  $z = \cos \theta$ .

**FORMAT** 

call ang2vec(theta, phi, vector)

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
theta	DP	IN	colatitude in radians measured southward from north pole (in
phi	DP	IN	$[0, \pi]$ ). longitude in radians measured eastward (in $[0, 2\pi]$ ).
vector(3)	DP	OUT	three dimensional cartesian position vector $(x, y, z)$ normalised to unity. The north pole is $(0, 0, 1)$

#### RELATED ROUTINES

This section lists the routines related to ang2vec.

vec2ang

converts the 3D position vector of point into its position angles on the sphere.

# angdist

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Returns the angular distance in radians between two vectors. The input vectors do not have to be normalised. For almost colinear or anti-colinear vectors, renders numerically more accurate results than the  $\cos^{-1}$  of the scalar product.

#### **FORMAT**

call angdist(v1, v2, dist)

#### ARGUMENTS

name & dimension-	kind	in/out	description
ality			
v1(3) v2(3) dist	DP DP DP	IN IN OUT	cartesian vector. cartesian vector. angular distance in radians between the 2 vectors.

#### **EXAMPLE:**

```
use healpix_types
use pix_tools, only : angdist
real(DP) :: dist, one = 1.0_dp
call angdist((/1,2,3/)*one, (/1,2,4/)*one, dist)
print*, dist
```

Returns the angular distance between 2 vectors.

#### RELATED ROUTINES

This section lists the routines related to **angdist**.

vect\_prod computes the vector product between two 3D vectors

angdist 33

# assert\_alloc, assert\_directory\_present, ...

#### Location in HEALPix directory tree: src/f90/mod/misc\_utils.F90

The Fortran90 module misc\_utils contains a few routines to test an assertion and return an error message if it is false.

#### **FUNCTIONS:**

call assert(test [, msg, errcode])

if test is true, proceeds with normal code execution. If test is false, issues a standard error message (unless msg is provided) and stops the code execution with the status errcode (or 1 by default).

call assert\_alloc(status, code, array)

if status is 0, proceeds with normal code execution. If not, issues an error message indicating a problem during memory allocation of array in program code, and stops the code execution.

call assert\_directory\_present(directory)

issues an error message and stops the code execution if the directory named directory can not be found

call assert\_present(filename)

issues an error message and stops the code execution if the file named filename can not be found.

call assert\_not\_present(filename)

issues an error message and stops the code execution if a file with name filename already exists.

### **ARGUMENTS**

name & di	mensionality	kind	in/out	description
test msg errorcode	OPTIONAL OPTIONAL	LGT CHR I4B	IN IN IN	result of a logical test character string describing nature of error error status given to code interruption
status		I4B	IN	value of the stat flag returned by the F90
code		CHR	IN	allocate command name of program or code in which alloca- tion is made
array		CHR	IN	name of array allocated
directory		CHR	IN	directory name (contains a '/')
filename		CHR	IN	file name

#### **EXAMPLE:**

```
program my_code
use misc_utils
real, allocatable, dimension(:) :: vector
integer :: status
real :: a = -1.

allocate(vector(12345), stat=status)
call assert_alloc(status, 'my_code', 'vector')

call assert_directory_present('/home')

call assert(a > 0., 'a is NEGATIVE !!!')
end program my_code
```

Will issue a error message and stops the code if vector can not be allocated, will stop the code if '/home' is not found, and will stop the code and complain loudly about it because a is actually negative.

# brag\_openmp

Location in HEALPix directory tree: src/f90/mod/misc\_utils.F90

If compiled with shared memory libraries (OpenMP), this routine prints out the number of CPUs used (controlled by the environment variable OMP\_NUM\_THREADS) and the number of CPUs available.

### **FORMAT**

call brag\_openmp()

#### **EXAMPLE:**

use misc\_utils
call brag\_openmp()

Will print out:

-----

Number of OpenMP threads in use: 2 Number of CPUs available: 2

\_\_\_\_\_\_

on bi-pro (or dual core) computer

complex\_fft 37

# complex\_fft

### Location in HEALPix directory tree: src/f90/mod/healpix\_fft.F90

This routine performs a forward or backward Fast Fourier Transformation on its argument data.

**FORMAT** 

call complex\_fft(data, backward)

# **ARGUMENTS**

name&dimensionality	kind in/out	description
data(:)	XXX INOUT	array containing the input and output data. It can be of type real(sp), real(dp), complex(spc) or complex(dpc). If it is of
backward	LGT IN	type real, it is interpreted as an array of size(data)/2 complex variables.  Optional argument. If present and true, perform backward transformation, else forward

# **EXAMPLE:**

use healpix\_fft
call complex\_fft (data, backward=.true.)

Performs a backward FFT on data.

### RELATED ROUTINES

This section lists the routines related to **complex\_fft**.

real\_fft routine for FFT of real data

# compute\_statistics\*

 $Location \ in \ HEALPix \ directory \ tree: \ src/f90/mod/statistics.f90$ 

This routine computes the min, max, absolute deviation and first four order moment of a data set

**FORMAT** 

call compute\_statistics\*(data ,stats [, badval])

# **ARGUMENTS**

name & dimensionality	kind	in/outdescription		
data(:)	SP/	IN	data set	
data(.)	DP	111	uata set	
stats	tstats	OUT	structure containing the statistics of the data.	
			The respective fields (stats%field) are:	
$\operatorname{ntot}$	I4B	_	total number of data points	
nvalid	I4B	_	number $n$ of valid data points	
mind, maxd	DP	_	minimum and maximum valid data	
average	DP	_	average of valid points $m = \sum x/n$	
absdev	DP	_	absolute deviation $a = \sum  x - m /n$	
var	DP	_	variance $\sigma^2 = \sum (x-m)^2/(n-1)$	
${ m rms}$	DP	_	standard deviation $\sigma$	
skew	DP	_	skewness factor $s = \sum (x - m)^3 / (n\sigma^3)$	
kurt	DP	_	kurtosis factor $k = \sum (x - m)^4 / (n\sigma^4) - 3$	
badval	SP/	IN	sentinel value given to bad data points. Data	
(OPTIONAL)	$\overrightarrow{\mathrm{DP}}$		points with this value will be ignored during	
,			calculation of the statistics. If not set, all	
			points will be considered. Do not set to 0!.	

### **EXAMPLE:**

use statistics, only: compute\_statistics, print\_statistics, tstats

type(tstats) :: stats

. . .

compute\_statistics(map, stats)
print\*,stats%average, stats%rms
print\_statistics(stats)

Computes the statistics of map, prints its average and rms and prints the whole list of statistical measures.

# RELATED ROUTINES

This section lists the routines related to **compute\_statistics\***.

median routine to compute median of a data set

# concatnl

## Location in HEALPix directory tree: src/f90/mod/paramfile\_io.F90

Function to concatenate up to 10 subtrings interspaced with LineFeed character. Upon printing each subtring will be on a different line.

FORMAT var=concatnl(string1[, string2, string3, ...])

### **ARGUMENTS**

name & dimensionality	kind	in/out	description
string1 string2	CHR CHR		the first substring to be concatenated. the second substring (if any) to be con-
string3	CHR	optional	catenated up to 10 substrings can be concate-
var	CHR	optional OUT	nated. concatenation of the substrings inter- spaced with LineFeed character.

### **EXAMPLE:**

# RELATED ROUTINES

This section lists the routines related to **concatnl**.

parse\_xxx parse an ASCII file for parameters definition

concatnl 41

# convert\_inplace\*

## Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to convert a **HEALPix** map from NESTED to RING scheme or vice versa. The conversion is done inplace, meaning that it doesn't require memory for a temporary map, like the *convert\_nest2ring* or *convert\_ring2nest* routines. But for that reason, this routine is slower and not parallelized. The routine is a wrapper for 6 different routines and can threfore process integer, single precision and double precision maps as well as mono or bi dimensional arrays.

# **FORMAT**

call convert\_inplace\*(subcall, map)

### **ARGUMENTS**

nama (z dimonsionality	kind	in /out	description
name & dimensionality	KIIIU	in/out	description
subcall	_	IN	routine to be called by convert_inplace_real. Set this to ring2nest or nest2ring dependent on wether the conversion is RING to NESTED or vice versa.
map(0:npix-1)	I4B/ SP/ DP	INOUT	mono-dimensional full sky map to be converted, the routine finds the size itself.
map(0:npix-1,1:nd)	I4B/ SP/ DP	INOUT	bi-dimensional (nd>0) full sky map to be converted, the routine finds both dimensions itself. Processing a bidimensional map with nd> 1 should be faster than each of the nd 1D-maps consecutively.

convert\_inplace\*

### **EXAMPLE:**

call convert\_inplace(ring2nest,map)

Converts an map from RING to NESTED scheme.

### MODULES & ROUTINES

This section lists the modules and routines used by **convert\_inplace\***.

nest2ring routine to convert a NESTED pixel index to

RING pixel number.

ring2nest routine to convert a RING pixel index to

NESTED pixel number.

## RELATED ROUTINES

This section lists the routines related to **convert\_inplace\***.

convert\_nest2ring convert from NESTED to RING scheme using a

temporary array. Requires more space then con-

vert\_inplace, but is faster.

convert\_ring2nest convert from RING to NESTED scheme using a

temporary array. Requires more space then con-

vert\_inplace, but is faster.

# convert\_nest2ring\*

## Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to convert a **HEALPix** map from NESTED to RING scheme.

The routine is a wrapper for 6 different routines and can threfore process integer, single precision and double precision maps as well as mono or bi dimensional arrays.

This routine is fast, and is parallelized for shared memory architecture, but requires extra memory to store a temporary map in.

# **FORMAT**

call convert\_nest2ring\*(nside, map)

## **ARGUMENTS**

name & dimensionality	kind	in/out	description
nside	I4B	IN	the $N_{side}$ parameter of the map to be converted.
map(0:12*nside**2-1)	I4B/ SP/ DP	INOUT	mono-dimensional full sky map to be converted to RING scheme.
map(0:12*nside**2-1,1:nd)	I4B/ SP/ DP	INOUT	bi-dimensional full sky map to be converted to RING scheme. The routine finds the second di- mension (nd) by itself. Process- ing a bidimensional map with nd> 1 should be faster than each of the nd 1D-maps consec- utively.

### **EXAMPLE:**

call convert\_nest2ring(256,map)

convert\_nest2ring\* 45

Converts an  $N_{side} = 256$  map given in array map from NESTED to RING scheme.

# MODULES & ROUTINES

This section lists the modules and routines used by **convert\_nest2ring\***.

nest2ring

routine to convert a NESTED pixel index to RING pixel number.

### RELATED ROUTINES

This section lists the routines related to **convert\_nest2ring\***.

convert\_ring2nest convert\_inplace

convert between RING and NESTED schemes. convert between NESTED and RING schemes inplace. This routine is slower than convert\_nest2ring\*, but doesn't require as much memory.

# convert\_ring2nest\*

## Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to convert a **HEALPix** map from RING to NESTED scheme.

The routine is a wrapper for 6 different routines and can threfore process integer, single precision and double precision maps as well as mono or bi dimensional arrays.

This routine is fast, and is parallelized for shared memory architecture, but requires extra memory to store a temporary map in.

# **FORMAT**

call convert\_ring2nest\*(nside, map)

## ARGUMENTS

name & dimensionality	kind	in/out	description
nside	I4B	IN	the $N_{side}$ parameter of the map to be converted.
map(0:12*nside**2-1)	I4B/ SP/ DP	INOUT	mono-dimensional full sky map to be converted to RING scheme.
map(0:12*nside**2-1,1:nd)	I4B/ SP/ DP	INOUT	bi-dimensional full sky map to be converted to RING scheme. The routine finds the second di- mension (nd) by itself. Process- ing a bidimensional map with nd> 1 should be faster than each of the nd 1D-maps consec- utively.

### **EXAMPLE:**

call convert\_ring2nest(256,map)

convert\_ring2nest\* 47

Converts an  $N_{side} = 256$  map given in array map from RING to NESTED scheme.

# MODULES & ROUTINES

This section lists the modules and routines used by **convert\_ring2nest\***.

ring2nest

routine to convert a RING pixel index to NESTED pixel number.

### RELATED ROUTINES

This section lists the routines related to **convert\_ring2nest\***.

convert\_nest2ring convert\_inplace convert between NESTED and RING schemes. convert between RING and NESTED schemes inplace. This routine is slower than convert\_ring2nest\*, but doesn't require as much memory.

# coordsys2euler\_zyz

# $Location \ in \ HEALPix \ directory \ tree: \ src/f90/mod/coord\_v\_convert.f90$

This routine returns the three Euler angles  $\psi$ ,  $\theta$ ,  $\varphi$ , corresponding to a rotation between standard astronomical coordinate systems. This angles can then be used in rotate\_alm

# FORMAT call coordsys2euler\_zyz(iepoch, oepoch, isys, osys, psi, theta, phi)

# **ARGUMENTS**

name & dimension-	kind	in/out	description
ality			
iepoch	DP	IN	epoch of the input astronomical coordinate system.
oepoch	DP	IN	epoch of the output astronomical coordinate
			system.
isys(len=*)	CHR	IN	input coordinate system, should be
			one of 'E'=Ecliptic, 'G'=Galactic,
			'C'/'Q'=Celestial/eQuatorial.
osys(len=*)	CHR	IN	output coordinate system, same choice as
			above.
psi	DP	OUT	first Euler angle: rotation $\psi$ about the z-axis.
theta	DP	OUT	second Euler angle: rotation $\theta$ about the orig-
			inal (unrotated) y-axis;
phi	DP	OUT	third Euler angle: rotation $\varphi$ about the orig-
			inal (unrotated) z-axis;

# **EXAMPLE:**

use coord\_v\_convert, only: coordsys2euler\_zyz

use alm\_tools, only: rotate\_alm

. . .

call coordsys2euler\_zyz(2000.0\_dp, 2000.0\_dp, 'E', 'G', psi, theta, phi)

coordsys2euler\_zyz 49

call rotate\_alm(64, alm\_TGC, psi, theta, phi)

Rotate the  $a_{lm}$  from Ecliptic to Galactic coordinates.

# RELATED ROUTINES

This section lists the routines related to **coordsys2euler\_zyz**.

rotate\_alm apply arbitrary sky rotation to a set of  $a_{lm}$  coeffi-

cients.

xcc\_v\_convert rotates a 3D coordinate vector from one astronom-

ical coordinate system to another.

# $create\_alm*$

### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine generates scalar (and tensor)  $a_{lm}$  for a temperature (and polarisation) power spectrum read from an input FITS file. The  $a_{lm}$  are gaussian distributed with a zero mean, and their amplitude is multiplied with the  $\ell$ -space window function of a gaussian beam characterized by its FWHM or an arbitrary circular beam and a pixel window read from an external file.

# **FORMAT**

call create\_alm\*(nsmax, nlmax, nmmax, polar, filename, iseed, fwhm\_arcmin, alm\_TGC, header [, windowfile, units, beam\_file, rng\_handle])

### ARGUMENTS

create\_alm\* 51

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	$N_{side}$ of the map to be synthetized from the $a_{\ell m}$ created by this routine.
nlmax	I4B	IN	maximum $\ell$ value to be considered $(MAX = 3 \times N_{side})$ .
nmmax	I4B	IN	maximum $m$ value for the $a_{\ell m}$ .
polar	I4B	IN	equals 1 if polarisation is used, 0 otherwise.
filename(LEN = filenamelen)	CHR	IN	name of FITS file containing power spectrum.
rng_handle	planc	k_rng INOUT	structure containing information necessary to continue a random sequence initiated previously with the subroutine rand_init. Consecutive calls to create_alm*can be made after a single invocation to rand_init.
$fwhm_arcmin$	SP/ DP	IN	FWHM size of the gaussian beam in arcminutes.

$alm\_TGC(1:p,0:nlmax,0:nmmax)$	SPC/ OUT	complex $a_{\ell m}$ values generated
	DPC	from the powerspectrum in the
		FITS-file. The first index here
		runs form 1:1 for temperature
		only, and 1:3 for polarisation.
		• • • • • • • • • • • • • • • • • • • •
		In the latter case, 1=T, 2=E, 3=B.
header(LEN=80),dimension(60)	CHR OUT	part of header which will be in-
,,,		cluded in the FITS-file contain-
		ing the map synthesised from
		the $a_{\ell m}$ which create_alm gen-
		erates.
windowfile(LEN=filenamelen)	CHR IN	full filename specification of the
,	CIII( IIV	-
(OPTIONAL)		FITS file with the pixel window
(1777 00) 11 (1)	CIID OIIT	function.
units(LEN=80), dimension(1:)	CHR OUT	physical units of the created $a_{\ell m}$
(OPTIONAL)		(square-root of the input power
		spectrum units).
$beam\_file(LEN=filenamelen)$	CHR IN	name of the file containing
(OPTIONAL)		the (non necessarily gaussian)
( )		window function $B_{\ell}$ of a cir-
		cular beam. If present, it
		- ,
		will override the argument
		${ t fwhm\_arcmin.}$

# **EXAMPLE:**

```
use alm_tools, only: create_alm
use rngmod, only: rand_init, rng_handle
type(planck_rng) :: rng_handle

call rand_init(rng_handle, -1)
call create_alm(64, 128, 128, 1, 'cl.fits', rng_handle, 5.0, alm_TGC, header, 'data/pixel_window_n0064.fits')
```

create\_alm\* 53

Creates scalar and tensor  $a_{lm}$  from the power spectrum given in the file 'cl.fits'. The map to be created from these  $a_{lm}$  is assumed to have  $N_{side}=64$ .  $C_{l}$ s from the power spectrum are used up to an  $\ell$  value of 128. Corresponding  $a_{lm}$  values up to l=128 and m=128 are created as gaussian distributed complex numbers. Their are drawn from a sequence of pseudorandom numbers initiated with a seed of -1. The produced  $a_{lm}$  are convolved with a gaussian beam of FWHM 5 arcminutes and a pixel window read from 'data/pixel\_window\_n0064.fits'. It is assumed that after the return from this routine, a map is generated from the created  $a_{lm}$ . For this purpose, header is updated with FITS format information describing the origin and history of these  $a_{lm}$ .

### MODULES & ROUTINES

This section lists the modules and routines used by **create\_alm\***.

$\mathrm{alm\_tools}$	<u>module</u> , containing:
$pow2alm\_units$	routine to convert from power spectrum units to
	$a_{\ell m}$ units
$generate\_beam$	routine to generate beam window function
$pixel\_window$	routine to read in pixel window function
utilities	module, containing:
die_alloc	routine that prints an error message if there is not enough space for allocation of variables.
${f fitstools}$	module, containing:
fits2cl	routine to read a FITS file containing a power spectrum.
$read_dbintab$	routine to read a FITS-binary file containing the pixel window functions.
$\mathbf{head\_fits}$	module, containing:
${\rm add\_card}$	routine to add a keyword to a FITS header.
$\operatorname{get\_card}$	routine to read a keyword value from FITS header.
$merge\_headers$	routine to merge two FITS headers.
$\operatorname{rngmod}$	module, containing:
${ m rand\_gauss}$	function which returns a gaussian distributed ran-

dom number.

# RELATED ROUTINES

This section lists the routines related to **create\_alm\***.

rand\_init subroutine to initiate a random number sequence.

synfast executable using create\_alm\* to synthesize CMB

maps from a given power spectrum.

alm2map Routine to transform a set of  $a_{lm}$  created by cre-

ate\_alm\* to a **HEALPix** map.

alms2fits, dump\_alms Routines to save a set of  $a_{lm}$  in a FITS file.

del\_card 55

# $del_card$

## Location in HEALPix directory tree: src/f90/mod/head\_fits.F90

This routine removes one or several keywords from a FITS header.

## **FORMAT**

call del\_card(header, kwds)

# **ARGUMENTS**

name & dimensionality	kind in/out	description
header(LEN=80)(1:nlheader)	CHR INOUT	The header to remove the keyword(s) from. The routines
kwds(LEN=20)(1:nkws)	CHR IN	finds out the header size. list of FITS keywords to re- move. The routine accepts ei-
kwds(LEN=20)	CHR IN	ther a vector a keywords or a single one in a scalar variable the one FITS keyword to remove.

# EXAMPLES: #1

call del\_card(header,(/ 'NSIDE ','COORD ','ORDERING' /) )

Removes the keywords 'NSIDE', 'COORD' and 'ORDERING' from Header

# EXAMPLES: #2

call del\_card(header, 'ORDERING')

### Removes the keyword 'ORDERING' from Header

### MODULES & ROUTINES

This section lists the modules and routines used by del\_card.

write\_hl more general routine for adding a keyword to a

header.

**cfitsio** library for FITS file handling.

### RELATED ROUTINES

This section lists the routines related to **del\_card**.

add\_card general purpose routine to write any keywords

into a FITS file header

get\_card general purpose routine to read any keywords

from a header in a FITS file.

read\_par, number\_of\_alms routines to read specific keywords from a header

in a FITS file.

getsize\_fits function returning the size of the data set in a fits

file and reading some other useful FITS keywords

merge\_headers routine to merge two FITS headers

 $dump\_alms^*$  57

# dump\_alms\*

### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine stores  $a_{lm}$  values in a binary FITS file. The FITS file created will contain one integer column with  $index = \ell^2 + \ell + m + 1$  and 2 single precision columns with real/imaginary  $a_{lm}$  values. One can store temperature  $a_{lm}$  or polarisation,  $a_{lm}^E$  or  $a_{lm}^B$ . If temperature is specified, a FITS file is created. If polarisation is specified, an old FITS file is opened and extra extensions is created.

# FORMAT call dump\_alms\*(filename, alms, nlmax, header, nlheader, extno)

# **ARGUMENTS**

name & dimensionality	kind in/ou	t description
$\mathrm{filename}(\mathrm{LEN} {=} \mathtt{filenamelen})$	CHR IN	filename for the FITS-file to store the $a_{lm}$ in.
$\begin{array}{l} nlmax \\ alms(0:nlmax,0:nlmax) \end{array}$	I4B IN SPC/ IN	maximum $\ell$ value to store. array with $a_{lm}$ . alms(l,m) cor-
extno	DPC I4B IN	responds to $a_{lm}$ extension number. If 0 is spec-
		ified, a FITS file is created and $a_{lm}$ is stored in the first FITS extension as temperature $a_{lm}$ .
		If 1 or 2 is specified, an already existing file is opened and
		a 2nd or 3rd extension is created, treating $a_{lm}$ as $a_{lm}^E$ or $a_{lm}^B$ .
nlheader	I4B IN	number of header lines to write to the file.
header(LEN=80) (1:nlheader)	CHR IN	the header to the FITS-file.

# **EXAMPLE:**

call dump\_alms ('alms.fits', alms, 64, header, 80, 1)

Opens an already existing FITS file which contains temperature  $a_{lm}$ . An extra extension is added to the file where the  $a_{lm}$  array are written in a three-column format as described above. 80 header lines are written to the file from the array header(1:80).

### MODULES & ROUTINES

This section lists the modules and routines used by dump\_alms\*.

fitstools module, containing:

printerror routine for printing FITS error messages.

**cfitsio** library for FITS file handling.

### RELATED ROUTINES

This section lists the routines related to dump\_alms\*.

fits2alms, read\_conbintab routines to read  $a_{lm}$  from a FITS-file

alms2fits has the same function as dump\_alms\* but is more

general.

fits2alms\*

# fits2alms\*

# Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads  $a_{lm}$  values from a binary FITS file. Each FITS file extension is supposed to contain one integer column with  $index = \ell^2 + \ell + m + 1$  and 2 or 4 single (or double) precision columns with real/imaginary  $a_{lm}$  values and real/imaginary standard deviation. One can read temperature  $a_{lm}$  or temperature and polarisation,  $a_{lm}^T$ ,  $a_{lm}^E$  and  $a_{lm}^B$ .

FORMAT	call fits2alms*(filename,	nalms,	alms,	ncl,
	header, nlheader, next)			

# **ARGUMENTS**

name & dimensionality	kind	in/outdescription
filename(LEN=filenamelen)	CHR	IN filename of the FITS-file to read the $a_{lm}$ from.
nalms ncl	I4B I4B	IN number of $a_{lm}$ to read.  IN number of columns to read in the FITS file. If an standard deviation is to be read, this number is 5, oth-
next	I4B	erwise it is 3.  IN the number of extensions to read. 1 for temperature only, 3 for temperature and polarisation.

alms(1:nalms,1:(ncl+1),	1:next)	SP/	OUT	the $a_{lm}$ to read from the file.
, , , , , , , , , , , , , , , , , , , ,	,	$\overrightarrow{\mathrm{DP}}$		alms(i,1,j) and $alms(i,2,j)$ contain
				the $\ell$ and $m$ values for the ith
				$a_{lm}$ (j=1,2,3 for (T,E,B)). alms(i,3,j)
				and alms(i,4,j) contain the real and
				imaginary value of the ith $a_{lm}$ . Fi-
				nally, the standard deviation for the
				ith $a_{lm}$ is contained in alms(i,5,j)
				(real) and $alms(i,6,j)$ (imaginary).
nlheader		I4B	IN	number of header lines to read from
				the file.
header(LEN=80)	(1:nlheader,	CHR	OUT	the header(s) read from the FITS-
1:next)				file.

## **EXAMPLE:**

call fits2alms ('alms.fits', 65\*66/2, alms, 3, header, 80, 3)

Reads a FITS file with the  $a_{lm}^T$ ,  $a_{lm}^E$  and  $a_{lm}^B$  values read into alms(1:65\*66/2,1:4,1:3). The last index specifies (T,E,B). The second index gives l, m, real( $a_{lm}$ ), imaginary( $a_{lm}$ ) for each of the  $a_{lm}$ . The number 65\*66/2 is the number of  $a_{lm}$  values up to an  $\ell$  value of 64. 80 lines is read from the header in each extension and returned in header(1:80,1:3).

### MODULES & ROUTINES

This section lists the modules and routines used by fits2alms\*.

read\_alms routine called by fits2alms\* for each extension.

fitstools module, containing:

printerror routine for printing FITS error messages.

**cfitsio** library for FITS file handling.

fits2alms\*

# RELATED ROUTINES

This section lists the routines related to fits2alms\*.

alms2fits, dump\_alms routines to store  $a_{lm}$  in a FITS-file

read\_conbintab has the same function as fits2alms\* but with pa-

rameters passed differently.

number\_of\_alms,[getsize\_fits can be used to find out the number of  $a_{lm}$  avail-

able in the file.

# fits2cl\*

### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads a power spectrum from a FITS ASCII or binary table. The routine can read temperature coeffecients  $C_l^T$  or both temperature and polarisation coeffecients  $C_l^T$ ,  $C_l^E$ ,  $C_l^B$ ,  $C_l^{T \times E}$ . If the keyword PDMTYPE is found in the header, fits2cl assumes the table to be in the special format used by Planck and will ignore the first data column.

# FORMAT

call fits2cl\*(filename, clin, lmax, ncl, header, [units])

### ARGUMENTS

name & dimensionality	kind	in/out	description
filename(LEN=filenamelen)	CHR	IN	the FITS file containing the
lmax	I4B	IN	power spectrum.  Maximum $\ell$ value to be read.
ncl	14B I4B	IN	1 for temperature coeffecients
olin (Oulmore 1 mol)	SP/	OUT	only, 4 for polarisation.
clin(0:lmax,1:ncl)	DP	OUT	the power spectrum read from the file.
header(LEN=80) (1:)	CHR	OUT	the header read from the FITS-
units(LEN= $80$ ) (1:)	CHR	OUT	file. the column units read from the FITS-file.

### **EXAMPLE:**

call fits2cl ('cl.fits',cl,64,4,header,units)

Reads a power spectrum from the FITS file 'cl.fits' and stores the result in cl(0:64,1:4) which are the  $C_l$  coeffecients up to l = 64 for  $(T, E, B, T \times E)$ . The FITS header is returned in header, the column units in units.

 $fits2cl^*$ 

# MODULES & ROUTINES

This section lists the modules and routines used by fits2cl\*.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

### RELATED ROUTINES

This section lists the routines related to fits2cl\*.

create\_alm Routine to create  $a_{\ell m}$  values from an input power

spectrum.

write\_asctab Routine to create an ascii FITS file containing a

power spectrum.

# gaussbeam

### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine generates the beam window function in multipole space of a gaussian beam parametrized by its FWHM. The polarization beam is also provided assuming a perfectly co-polarized beam (eg, Challinor et al 2000, astro-ph/0008228)

# **FORMAT**

call gaussbeam(fwhm\_arcmin, lmax, beam)

### ARGUMENTS

name & dimensionality	kind	in/oı	in/outdescription		
fwhm_arcmin	DP	IN	FWHM of the gaussian beam in arcmin-		
lmax	I4B	IN	utes. maximum $\ell$ value of the window function.		
beam(0:lmax,1:p)	DP	OUT			

# **EXAMPLE:**

call gaussbeam(5.0\_dp, 1024, beam)

Generates the window function of a gaussian beam of FWHM = 5 arcmin, for  $\ell \leq 1024$ .

### RELATED ROUTINES

This section lists the routines related to gaussbeam.

generate\_beam

Routine returning a beam window function.

gaussbeam 65

 $pixel\_window$ 

Routine returning a pixel window function.

# $generate\_beam$

### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine generates the beam window function in multipole space. It is either a gaussian parametrized by its FWHM in arcmin in real space, or it is read from an external file.

# FORMAT call generate\_beam(fwhm\_arcmin, lmax, beam [, beam\_file])

### **ARGUMENTS**

name & dimensionality	kind	in/out	description
fwhm_arcmin	DP	IN	fwhm size of the gaussian beam in arcminutes.
lmax	I4B	IN	maximum $\ell$ value of the window function.
beam(0:lmax,1:p)	DP	OUT	beam window function generated. The second index runs form 1:1 for temperature only, and 1:3 for polarisation. In the latter case, 1=T, 2=E, 3=B.
beam_file(LEN=filenamelen) (OPTIONAL)	CHR	IN	name of the file containing the (non necessarily gaussian) window function $B_{\ell}$ of a circular beam. If present, it will override the argument fwhm_arcmin.

### **EXAMPLE:**

call generate\_beam(5.0\_dp, 1024, beam)

Generates the window function of a gaussian beam of FWHM = 5 arcmin, for  $\ell \leq 1024$ .

generate\_beam 67

# MODULES & ROUTINES

This section lists the modules and routines used by **generate\_beam**.

alm\_tools module, containing:

gaussbeam routine to generate a gaussian beam

# RELATED ROUTINES

This section lists the routines related to **generate\_beam**.

create\_alm Routine to create  $a_{\ell m}$  coefficients using gener-

 $ate\_beam.$ 

alter\_alm Routine to alter  $a_{\ell m}$  coefficients using gener-

 $ate\_beam.$ 

pixel\_window Routine returning a pixel window function.

# $get\_card$

### Location in HEALPix directory tree: src/f90/mod/head\_fits.F90

This routine reads a keyword of any kind from a FITS header. It is a wrapper to other routines that read keywords of different kinds.

# **FORMAT**

call get\_card(header, kwd, value, comment)

# **ARGUMENTS**

name & dimensionality	kind	in/out	description
header(LEN=80) DIMENSION(:)	CHR	IN	The header to read the keyword from.
kwd(LEN=8)	CHR	IN	the FITS keyword to read (NOT case sensitive).
value	any	OUT	the value read for the keyword. The type of the fortran variable 'value' (double, real, integer, logical or character) should match the type under which the value is written in the FITS file, except if 'value' is a character string, in which case it can read any keyword value, or if 'value' if real or double, in which case it can read any numerical value
comment(LEN=*)	CHR	OUT	comment read for the keyword.

# **EXAMPLE:**

call get\_card(header,'NsIdE',nside,comment)

if nside is defined as an integer, it will contain on output the value of NSIDE (say 256) found in header

 $get\_card$  69

# **EXAMPLE:**

call get\_card(header, 'ORDERING', ordering, comment)

if ordering is defined as an character string, it will contain on output the value of ORDERING (say 'RING') found in header

# MODULES & ROUTINES

This section lists the modules and routines used by **get\_card**.

**cfitsio** library for FITS file handling.

# RELATED ROUTINES

This section lists the routines related to  $\mathbf{get\_card}$ .

${ m add\_card}$	general purpose routine to write any keywords into a FITS file header
$\operatorname{del\_card}$	routine to discard a keyword from a FITS header
read_par, number_of_alms	routines to read specific keywords from a header in a FITS file.
getsize_fits	function returning the size of the data set in a fits file and reading some other useful FITS keywords
$merge\_headers$	routine to merge two FITS headers

# get\_healpix\_main\_dir, ...

### Location in HEALPix directory tree: src/f90/mod/paramfile\_io.F90

A few functions are available to return the full path to **HEALPix** main directory and its data and test subdirectories. This allow those paths to be controlled by preprocessing macros or environment variables in case of non-standard installation of the **HEALPix** directory structure.

### **FUNCTIONS:**

hmd = get\_healpix\_main\_dir()

returns the full path to the main **HEALPix** directory. It will be determined, in this order, from the value of the preprocessing macros <code>HEALPIX</code> and <code>HEALPIXDIR</code> if they are defined or the environment variable <code>\$HEALPIX</code> otherwise

hdd = get\_healpix\_data\_dir()

returns the full path to **HEALPix** data subdirectory. It will be determined from the preprocessing macro HEALPIXDATA or the environment variable \$HEALPIXDATA. If both fail, it will return the list of directories { . . . /data . /data . . \$HEALPIX \$HEALPIX/data \$HEALPIX/. . . /data \$HEALPIX\data \$ separated by LineFeed.

htd = get\_healpix\_test\_dir()

returns the full path to **HEALPix** test subdirectory. It will be determined, in this order, from the preprocessing macro HEALPIXTEST, the environment variable \$HEALPIXTEST or \$HEALPIX/test.

getArgument 71

# getArgument

Location in HEALPix directory tree: src/f90/mod/extension.F90

This subroutine emulates the C routine getarg, which returns the value of a given command line argument.

FORMAT call getArgument(index, value)

# **ARGUMENTS**

name & dimensionality	kind	in/out	description
index	I4B	IN	index of the command line argument
value	CHR	OUT	(where the first argument has index 1) value of the argument

# RELATED ROUTINES

This section lists the routines related to **getArgument**.

getEnvironment returns value of environment variable

nArguments returns number of command line arguments

# getEnvironment

Location in HEALPix directory tree: src/f90/mod/extension.F90

This subroutine emulates the C routine getenv, which returns the value of an environment variable.

**FORMAT** 

call getEnvironment(name, value)

### ARGUMENTS

name & dimensionality	kind in/out	description
name value	CHR IN CHR OUT	name of the environment variable value of the environment variable

### **EXAMPLE:**

use extension

character(len=128) :: healpixdir

call getEnvironment('HEALPIX', healpixdir)

print\*,healpixdir

Will return the value of the \$HEALPIX system variable (if it is

defined)

### RELATED ROUTINES

This section lists the routines related to **getEnvironment**.

getArgument returns list of command line arguments
nArguments returns number of command line arguments

getdisc\_ring 73

# $\underline{\mathbf{getdisc\_ring}}$

Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

This routine is obsolete, use query\_disc instead

# $getnumext\_fits$

Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine returns the number of extensions present in a given FITS file.

FORMAT var=getnumext\_fits(filename)

#### **ARGUMENTS**

name & dimensionality	kind	in/ou	tdescription
var	I4B	OUT	number of extensions in the FITS file (excluding the primary unit). According to the current format, <b>HEALPix</b> files have at least one
filename(LEN=filenamelen)	CHR	IN	extension. filename of the FITS file.

getnumext\_fits 75

#### **EXAMPLE:**

next = getnumext\_fits('map.fits')

Returns in **next** the number of extensions present in the FITS file 'map.fits'.

#### MODULES & ROUTINES

This section lists the modules and routines used by **getnumext\_fits**.

fitstools module, containing:

printerror routine for printing FITS error messages.

**cfitsio** library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to **getnumext\_fits**.

getsize\_fits routine returning the number of data points in a

FITS file, as well as much more information on

the file.

input\_map routine to read a **HEALPix** FITS file

# ${\bf getsize\_fits}$

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads the number of maps and/or the pixel ordering of a FITS file containing a **HEALPix** map.

#### **FORMAT**

var=getsize\_fits(filename [, nmaps, ordering, obs\_npix, nside, mlpol, type, polarisation, fwhm\_arcmin, beam\_leg, coordsys, polcconv, extno])

#### **ARGUMENTS**

getsize\_fits 77

name & dimensionality	kind	in/ou	itdescription			
var	I8B	OUT	number of pixels or time samples in the chosen extension of the FITS file			
filename(LEN=filenamele)	n)CHR	IN	filename of the FITS-file containing <b>HEALPix</b> map(s).			
nmaps (OPTIONAL)	I4B	OUT	number of maps in the extension.			
ordering (OPTIONAL)	I4B	OUT	pixel ordering, 0=unknown, 1=RING, 2=NESTED			
obs_npix (OPTIONAL)	I4B	OUT	number of non blanck pixels. It is set to -1 if it can not be determined from header information alone			
nside (OPTIONAL)	I4B	OUT	Healpix resolution parameter Nside. Returns a negative value if not found.			
mlpol (OPTIONAL)	I4B	OUT	maximum multipole used to generate the map (for simulated map). Returns a negative value if not found.			
type (OPTIONAL)	I4B	OUT	Healpix/FITS file type <0: file not found, or not valid 0: image only fits file, deprecated Healpix format (var = 12 * nside * nside) 1: ascii table, generally used for C(l) storage 2: binary table: with implicit pixel indexing (full sky) (var = 12 * nside * nside) 3: binary table: with explicit pixel indexing (generally cut sky) (var ≤ 12 * nside * nside) 999: unable to determine the type			
polarisation (OPTIONAL)	I4B	OUT	presence of polarisation data in the file <0: can not find out 0: no polarisation 1: contains polarisation (Q,U or G,C)			
fwhm_arcmin (OP-TIONAL)	DP	OUT	returns the beam FWHM read from FITS header, translated from Deg (hopefully) to arcmin. Returns a negative value if not found.			
$\begin{array}{c} beam\_leg(LEN = \texttt{filenamele}\\ (OPTIONAL) \end{array}$	en¢HR	OUT	filename of beam or filtering window function applied to data (FITS keyword BEAM_LEG). Returns a empty string if not found.			
coordsys(LEN=20) (OP-TIONAL)	CHR	OUT	- • •			
polcconv (OPTIONAL)	I4B	OUT	polarisation coordinate convention (see Healpix primer for details) 0=unknown, 1=COSMO, 2=IAU			
$\underset{\scriptscriptstyle \mathrm{HEALPix}}{\mathrm{extno}} (\underset{\scriptscriptstyle 2.15a}{\mathrm{OPTIONAL}})$	I4B	IN	extension number (0 based) for which information is provided. Default = 0 (first extension).			

#### **EXAMPLE:**

npix= getsize\_fits('map.fits', nmaps=nmaps, ordering=ordering,
obs\_npix=obs\_npix, nside=nside, mlpol=mlpol, type=type,
polarisation=polarisation)

Returns 1 or 3 in nmaps, dependent on wether 'map.fits' contain only temperature or both temperature and polarisation maps. The pixel ordering number is found by reading the keyword ORDERING in the FITS file. If this keyword does not exist, 0 is returned.

#### MODULES & ROUTINES

This section lists the modules and routines used by getsize\_fits.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to **getsize\_fits**.

getnumext\_fits routine returning the number of extension in a

FITS file

input\_map routine to read a **HEALPix** FITS file

# healpix\_modules

Location in HEALPix directory tree: src/f90/mod/healpix\_modules.f90

This module is a meta module containing most of the **HEALPix** modules. It currently includes

- alm\_tools,
- bit\_manipulation,
- coord\_v\_convert,
- extension,
- fitstools,
- head\_fits,
- healpix\_fft,
- healpix\_types,
- misc\_utils,
- num\_rec,
- obsolete,
- paramfile\_io,
- pix\_tools,
- ran\_tools,
- rngmod,
- statistics,
- udgrade\_nr,
- utilities.

Note that mpi\_alm\_tools is not included since it requires the MPI library for compilation.

#### **EXAMPLE:**

```
use healpix_modules
print*,' pi = ',PI
print*,' number of pixels in a Nside=64 map:',nside2npix(64)
```

Invoking healpix\_modules gives access to all **HEALPix** routines and parameters.

# healpix\_types

Location in HEALPix directory tree: src/f90/mod/healpix\_types.F90

This module defines a set of parameters used by most other **HEALPix** modules.

The parameters defined in healpix\_types include

• 'kind' parameters, used when defining the type of a variable,

name	type	$value^a$	definition
I1B	integer	1	number of bytes in the hardware-supported signed inte-
			gers covering the range -99 to 99 with the least margin
I2B	integer	2	same as above for the range -9999 to 9999 (ie, 4 digits)
I4B	integer	4	same as above for 9 digits
I8B	integer	8	same as above for 16 digits <sup><math>b</math></sup>
SP	integer	4	number of bytes in the hardware-supported floating-point
			numbers covering the range $10^{-30}$ to $10^{30}$ with the least
			margin (hereafter single precision)
DP	integer	8	same as above for the range $10^{-200}$ to $10^{200}$ (double pre-
			cision)
SPC	integer	4	number of bytes in real (or imaginary) part of single pre-
			cision complex numbers
DPC	integer	8	same as above for double precision complex numbers
LGT	integer	4	number of bytes in logical variables

 $<sup>^{</sup>a}$ actual value may depend on hardware or compiler

• largest accessible numbers,

name	type or kind	$\mathrm{value}^a$	definition
MAX_I1B	integer	127	largest number accessible to inte-
			gers of kind I1B
$MAX_{12}B$	integer	32767	same as above for I2B integers
MAX_I4B	integer	$2^{31} - 1 \simeq 2.1 \ 10^9$	same as above for I4B integers
MAX_I8B	I8B	$2^{63} - 1 \simeq 9.2 \ 10^{18}$	same as above for I4B integers
$MAX\_SP$	SP	$\simeq 3.40 \ 10^{38}$	same as above for SP floating-point
MAX_DP	DP	$\simeq 1.80 \ 10^{308}$	same as above for DP floating-point

<sup>&</sup>lt;sup>a</sup>actual value may depend on hardware or compiler

 $<sup>^</sup>b$ may not be supported by some hardware or compiler; on those systems, the user should set the preprocessing variable N064BITS to 1 during compilation to demote automatically I8B to I4B

• mathematical definitions,

name	kind	value	definition
QUARTPI	DP	$\pi/4$	
HALFPI	DP	$\pi/2$	
PI	DP	$\pi$	
TWOPI	DP	$2\pi$	
FOURPI	DP	$4\pi$	
SQRT2	DP	$\sqrt{2}$	
EULER	DP	$\gamma \simeq 0.577\dots$	Euler constant
SQ4PI_INV	DP	$1/\sqrt{4\pi}$	
TWOTHIRD	DP	2/3	
DEG2RAD	DP	$\pi/180$	Degrees to Radians conversion factor
RAD2DEG	DP	$180/\pi$	Radians to Degrees conversion factor

ullet and  $egin{aligned} \mathbf{HEALPix} \end{aligned}$  specific definitions,

name	type or kind	value	definition
HPX_SBADVAL	SP	$-1.6375 \ 10^{30}$	default sentinel value given to
			missing pixels in single precision
			data sets
HPX_DBADVAL	DP	$-1.6375 \ 10^{30}$	same as above for double preci-
			sion data sets
FILENAMELEN	integer	1024	default length in character of file
			names.

### **EXAMPLE:**

use healpix\_types
real(kind=DP) :: dx
print\*,' pi = ',PI

The value of PI, as well as all other healpix\_types parameters are made known to the code

## in\_ring

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to find the pixel index of all pixels on a slice of a given ring. The output indices can be either in the RING or NESTED scheme, depending on the nest keyword.

**FORMAT** 

call in\_ring(nside, iz, phi0, dphi, listir, nir, nest)

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
nside	I4B	IN	the $N_{side}$ parameter of the map.
iz	I4B	IN	ring number, counted south-
			wards from the north pole.
phi0	DP	IN	central $\phi$ position in the slice.
dphi	DP	IN	defines the size of the slice. The
			slice has length $2 \times dphi$ along
			the ring with center at $phi0$ .
listir(0:4*nside-1)	I4B	OUT	The pixel indexes in the slice.
nir	I4B	OUT	the number of pixels in the slice.
nest (OPTIONAL)	I4B	IN	The pixel indexes are in the
,			NESTED numbering scheme if
			nest=1, and in RING scheme
			otherwise.

#### **EXAMPLE:**

call in\_ring(256, 10, 0, 0.1, listir, nir, nest=1)

Returns the NESTED pixel index of all pixels within 0.1 radians on each side of  $\phi = 0$  on the 10th ring.

in\_ring 83

#### MODULES & ROUTINES

This section lists the modules and routines used by in\_ring.

ring2nest conversion from RING scheme pixel index to

NESTED scheme pixel index

next\_in\_line\_nest returns NESTED index of pixel lying to the East

of the current pixel and on the same ring

#### RELATED ROUTINES

This section lists the routines related to in\_ring.

pix2ang, ang2pix convert between angle and pixel number.

pix2vec, vec2pix convert between a cartesian vector and pixel num-

ber.

getdisc\_ring find all pixels within a certain radius.

# input\_map\*

Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads a **HEALPix** map from a FITS file. This can deal with full sky as well as cut sky maps

**FORMAT** 

call input\_map\*(filename, map, npixtot, nmaps [, fmissval, header, units, extno])

#### **ARGUMENTS**

name & dimensionality	kind	in/ou	tdescription
	CIID	TNT	
filename(len=filenamelen)	CHR	IN	FITS file to be read from, containing a full sky or cut sky map
map(0:npixtot-1,1:nmaps)	SP/ DP	OUT	full sky map(s) constructed from the data present in the file, missing pixels are filled with fmissval
npixtot	I4B	IN	number of pixels in the full sky map
nmaps	I4B	IN	number of maps in the file
fmissval (OPTIONAL) header(LEN=80)(1:) (OPTIONAL)	SP/ DP CHR	IN OUT	value to be given to missing pixels, its default value is $0$ FITS extension header
units(LEN=20)(1:nmaps) (OPTIONAL)	CHR	OUT	maps units
extno (OPTIONAL)	I4B	IN	extension number to read the data from (0 based).( <b>default:</b> 0) (the first extension is read)

#### **EXAMPLE:**

use pix\_tools, only: nside2npix

use fitstools, only: getsize\_fits, input\_map

. . .

input\_map\* 85

```
npixtot = getsize_fits('map.fits',nmaps=nmaps, nside=nside)
npix = nside2npix(nside)
allocate(map(0:npix-1,1:nmaps))
call input_map('map.fits', map, npix, nmaps)
```

Reads into map the content of the FITS file 'map.fits'

#### MODULES & ROUTINES

This section lists the modules and routines used by **input\_map\***.

${ m fitstools}$	module, containing:
printerror	routine for printing FITS error messages.
$read\_bintab$	routine to read a binary table from a FITS file
$read\_fits\_cut4$	routine to read cut sky map from a FITS file
$\operatorname{cfitsio}$	library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to **input\_map\***.

anafast	executable that reads a <b>HEALPix</b> map and anal-
	yses it.
synfast	executable that generate full sky $\mathbf{HEALPix}$ maps
$getsize\_fits$	subroutine to know the size of a FITS file.
$output\_map$	subroutine to write a FITS file from a $\mathbf{HEALPix}$
	map
$write\_bintabh$	subroutine to write a large array into a FITS file piece by piece
$\mathrm{input\_tod}*$	subroutine to read an arbitrary subsection of a large binary table

# $input\_tod*$

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads a large binary table (for instance a Time Ordered Data set) from a FITS file. The user can choose to read only a section of the table, starting from an arbitrary position. The data can be read into a single or double precision array.

# FORMAT call input\_tod\*(filename, tod, npix, ntods [, header, firstpix, fmissval])

#### **ARGUMENTS**

name & dimensionality	kind	in/outdescription		
filename (LEN = filenamelen)	CHR	IN	FITS file to be read from	
tod(0:npix-1,1:ntods)	SP/ DP	OUT	array constructed from the data present in the file (from the sample firstpix to firstpix + npix - 1. Missing pixels or time samples are filled with fmissval.	
npix	I8B	IN	number of pixels or samples to be read. See Note below.	
ntods	I4B	IN	number of columns to read	
header(LEN=80)(1:) (OPTIONAL)	CHR	OUT	FITS extension header	
firstpix (OPTIONAL)	I8B	IN	first pixel (or time sample) to read from (0 based). ( <b>default:</b> 0). See Note below.	
fmissval (OPTIONAL)	SP/ DP	IN	value to be given to missing pixels, its default value is 0. Should be of the same type as tod.	

**Note:** Indices and number of data elements larger than  $2^{31}$  are only accessible in FITS files on computers with 64 bit enabled compilers and with some specific compilation options of cfitsio (see cfitsio documentation).

#### MODULES & ROUTINES

input\_tod\*

This section lists the modules and routines used by **input\_tod\***.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to **input\_tod\***.

anafast executable that reads a **HEALPix** map and anal-

yses it.

synfast executable that generate full sky **HEALPix** maps

getsize\_fits subroutine to know the size of a FITS file.

write\_bintabh subroutine to write large arrays into FITS files output\_map subroutine to write a FITS file from a **HEALPix** 

map

input\_map subroutine to read a **HEALPix** map (either full

sky of cut sky) from a FITS file

# map2alm\*

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine is a wrapper to 5 internal routines:map2alm\_sc, map2alm\_sc\_pre, map2alm\_pol, map2alm\_pol\_pre1, map2alm\_pol\_pre2. These routines analyse a **HEALPix** RING ordered map and return  $a_{lm}^T$  (and if specified  $a_{lm}^E$  and  $a_{lm}^B$ ) values up to the desired order in  $\ell$  (maximum  $3*N_{side}$ ). The different routines are called depending on what parameters are passed. Some routines analyse with or without precomputed harmonics and some with or without polarisation.

### $\mathbf{FORMAT}$

call map2alm\*(nsmax, nlmax, nmmax, map\_TQU, alm\_TGC, zbounds, w8ring\_TQU [, plm])

#### ARGUMENTS

name & dimensionality	kind	in/outde	escription
nsmax	I4B	IN th	ne $N_{side}$ value of the map to anal-
nlmax	I4B	v	ne maximum $\ell$ value for the analy-
nmmax	I4B		ne maximum $m$ value for the analsis.
map_TQU(0:12*nsmax**2-1)	SP/ DP	be	only the temperature map is to e analyse, the map-array should be assed with this rank.
map_TQU(0:12*nsmax**2-1, 1:3)	SP/ DP	m ra se	both temperature an polarisation aps are to be analysed, the map arely should have this rank, where the econd index is $(1,2,3)$ corresponding to $(T,Q,U)$ .

map2alm\*

alm_TGC(1:p, 0:nlmax, 0:nmmax)	SPC/ DPC	OUT	The $a_{lm}$ values output from the analysis. p is 1 or 3 dependent on wether polarisation is included or not. In the former case, the first index is $(1,2,3)$ corresponding to $(T,E,B)$ .
zbounds(1:2)	DP	IN	section of the map on which to perform the $a_{lm}$ analysis, expressed in terms of $z = \sin(\text{latitude}) = \cos(\theta)$ . If zbounds(1) <zbounds(2), analysis="" is="" on="" performed="" strip="" the="" zbounds(1)<<math="">z<zbounds(2); if="" is="" it="" not,="" of="" outside="" performed="" td="" the<=""></zbounds(2);></zbounds(2),>
w8ring_TQU(1:2*nsmax, 1:p)	DP	IN	strip zbounds(2) $< z <$ zbounds(1). ring weights for quadrature corrections. If ring weights are not used, this array should be 1 everywhere. p is 1 for a temperature analysis and 3 for $(T,Q,U)$ .
plm(0:(nlmax+1)(nlmax+2)nsmax-1), OPTIONAL	DP	IN	If this optional matrix is passed with this rank, precomputed $P_{lm}(\theta)$ are used instead of recursion.
plm(0:(nlmax+1)(nlmax+2)nsmax-1,1:3), TIONAL	DP	IN	If this optional matrix is passed with $\Omega$ Ris rank, precomputed $P_{lm}(\theta)$ AND precomputed tensor harmonics are used instead of recursion.

#### **EXAMPLE:**

```
use healpix_types
use alm_tools
use pix_tools
integer(i4b) :: nside, lmax
real(dp), allocatable, dimension(:,:) :: dw8
real(dp), dimension(2) :: z
real(sp), allocatable, dimension(:,:) :: map
complex(spc), allocatable, dimension(:,:,:) :: alm

nside = 256
lmax = 512
allocate(dw8(1:2*nside, 1:3))
allocate(map(0:nside2npix(nside)-1,1:3))
allocate(alm(1:3, 0:lmax, 0:lmax))
```

Analyses temperature and polarisation maps passed in map. The map has an  $N_{side}$  of 256, and the analysis is performed up to 512 in  $\ell$  and m. The resulting  $a_{lm}$  coefficients for temperature and polarisation are returned in alm. A 10° cut on each side of the equator is applied. Uniform weights are used. Since the optional plm array is provided with rank one, precomputed scalar  $P_{lm}(\theta)$  are used while tensor harmonics are computed with a recursion.

#### MODULES & ROUTINES

This section lists the modules and routines used by **map2alm\***.

ring\_analysis Performs FFT for the ring analysis.

misc\_util module, containing:

assert\_alloc routine to print error message when an array is

not properly allocated

#### RELATED ROUTINES

This section lists the routines related to map2alm\*.

anafast executable using map2alm\*to analyse maps.

alm2map routine performing the inverse transform of

map2alm\*.

map2alm\_iterative similar to map2alm\* with iterative scheme.

# map2alm\_iterative\*

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine covers and extends the functionalities of map2alm: it analyzes a (polarised) **HEALPix** RING ordered map and returns its  $a_{lm}$  coefficients for temperature (and polarisation) up to a specified multipole, and use precomputed harmonics if those are provided, but it also can also perform an iterative (Jacobi) determination of the  $a_{lm}$ , and apply a pixel mask if one is provided.

#### **FORMAT**

call map2alm\_iterative\*(nsmax, nlmax, nm-max, iter\_order, map\_TQU, alm\_TGC [, zbounds, w8ring\_TQU , plm, mask])

#### **ARGUMENTS**

name & dimensionality	kind	in/outdescription
nsmax	I4B	IN the $N_{side}$ value of the map to anal-
		yse.
nlmax	I4B	IN the maximum $\ell$ value for the analy-
		sis.
nmmax	I4B	IN the maximum $m$ value for the anal-
		ysis.
iter_order	I4B	IN the order of Jacobi iteration. In-
		creasing that order improves the ac-
		curacy of the final $a_{lm}$ but increases
		the computation time $T_{\rm CPU} \propto 1 +$
		$2 \times \text{iter\_order}$ iter\_order = 0 is a
		straight analysis, while iter_order =
TIOII (0.10\)	CD /	3 is usually a good compromise.
$map_TQU(0:12*nsmax**2-1, 1:p)$	SP/	INOUTinput map. $p$ is 1 or 3 depending
	DP	if temperature (T) only or tempera-
		ture and polarisation (T, Q, U) are
		to be analysed. It will be altered on
		output if a mask is provided.

alm_TGC(1:p, 0:nlmax, 0:nmmax)	SPC/ DPC	OUT	The $a_{lm}$ values output from the analysis. $p$ is 1 or 3 depending on whether polarisation is included or not. In the former case, the first index is $(1,2,3)$ corresponding to $(T,E,B)$ .
zbounds(1:2), OPTIONAL	DP	IN	section of the map on which to perform the $a_{lm}$ analysis, expressed in terms of $z = \sin(\text{latitude}) = \cos(\theta)$ . If zbounds(1) <zbounds(2), <math="" analysis="" is="" on="" performed="" strip="" the="" zbounds(1)<="">z <zbounds(2); <math="" if="" is="" it="" not,="" of="" outside="" performed="" strip="" the="" zbounds(2)<="">z <zbounds(1). absent,="" analyzed<="" if="" is="" map="" td="" the="" whole=""></zbounds(1).></zbounds(2);></zbounds(2),>
w8ring_TQU(1:2*nsmax,1:p), OPTIONAL	DP	IN	ring weights for quadrature corrections. p is 1 for a temperature analysis and 3 for (T,Q,U). If absent, the ring weights are all set to 1.
plm(0:,1:p), OPTIONAL	DP	IN	If this optional matrix is passed, precomputed scalar (and tensor) $P_{lm}(\theta)$ are used instead of recursion.
mask(0:12*nsmax**2-1,1:q), OPTIONAL	SP/ DP	IN	pixel mask, assumed to have the same resolution (and RING ordering) as the map. The map map_TQU is multiplied by that mask before being analyzed, and will therefore be altered on output. $q$ should be in $\{1,2,3\}$ . If $p=q=3$ , then each of the 3 masks is applied to the respective map. If $p=3$ and $q=2$ , the first mask is applied to the first map, and the second mask to the second (Q) and third (U) map. If $p=3$ and $q=1$ , the same mask is applied to the 3 maps. Note: the output $a_{lm}$ are computed directly on the masked map, and are not corrected for the loss of power, correlation or leakage created by the mask.

### EXAMPLE:

```
use healpix_types
use alm_tools
use pix_tools
integer(i4b) :: nside, lmax, npix, iter
real(sp), allocatable, dimension(:,:) ::
real(sp), allocatable, dimension(:) :: mask
complex(spc), allocatable, dimension(:,:,:)
                                                 alm
nside = 256
lmax = 512
iter = 2
npix = nside2npix(nside)
allocate(map(0:npix-1,1:3))
allocate(mask(0:npix-1))
mask(0:) = 0.! set unvalid pixels to 0
mask(0:10000-1) = 1. ! valid pixels
allocate(alm(1:3, 0:lmax, 0:lmax)
call map2alm_iterative(nside, lmax, lmax, iter, map, alm, mask=mask)
```

Analyses temperature and polarisation signals in the first 10000 pixels of map (as determined by mask). The map has an  $N_{side}$  of 256, and the analysis is supposed to be performed up to 512 in  $\ell$  and m. The resulting  $a_{lm}$  coefficients for temperature and polarisation are returned in alm. Uniform weights are assumed. In order to improve the allm accuracy, 2 Jacobi iterations are performed.

#### MODULES & ROUTINES

This section lists the modules and routines used by map2alm\_iterative\*.

ring\_analysis Performs FFT for the ring analysis.

map2alm Perform the alm analysis

misc\_util module, containing:

assert\_alloc routine to print error message when an array is

not properly allocated

#### RELATED ROUTINES

This section lists the routines related to map2alm\_iterative\*.

anafast executable using map2alm\_iterative\* to analyse

maps.

alm2map routine performing the inverse transform of

map2alm\_iterative\*.

 $alm 2 map\_spin \hspace{1cm} synthesize \hspace{0.1cm} spin \hspace{0.1cm} weighted \hspace{0.1cm} maps.$ 

map2alm\_spin analyze spin weighted maps.

map2alm\_spin\*

# map2alm\_spin\*

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine extracts the alm coefficients out of maps of spin s and -s. A (complex) map S of spin s is a linear combination of the spin weighted harmonics  ${}_sY_{lm}$ 

$${}_{s}S(p) = \sum_{lm} {}_{s}a_{lm} \quad {}_{s}Y_{lm}(p) \tag{8}$$

for  $l \ge |m|, l \ge |s|$ , and is such that  ${}_sS^* = {}_{-s}S$ .

The two (real) input maps for map2alm\_spin\* are defined respectively as

$$|s|S^{+} = (|s|S + -|s|S)/2$$
 (9)

$$|s|S^{-} = (|s|S - -|s|S)/(2i).$$
 (10)

map2alm\_spin\* outputs the alm coefficients defined as

$$_{|s|}a_{lm}^{+} = -(_{|s|}a_{lm} + (-1)^{s}_{-|s|}a_{lm})/2$$
 (11)

$$a_{ls}^{-} = -({}_{|s|}a_{lm} - (-1)^{s}{}_{-|s|}a_{lm})/(2i)$$
 (12)

for  $m \ge 0$ , knowing that, just as for spin 0 maps, the coefficients for m < 0 are given by

$$_{|s|}a_{l-m}^{+} = (-1)^{m}{}_{|s|}a_{lm}^{+*},$$
 (13)

$$a_{l-m}^- = (-1)^m{}_{|s|}a_{lm}^{-*}.$$
 (14)

With these definitions,  ${}_2a^+, {}_2a^-, {}_2S^+$  and  ${}_2S^-$  match **HEALPix** polarization  $a^E, a^B, Q$  and U respectively. However, for  $s=0, {}_0a^+_{lm}=-a^T_{lm}, {}_0a^-_{lm}=0, {}_0S^+=T, {}_0S^-=0.$ 

**FORMAT** 

call map2alm\_spin\*(nsmax, nlmax, nmmax, spin, map, alm [, zbounds, w8ring\_TQU])

#### ARGUMENTS

name & dimensionality	kind	in/oı	utdescription
nsmax	I4B	IN	the $N_{side}$ value of the map to analyse.
nlmax	I4B	IN	the maximum $\ell$ value for the analysis.
nmmax	I4B	IN	the maximum $m$ value for the analysis.
spin	I4B	IN	the spin $s$ of the maps to be analysed (only its absolute value is relevant).
map(0:12*nsmax**2-1, 1:2)	SP/ DP	IN	$ s S^+$ and $ s S^-$ input maps
alm(1:2, 0:nlmax, 0:nmmax)	SPC/ DPC	OUT	The $_{ s }a_{lm}^+$ and $_{ s }a_{lm}^-$ output values.
zbounds(1:2), OPTIONAL	DP	IN	section of the map on which to perform the $a_{lm}$ analysis, expressed in terms of $z = \sin(\text{latitude}) = \cos(\theta)$ . If zbounds(1) <zbounds(2), analysis="" is="" on="" performed="" strip="" the="" zbounds(1)<<math="">z<zbounds(2); if="" is="" it="" not,="" of="" outside="" performed="" strip="" the="" zbounds(2)<<math="">z<zbounds(1).< td=""></zbounds(1).<></zbounds(2);></zbounds(2),>
w8ring(1:2*nsmax,1:2), OPTIONAL	DP	IN	ring weights for quadrature corrections. If ring weights are not used, this array should be 1 everywhere.

#### **EXAMPLE:**

```
use healpix_types
use alm_tools
use pix_tools
integer(i4b) :: nside, lmax, spin
real(sp), allocatable, dimension(:,:) :: map
complex(spc), allocatable, dimension(:,:,:) :: alm

nside = 256
lmax = 512
spin = 5
allocate(map(0:nside2npix(nside)-1,1:2))
allocate(alm(1:2, 0:lmax, 0:lmax)
...
call map2alm_spin(nside, lmax, lmax, spin, map, alm)
```

map2alm\_spin\*

Analyses spin 5 and -5 maps. The maps have an  $N_{side}$  of 256, and the analysis is performed up to 512 in  $\ell$  and m. The resulting  $a_{lm}$  coefficients for are returned in alm.

#### MODULES & ROUTINES

This section lists the modules and routines used by map2alm\_spin\*.

ring\_analysis Performs FFT for the ring analysis.

compute\_lam\_mm, get\_pixel\_layout,

gen\_lamfac\_der, gen\_mfac,

gen\_recfac, init\_rescale, l\_min\_ylm Ancillary routines used for  ${}_sY_{\ell m}$  recursion

misc\_util module, containing:

assert\_alloc routine to print error message when an array is

not properly allocated

#### RELATED ROUTINES

This section lists the routines related to map2alm\_spin\*.

alm2map\_spin routine performing the inverse transform of

map2alm\_spin\*.

map2alm routine analyzing temperature and polarization

maps

# medfiltmap\*

 $Location \ in \ HEALPix \ directory \ tree: \ src/f90/mod/pix\_tools.f90$ 

This routine performs the median filtering of a **HEALPix** full sky map for a given neighborhood radius

FORMAT call medfiltmap\*(in\_map, radius, med\_map [, nest, fmissval, fill\_holes])

#### **ARGUMENTS**

name &	dimensionality	kind	in/ou	utdescription
$in_map(0)$	:npix-1)	SP/	IN	Full sky <b>HEALPix</b> map to filter. npix
		DP		should be valid <b>HEALPix</b> pixel number.
radius		DP	IN	Radius in RADIANS of the disk on which the
				median is computed.
med_map	0 = 0 = 0	SP/	OUT	Median filtered map: each pixel is the median
		$\overline{\mathrm{DP}}$		of the input map valid neighboring pixels con-
				tained within a distance radius
nest	OPTIONAL	I4B	IN	set to 1 if the map ordering is NESTED, set
				to 0 if it is RING.
fmissval	OPTIONAL	SP/	IN	sentinel value given to missing or non-
		$\overline{\mathrm{DP}}$		valid pixels. Default: HPX_SBADVAL or
				${\tt HPX\_DBADVAL} = -1.6375 \ 10^{30}$
fill_holes	OPTIONAL	LGT	IN	if set to .true. will replace non-valid pixels
				by median of neighbors; if set to .false. will
				leave non-valid pixels unchanged. Default:
				.false.

#### **EXAMPLE:**

```
use healpix_types
use pix_tools
...
call medfiltmap(map, 0.5*DEG2RAD, med)
```

medfiltmap\*

Output in  $\mathtt{med}$  the median filter of  $\mathtt{map},$  using a filter radius of  $0.5~\mathrm{Deg}$ 

#### MODULES & ROUTINES

This section lists the modules and routines used by **medfiltmap\***.

statistics module, containing:

median routine to compute the median of a data set

pix\_tools module, containing:

pix2vec\_ring, pix2vec\_nest routines to find the location of a pixel on the sky

query\_disc routine to find pixels lying within a radius of a

given point

# median\*

Location in HEALPix directory tree: src/f90/mod/statistics.f90

This function computes the median of a data set

FORMAT var=median\*(data [, badval, even])

#### **ARGUMENTS**

name & dimensionality	kind	in/oı	ıtdescription
var	SP/ DP	OUT	median of the data set, defined as the middle number (or the average of the 2 middle num- bers) once the valid data points are sorted in monotonous order
data(:)	SP/ DP	IN	data set
badval (OPTIONAL)	SP/ DP	IN	sentinel value given to bad data points. Data points with this value will be ignored during calculation of the median. If not set, all points will be considered. <b>Do not set to 0!</b> .
even (OPTIONAL)	LGT	IN	if set to .true. and the number of valid data points is even, will output the average of the 2 middle points (which doubles the calculation time). If the number of points is odd, the single middle point is output and this keyword is ignored.

#### **EXAMPLE:**

```
use statistics, only: median
...
med = median(map, even=.true.)
```

Outputs in med the median of map

median\*

#### MODULES & ROUTINES

This section lists the modules and routines used by **median\***.

m\_indmed module of the Orderpack 2.0 package, writ-

ten by: Michel Olagnon, http://www.fortran-

2000.com/rank/

indmed routine to output rank of median

#### RELATED ROUTINES

This section lists the routines related to **median\***.

compute\_statistics routine min, max, absolute deviation, and first

four order moments of a data set

# merge\_headers

Location in HEALPix directory tree: src/f90/mod/head\_fits.F90 This routine merges two FITS headers.

**FORMAT** 

call merge\_headers(header1, header2)

#### **ARGUMENTS**

name&dimensionality	kind in/out	$\operatorname{description}$
header1(LEN=80) DIMENSION(:) header2(LEN=80) DIMENSION(:)	CHR IN CHR INOUT	First header. Second header. On output, will contain the concatenation of (in that order) header2 and header1. If header2 is too short to allow the merging the output will be truncated

#### **EXAMPLE:**

call merge\_headers(header1, header2)

On output header2 will contain the original header2, followed by the content of header1

#### MODULES & ROUTINES

This section lists the modules and routines used by merge\_headers.

$\mathrm{write\_hl}$	more general routine for adding a keyword to a
	header.
cfitsio	library for FITS file handling.

merge\_headers 103

#### RELATED ROUTINES

This section lists the routines related to merge\_headers.

$\operatorname{add\_card}$	general purpose routine to write any keywords
	into a FITS file header
$\operatorname{get\_card}$	general purpose routine to read any keywords from a header in a FITS file.
$\operatorname{del}$ _card	routine to discard a keyword from a FITS header
$read_par, number_of_alms$	routines to read specific keywords from a header

in a FITS file.
getsize\_fits function returning the size of the data set in a fits

file and reading some other useful FITS keywords

# mpi\_alm\_tools\*

#### Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This module implements MPI parallelization of the alm2map and map2alm routines. It is not compiled by default during installation, but rather intended for users who need massive parallelization in their own programming. Typical applications are Monte Carlo simulations and Markov chain type analyses.

The routines can be called in two modes, either simple or advanced. The former mimics the interface of the standard routines, but with an additional MPI handle as a first argument, and is intended for applications which requires only one or a few transforms. The latter interface provides both more flexibility (in particular the option of pre-computation of the Legendre polynomials) and a simpler interface when multiple transforms are required. This interface is particularly well suited for Monte Carlo simulations and Markov chain type analyses.

#### **EXAMPLE:**

- Simple one-line interfaces:
  - mpi\_map2alm\_simple
  - mpi\_alm2map\_simple
- Three-step advanced interfaces:
  - 1. Initialization:
     mpi\_initialize\_alm\_tools
  - 2. Execution of spherical harmonics transforms
    - mpi\_map2alm (root processor)
    - mpi\_alm2map (root processor)
    - mpi\_map2alm\_slave (slave processor)
    - mpi\_alm2map\_slave (slave processor)
  - 3. Finalizing:

mpi\_cleanup\_alm\_tools

mpi\_alm\_tools\*

# mpi\_alm2map\*

#### Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This subroutine implements MPI parallelization of the serial alm2map routine. It supports both temperature and polarization inputs in both single and double precision. It must only be run by the root node of the MPI communicator.

### FORMAT call mpi\_alm2map\*(alms, map)

#### ARGUMENTS

name & dimensionality	kind	in/outdescription
alms(1:nmaps,0:lmax,0:nmax)	SPC or DPC	IN Input alms. If nmaps=1, only temperature information is included; if nmaps=3, polarization information is included
map(0:npix,1:nmaps)	SP or DP	OUT Output map. nmaps must match that of the input alms array.

#### **EXAMPLE:**

mpi\_alm2map\*

This example 1) initializes the mpi\_alm\_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel alm2map operation, and 3) frees the previously allocated memory.

#### MODULES & ROUTINES

This section lists the modules and routines used by mpi\_alm2map\*.

alm\_tools module

#### RELATED ROUTINES

This section lists the routines related to mpi\_alm2map\*.

$mpi\_cleanup\_alm\_tools$	Frees memory that is allocated by the current routine.
$mpi\_initialize\_alm\_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
$mpi\_alm2map\_slave$	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
${ m mpi\_map2alm}$	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi\_map2alm\_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
$mpi\_alm2map\_simple$	One-line interface to the parallel inverse spherical harmonics transform
mpi_map2alm_simple	One-line interface to the parallel spherical harmonics transform

# mpi\_alm2map\_simple\*

#### Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This subroutine provides a simplified (one-line) interface to the MPI version of alm2map. It supports both temperature and polarization inputs in both single and double precision. It must only be run by all nodes in the MPI communicator.

#### **FORMAT**

call mpi\_alm2map\_simple\*(comm, alms, map)

#### ARGUMENTS

name & dimensionality	kind	in/oı	ntdescription
$\begin{array}{l} comm \\ alms(1:nmaps,0:lmax,0:nmax) \end{array}$	I4B SPC or	IN IN	MPI communicator. Input alms. If nmaps=1, only temperature information is included; if
map(0:npix,1:nmaps)	DPC SP or DP	OUT	nmaps=3, polarization information is included Output map. nmaps must match that of the input alms array.

#### **EXAMPLE:**

call mpi\_alm2map\_simple(comm, map, alms)

This example executes a parallel map2alm operation through the one-line interface. Although all processors must supply allocated arrays to the routine, only the root processor's information will be used as input, and only the root processor's alms will be complete after execution.

#### MODULES & ROUTINES

This section lists the modules and routines used by mpi\_alm2map\_simple\*.

alm\_tools module

# RELATED ROUTINES

This section lists the routines related to mpi\_alm2map\_simple\*.

$mpi\_cleanup\_alm\_tools$	Frees memory that is allocated by the current routine.
$mpi\_initialize\_alm\_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
mpi_alm2map	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
$mpi\_alm2map\_slave$	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
$\rm mpi\_map2alm$	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi\_map2alm\_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
$mpi\_map2alm\_simple$	One-line interface to the parallel spherical harmonics transform

# mpi\_alm2map\_slave

#### Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This subroutine complements the master routine mpi\_alm2map, and should be run by all slaves in the current MPI communicator. It is run without arguments, but after an appropriate call to initialize\_mpi\_alm\_tools.

## **FORMAT**

call mpi\_alm2map\_slave()

#### ARGUMENTS

None.

#### **EXAMPLE:**

This example 1) initializes the mpi\_alm\_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel alm2map operation, and 3) frees the previously allocated memory.

#### MODULES & ROUTINES

This section lists the modules and routines used by mpi\_alm2map\_slave.

alm\_tools module

# RELATED ROUTINES

This section lists the routines related to  ${\bf mpi\_alm2map\_slave}.$ 

$mpi\_cleanup\_alm\_tools$	Frees memory that is allocated by the current rou-
	tine.
$mpi\_initialize\_alm\_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
${ m mpi\_alm2map}$	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
$mpi\_map2alm$	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi\_map2alm\_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
$mpi\_alm2map\_simple$	One-line interface to the parallel inverse spherical harmonics transform
$mpi\_map2alm\_simple$	One-line interface to the parallel spherical harmonics transform

# $\underline{mpi\_cleanup\_alm\_tools}$

#### Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This subroutine deallocates any private arrays previously allocated in the mpi\_alm\_tools module. It should be run (without arguments) by all processors in the current communicator after the last call to any of the working routines.

## **FORMAT**

call mpi\_cleanup\_alm\_tools()

#### **ARGUMENTS**

None.

#### **EXAMPLE:**

This example 1) initializes the mpi\_alm\_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel map2alm operation, and 3) frees the previously allocated memory.

#### RELATED ROUTINES

This section lists the routines related to mpi\_cleanup\_alm\_tools.

$mpi\_initialize\_alm\_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
$\mathrm{mpi\_alm2map}$	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
$mpi\_alm2map\_slave$	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
$mpi\_map2alm$	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi\_map2alm\_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
$mpi\_alm2map\_simple$	One-line interface to the parallel inverse spherical harmonics transform
$mpi\_map2alm\_simple$	One-line interface to the parallel spherical harmonics transform

# mpi\_initialize\_alm\_tools

#### Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This subroutine initializes the mpi\_alm\_tools module, and must be run prior to any of the advanced interface working routines by all processors in the MPI communicator. The root processor must supply all arguments, while it is optional for the slaves. However, the information is disregarded if they do.

A major advantage of MPI parallelization is large quantities of memory, allowing for pre-computation of the Legendre polynomials even with high  $N_{\rm side}$  and  $\ell_{\rm max}$ , since each processor only needs a fraction  $(1/N_{\rm procs})$  of the complete table. This feature is controlled by the "precompute\_plms" parameter. In general, the CPU time can be expected to decrease by roughly 50% using pre-computed Legendre polynomials for temperature calculations, and by about 30% for polarization calculations.

# **FORMAT**

call mpi\_initialize\_alm\_tools(comm, [nsmax], [nlmax], [nmmax], [zbounds], [polarization], [precompute\_plms], [w8ring])

#### ARGUMENTS

name & dimensionality	kind	in/o	utdescription
COMMO	I4B	IN	MPI communicator.
comm			1.11 1 001111101110000011
nsmax	I4B	IN	the $N_{side}$ value of the HEALPix map. (OPTIONAL)
nlmax	I4B	IN	the maximum $\ell$ value used for the $a_{lm}$ . (OPTIONAL)
nmmax	I4B	IN	the maximum $m$ value used for the $a_{lm}$ . (OPTIONAL)

zbounds $(1:2)$	DP	IN	section of the map on which to
			perform the $a_{lm}$ analysis, expressed
			in terms of $z = \sin(\text{latitude}) =$
			$\cos(\theta)$ . If zbounds(1) <zbounds(2),< td=""></zbounds(2),<>
			the analysis is performed $on$ the
			strip zbounds(1) $< z <$ zbounds(2);
			if not, it is performed <i>outside</i> of the
			strip zbounds(2) $< z >$ zbounds(1).
			(OPTIONAL)
polarization	LGT	IN	if polarization is required, this
			should be set to true, else it should
			be set to false. (OPTIONAL)
$precompute\_plms$	I4B	IN	$0 = \text{do not pre-compute any } P_{\ell m}$ 's;
			$1 = \text{pre-compute } P_{\ell m}^{\text{T}}; 2 = \text{pre-}$
			compute $P_{\ell m}^{\mathrm{T}}$ and $P_{\ell m}^{\mathrm{P}}$ . (OP-
			TIONAL)
w8ring_TQU(1:2*nsmax, 1:p)	DP	IN	ring weights for quadrature correc-
			tions. If ring weights are not used,
			this array should be 1 everywhere. p
			is 1 for a temperature analysis and
			3 for (T,Q,U). (OPTIONAL)
			· · · · · · · · · · · · · · · · · · ·

## **EXAMPLE:**

This example 1) initializes the mpi\_alm\_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel map2alm operation, and 3) frees the previously allocated memory.

# RELATED ROUTINES

This section lists the routines related to  ${\bf mpi\_initialize\_alm\_tools}.$ 

mpi_cleanup_alm_tools	Frees memory that is allocated by the current routine.
$mpi\_alm2map$	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
mpi_alm2map_slave	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
${ m mpi\_map2alm}$	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi\_map2alm\_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
$mpi\_alm2map\_simple$	One-line interface to the parallel inverse spherical harmonics transform
$mpi\_map2alm\_simple$	One-line interface to the parallel spherical harmonics transform

mpi\_map2alm\*

# mpi\_map2alm\*

#### Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This subroutine implements MPI parallelization of the serial map2alm routine. It supports both temperature and polarization inputs in both single and double precision. It must only be run by the root node of the MPI communicator.

# FORMAT call mpi\_map2alm\*(map, alms)

#### **ARGUMENTS**

name & dimensionality	kind	in/outdescription	in/ou
map(0:npix,1:nmaps)	SP or DP	IN map to analyse. If nmaps=1, only temperature information is included; if nmaps=3, polarization in-	IN
alms(1:nmaps,0:lmax,0:nmax)	SPC	formation is included  OUT output alms. nmaps must equal that	OUT
amis(1.imaps,0.imax,0.imax)	or DPC	of the input map	001

## **EXAMPLE:**

This example 1) initializes the mpi\_alm\_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel map2alm operation, and 3) frees the previously allocated memory.

#### MODULES & ROUTINES

This section lists the modules and routines used by mpi\_map2alm\*.

alm\_tools module

#### RELATED ROUTINES

This section lists the routines related to mpi\_map2alm\*.

$mpi\_cleanup\_alm\_tools$	Frees memory that is allocated by the current routine.
$mpi\_initialize\_alm\_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
$mpi\_alm2map$	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
$mpi\_alm2map\_slave$	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
$mpi\_map2alm\_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
$mpi\_alm2map\_simple$	One-line interface to the parallel inverse spherical harmonics transform
$mpi\_map2alm\_simple$	One-line interface to the parallel spherical harmonics transform

# mpi\_map2alm\_simple\*

## Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This subroutine provides a simplified (one-line) interface to the MPI version of map2alm. It supports both temperature and polarization inputs in both single and double precision. It must only be run by all processors in the MPI communicator.

# **FORMAT**

call mpi\_map2alm\_simple\*(comm, map, alms, [zbounds], [w8ring])

# **ARGUMENTS**

name & dimensionality	kind	in/outdescription
comm map(0:npix-1,1:nmaps)	I4B SP or DP	IN MPI communicator. IN input map. If nmaps=1, only temperature information is included; if nmaps=3, polarization information is included
alms(1:nmaps,0:lmax,0:nmax)	SPC or DPC	IN output alms. nmaps must equal that of the input map
zbounds(1:2)	DP	IN section of the map on which to perform the $a_{lm}$ analysis, expressed in terms of $z = \sin(\text{latitude}) = \cos(\theta)$ . If zbounds(1) <zbounds(2), analysis="" is="" on="" performed="" strip="" the="" zbounds(1)<<math="">z<zbounds(2); if="" is="" it="" not,="" of="" outside="" performed="" strip="" the="" zbounds(2)<<math="">z<zbounds(1). (optional)<="" td=""></zbounds(1).></zbounds(2);></zbounds(2),>
w8ring_TQU(1:2*nsmax, 1:p)	DP	IN ring weights for quadrature corrections. If ring weights are not used, this array should be 1 everywhere. p is 1 for a temperature analysis and 3 for (T,Q,U). (OPTIONAL)

## **EXAMPLE:**

call mpi\_map2alm\_simple(comm, map, alms)

This example executes a parallel map2alm operation through the one-line interface. Although all processors must supply allocated arrays to the routine, only the root processor's information will be used as input, and only the root processor's alms will be complete after execution.

### MODULES & ROUTINES

This section lists the modules and routines used by mpi\_map2alm\_simple\*.

alm\_tools module

## RELATED ROUTINES

This section lists the routines related to mpi\_map2alm\_simple\*.

mpi_cleanup_alm_tools	Frees memory that is allocated by the current routine.
$mpi\_initialize\_alm\_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
${ m mpi\_alm2map}$	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
mpi_alm2map_slave	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
mpi_map2alm	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi\_map2alm\_slave$	Routine for executing a parallel spherical harmonics transform (slave processor interface)
$mpi\_alm2map\_simple$	One-line interface to the parallel inverse spherical harmonics transform

# mpi\_map2alm\_slave

#### Location in HEALPix directory tree: src/f90/mod/mpi\_alm\_tools.f90

This subroutine complements the master routine mpi\_map2alm, and should be run by all slaves in the current MPI communicator. It is run without arguments, but after an appropriate call to initialize\_mpi\_alm\_tools.

## **FORMAT**

call mpi\_map2alm\_slave()

#### ARGUMENTS

None.

#### **EXAMPLE:**

This example 1) initializes the mpi\_alm\_tools module (i.e., allocates internal arrays and defines required parameters), 2) executes a parallel map2alm operation, and 3) frees the previously allocated memory.

#### MODULES & ROUTINES

This section lists the modules and routines used by mpi\_map2alm\_slave.

alm\_tools module

# RELATED ROUTINES

This section lists the routines related to  ${\bf mpi\_map2alm\_slave}.$ 

$mpi\_cleanup\_alm\_tools$	Frees memory that is allocated by the current routine.
$mpi\_initialize\_alm\_tools$	Allocates memory and defines variables for the mpi_alm_tools module.
$mpi\_alm2map$	Routine for executing a parallel inverse spherical harmonics transform (root processor interface)
$mpi\_alm2map\_slave$	Routine for executing a parallel inverse spherical harmonics transform (slave processor interface)
${ m mpi\_map2alm}$	Routine for executing a parallel spherical harmonics transform (root processor interface)
$mpi\_alm2map\_simple$	One-line interface to the parallel inverse spherical harmonics transform
$mpi\_map2alm\_simple$	One-line interface to the parallel spherical harmonics transform

nArguments 123

# nArguments

Location in HEALPix directory tree: src/f90/mod/extension.F90

This function emulates the C routine iargc, which returns the number of command line arguments provided.

**FORMAT** var=nArguments()

# **ARGUMENTS**

name&dimensionality	kind	in/out	description
var	I4B	OUT	number of command line arguments

#### RELATED ROUTINES

This section lists the routines related to **nArguments**.

getEnvironment returns value of environment variable getArgument returns list of command line arguments

# $neighbours\_nest$

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

This subroutine returns the number and locations (in terms of pixel numbers) of the topological neighbours of a central pixel. The pixels are ordered in a clockwise sense about the central pixel with the southernmost pixel in first element. For the 4 pixels in the southern corners of the equatorial faces which have two equally southern neighbours the routine returns the southwestern pixel first and proceeds clockwise.

#### **FORMAT**

call neighbours\_nest(nside, ipix, list, nneigh)

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
nside	I4B	IN	The $N_{side}$ parameter of the map.
ipix	I4B	IN	The pixel number of the central pixel.
list(8)	I4B	OUT	On exit, the vector of neighbouring pixels. This contains nneigh relevant elements.
nneigh	I4B	OUT	The number of neighbours (mostly 8, except at 8 sites, where there are only 7 neighbours).

#### **EXAMPLE:**

use pix\_tools

integer :: n, list(1:8)

call neighbours\_nest(4, 1, list, nneigh)

print\*,nneigh

print\*,list(1:nneigh)

neighbours\_nest 125

This returns nneigh= 8 and a vector list, which contains the pixel numbers (90, 0, 2, 3, 6, 4, 94, 91).

#### MODULES & ROUTINES

This section lists the modules and routines used by **neighbours\_nest**.

mk\_xy2pix, mk\_pix2xy precomputing arrays for the conversion of

NESTED pixel numbers to Cartesian coords in

each face.

pix2xy\_nest, xy2pix\_nest Conversion between NESTED pixel numbers to

Cartesian coords in each face.

**bit\_manipulation** module, containing:

invMSB, invLSB,swapLSBMSB,invswapLSBMSB functions which manip-

ulate the bit vector which represents the NESTED pixel numbers. They correspond to NorthWest;-¿SouthEast, SouthWest;-¿NorthEast, East;-¿West and North-South flips of the diamond

faces, respectively.

## RELATED ROUTINES

This section lists the routines related to **neighbours\_nest**.

pix2ang, ang2pix convert between angle and pixel number.

pix2vec, vec2pix convert between a cartesian vector and pixel num-

ber.

# npix2nside

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Function to provide the resolution parameter  $N_{\rm side}$  corresponding to  $N_{\rm pix}$  pixels over the full sky.

FORMAT var=npix2nside(npix)

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
npix	I4B	IN	the number $N_{\text{pix}}$ of pixels over the whole sky.
var	I4B	OUT	the parameter $N_{\rm side}$ . If $N_{\rm pix}$ is valid (12 times a power of 2 in $\{1, \dots, 8192\}$ ), $N_{\rm side} = \sqrt{N_{\rm pix}/12}$ is returned; if not, an error message is issued and -1 is returned.

#### **EXAMPLE:**

nside= npix2nside(786432)

Returns the resolution parameter  $N_{\text{side}}$  (256) corresponding to 786432 pixels on the sky.

#### RELATED ROUTINES

This section lists the routines related to **npix2nside**.

nside2npix returns the number of pixels  $N_{\rm pix}$  corresponding to resolution parameter  $N_{\rm side}$ 

nside2npix 127

# nside2npix

Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Function to provide the number of pixels  $N_{\rm pix}$  over the full sky corresponding to resolution parameter  $N_{\rm side}$ .

**FORMAT** 

var = nside 2npix(nside)

# **ARGUMENTS**

name & dimensionality	kind	in/out	description
nside	I4B	IN	the $N_{\rm side}$ parameter of the map. the number of pixels $N_{\rm pix}$ of the map. If $N_{\rm side}$ is valid (a power of 2 in $\{1,\ldots,8192\}$ ), $N_{\rm pix}=12N_{\rm side}^2$ is returned; if not, an error message is issued and -1 is returned.
var	I4B	OUT	

## **EXAMPLE:**

npix= nside2npix(256)

Returns the number of **HEALPix** pixels (786432) for the resolution parameter 256.

#### RELATED ROUTINES

This section lists the routines related to **nside2npix**.

npix2nside

returns resolution parameter corresponding to the number of pixels.

# nside2ntemplates

Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Function to provide the number of template pixels

$$N_{\text{templates}} = \frac{1 + N_{\text{side}}(N_{\text{side}} + 6)}{4}$$

corresponding to resolution parameter  $N_{\text{side}}$ . Each template pixel has a different shape that  $can \ not$  be matched (by rotation or reflexion) to that of any of the other templates.

**FORMAT** 

var=nside2ntemplates(nside)

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
nside		IN	the $N_{\text{side}}$ parameter.
var		OUT	the number of template pixels $N_{\text{templates}}$ .

#### **EXAMPLE:**

ntpl= nside2ntemplates(256)

Returns in **ntpl** the number of **HEALPix** template pixels (16768) for the resolution parameter 256.

#### RELATED ROUTINES

This section lists the routines related to **nside2ntemplates**.

 $template\_pixel\_ring$ 

template\_pixel\_nest return the template pixel associated with any

**HEALPix** pixel

nside2ntemplates 129

 $same\_shape\_pixels\_ring \\ same\_shape\_pixels\_nest$ 

return the ordered list of pixels having the same shape as a given pixel template

# $number_of_alms$

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This function returns the number of  $a_{lm}$  values stored in each FITS extension in a FITS file containing  $a_{lm}$ 

FORMAT vai	=number_of_alms	(filename[	, extnum]	)
------------	-----------------	------------	-----------	---

# **ARGUMENTS**

name & dimensionality	kind	in/out	description
filename(LEN = filenamelen)	CHR	IN	filename of the FITS-file con-
extnum	I4B	OUT	taining $a_{\ell m}$ .  number of extensions in the file

## **EXAMPLE:**

print\*,number\_of\_alms('alms.fits')

Prints the number of  $a_{lm}$  stored in each extension of the file 'alms.fits'

## MODULES & ROUTINES

This section lists the modules and routines used by **number\_of\_alms**.

fitstools	module, containing:
printerror	routine for printing FITS error messages.
${f cfitsio}$	library for FITS file handling.

number\_of\_alms 131

# RELATED ROUTINES

This section lists the routines related to **number\_of\_alms**.

 $fits 2 alms, \ read\_conbintab$ 

routines that read  $a_{lm}$  values from FITS files.

# output\_map\*

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine writes a full sky **HEALPix** map into a FITS file. The map can be either single or double precision real. It *has* to be 2-dimensional.

#### ARGUMENTS

name & dimensionality	kind	in/out	description
map(0:,1:)	SP/ DP	IN	full sky map(s) to be output
header(LEN=80)(1:)	CHR	IN	string array containing the FITS header to be included in the file
filename(LEN=*)	CHR	IN	filename of the FITS-file to contain <b>HEALPix</b> map(s).
extno	I4B	IN	extension number in which to write the data (0 based). ( <b>default:</b> 0)

## **EXAMPLE:**

output\_map\* 133

#### MODULES & ROUTINES

This section lists the modules and routines used by **output\_map\***.

fitstools module, containing:

routine for printing FITS error messages. printerror

 $write\_bintab$ routine to write a binary table into a FITS file.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to **output\_map\***.

executable that reads a **HEALPix** map from a anafast

FITS file and analyses it.

synfast executable that generate full sky **HEALPix** maps input\_map

subroutine to read a **HEALPix** map from a a

FITS file

write\_bintabh subroutine to write a large array into a FITS file

piece by piece

input\_tod\* subroutine to read an arbitrary subsection of a

large binary table

write\_minimal\_header routine to write minimal FITS header

# $parse\_xxx$

Location in HEALPix directory tree: src/f90/mod/paramfile\_io.F90

The Fortran 90 module paramfile  $\perp$  io contains functions to obtain parameters from parameter files or interactively

# **ARGUMENTS**

parse\_xxx 135

name&dimensionality	kind	in/out	description
fname	CHR	IN	file containing the simulation parameters. If empty, parameters are obtained interactively.
handle	PMF	INOUT	Object of type (paramfile_handle) used to store parameter information
keyname	CHR	IN	name of the required parameter
default	XXX	IN	optional argument containing the default value for a given simulation parameter; must be of appropriate type.
vmin	XXX	IN	optional argument containing the minimum value for a given simulation parameter; must be of appropriate type.
vmax	XXX	IN	optional argument containing the maximum value for a given simulation parameter; must be of appropriate type.
descr	CHR	IN	optional argument containing a description of the required simulation parameter
filestatus	CHR	IN	optional argument. If present, the parameter must be a valid filename. If filestatus=='new', the file must not exist; if filestatus=='old', the file must exist.
code	CHR	IN	optional argument. Contains the name of the executable.
silent	LGT	IN	optional argument. If set to .true. the parsing routines will run silently in non-interactive mode (except for warning or error messages, which will always appear). This is mainly intended for MPI usage where many processors parse the same parameter file: silent can be set to .true. on all CPUs except one.

#### **ROUTINES:**

```
handle = parse_init (fname [,silent])
  initializes the parser to work on the file fname, or interactively, if fname is empty
intval = parse_int (handle, keyname [, default, vmin, vmax, descr])
longval = parse_long (handle, keyname [, default, vmin, vmax, descr])
realval = parse_real (handle, keyname [, default, vmin, vmax, descr])
doubleval = parse_double (handle, keyname [, default, vmin, vmax, descr])
stringval = parse_string (handle, keyname [, default, descr, filestatus])
logicval = parse_lgt (handle, keyname [, default, descr])
```

These routines obtain integer(i4b), integer(i8b), real(sp), real(dp), character(len=\*) and logical values, respectively.

Note: parse\_string will expand all environment variables of the form \${XXX} (eg: \${HOME}). It will also replace a leading ~/ by the user's home directory.

```
call parse_summarize (handle [, code])
```

if the parameters were set interactively, this routine will print out a parameter file performing the same settings.

```
call parse_check_unused (handle [, code])
```

if a parameter file was read, this routine will print out all the parameters found in the file but not used by the code. Intended at detecting typos in parameter names.

```
call parse_finish (handle)
```

frees the memory

#### **EXAMPLE:**

```
program who_r_u
use healpix_types
use paramfile_io
use extension

implicit none
type(paramfile_handle) :: handle
character(len=256) :: parafile, name
real(DP) :: age

parafile = ''
if (nArguments() == 1) call getArgument(1, parafile)
handle = parse_init(parafile)
name = parse_string(handle, 'name',descr='Enter your last name: ')
age = parse_double(handle, 'age', descr='Enter your age in years: ', &
```

parse\_xxx 137

```
& default=18.d0,vmin=0.d0)
call parse_summarize(handle, 'who_r_u')
end program who_r_u
```

If a file is provided as command line argument when running the executable who\_r\_u, that file will be parsed in search of the lines starting with 'name =' and 'age =', otherwise the same questions will be asked interactively.

## RELATED ROUTINES

This section lists the routines related to parse\_xxx.

concatnl generates from a set of strings the multi-line description

nArguments returns the number of command line arguments getArgument returns the list of command line arguments

# pixel\_window

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine returns the averaged  $\ell$ -space window function  $w_{\text{pix}}(\ell)$  (for temperature and polarisation) associated to **HEALPix** pixels of resolution parameter  $N_{\text{side}}$ . Because of the integration of the signal over the pixel area, the  $a_{lm}^{(\text{pix})}$  coefficients of a pixelized map are related to the unpixelized underlying  $a_{lm}$  by  $a_{lm}^{(\text{pix})} = a_{lm}w_{\text{pix}}(\ell)$ .

Unless specified otherwise, the  $w_{\rm pix}(\ell)$  are read from the files  $HEALPIX/data/pixel\_window\_n????.fits.$ 

# **FORMAT**

call pixel\_window(pixlw, nside [, windowfile])

#### **ARGUMENTS**

name & dimensionality	kind	in/ou	ıtdescription
pixlw(0:lmax,1:p)	DP	OUT	pixel window function(s) $w_{\rm pix}(\ell)$ generated. The first index must be $\ell_{\rm max} \leq 4N_{\rm side}$ . The second index runs from 1:1 for temperature only, and 1:3 for polarisation. In the latter case, 1=T, 2=E, 3=B.
nside	I4B	IN	<b>HEALPix</b> $N_{\text{side}}$ resolution parameter. Unless windowfile is set, the file associated with $N_{\text{side}}$ and shipped with the package is read by default. If $nside = 0$ , the pixel is assumed infinitely small and $pixlw$ is returned with value 1.
windowfile (OPTIONAL)	CHR	IN	FITS file containing the pixel window to be read instead of the default.

#### **EXAMPLE:**

call pixel\_window(pixlw, 64)

pixel\_window 139

returns in pixlw the pixel window function for  $N_{\text{side}} = 64$ .

## MODULES & ROUTINES

This section lists the modules and routines used by **pixel\_window**.

misc\_utils module, containing:

assert, fatal\_error interrupt code in case of error

**extension** module, containing:

getEnvironment read environment variable

fitstools module, containing:

read\_dbintab reads double precision binary table

#### RELATED ROUTINES

This section lists the routines related to **pixel\_window**.

gaussbeam routine to generate a gaussian beam window func-

tion

generate\_beam returns a beam window function

alter\_alm, rotate\_alm modifies  $a_{lm}$  to emulate effect of real space filtering

and coordinate rotation respectively

alm2map synthetize a **HEALPix** map from its  $a_{lm}$  (or

 $a_{lm}^{(\text{pix})}$ ).

alm2map\_der synthetize a map and its derivatives from its  $a_{lm}$ 

(or  $a_{lm}^{(pix)}$ ).

# $\begin{array}{l} pix2xxx, ang2xxx, vec2xxx, \\ nest2ring, ring2nest \end{array}$

Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

The Fortran90 module pix\_tools contains some subroutines to convert between pixel number in the **HEALPix** map and  $(\theta, \phi)$  or (x, y, z) coordinates on the sphere. Some of these routines are listed here.

# **ARGUMENTS**

kind	in/out	description
I4B	IN	$N_{\rm side}$ parameter for the <b>HEALPix</b> map.
I4B		pixel identification number in NESTED
		scheme over the range $\{0, N_{\text{pix}} - 1\}$ .
I4B		pixel identification number in RING scheme
		over the range $\{0, N_{\text{pix}} - 1\}$ .
DP	_	colatitude in radians measured southward
		from north pole in $\{0,\pi\}$ .
DP	_	longitude in radians, measured eastward in
		$[0, 2\pi].$
DP		three dimensional cartesian position vector
		(x, y, z). The north pole is $(0, 0, 1)$ . An out-
		put vector is normalised to unity.
DP	OUT	three dimensional cartesian position vectors
		(x, y, z) (normalised to unity) pointing to the
		4 vertices of a given pixel. The four vertices
		are listed in the order North, West, South,
		East.
	I4B I4B DP DP DP	I4B — I4B — DP — DP — DP —

#### **ROUTINES:**

call pix2ang\_ring(nside, ipring, theta, phi)

renders theta and phi coordinates of the nominal pixel center given the pixel number ipring and a map resolution parameter nside.

call pix2vec\_ring(nside, ipring, vector [,vertex])

renders cartesian vector coordinates of the nominal pixel center given the pixel number *ipring* and a map resolution parameter *nside*. Optionally renders cartesian vector coordinates of the considered pixel four vertices.

call ang2pix\_ring(nside, theta, phi, ipring)

renders the pixel number *ipring* for a pixel which, given the map resolution parameter *nside*, contains the point on the sphere at angular coordinates *theta* and *phi*.

call vec2pix\_ring(nside, vector, ipring)

renders the pixel number *ipring* for a pixel which, given the map resolution parameter *nside*, contains the point on the sphere at cartesian coordinates *vector*.

call pix2ang\_nest(nside, ipnest, theta, phi)

renders theta and phi coordinates of the nominal pixel center given the pixel number ipnest and a map resolution parameter nside.

call pix2vec\_nest(nside, ipnest, vector [,vertex])

renders cartesian vector coordinates of the nominal pixel center given the pixel number *ipnest* and a map resolution parameter *nside*. Optionally renders cartesian vector coordinates of the considered pixel four vertices.

call ang2pix\_nest(nside, theta, phi, ipnest)

renders the pixel number *ipnest* for a pixel which, given the map resolution parameter *nside*, contains the point on the sphere at angular coordinates *theta* and *phi*.

call vec2pix\_nest(nside, vector, ipnest)

renders the pixel number ipnest for a pixel which, given the map resolution parameter nside, contains the point on the sphere at cartesian coordinates vector.

call nest2ring(nside, ipnest, ipring)

performs conversion from NESTED to RING pixel number.

call ring2nest(nside, ipring, ipnest)

performs conversion from RING to NESTED pixel number.

#### MODULES & ROUTINES

This section lists the modules and routines used by pix2xxx,ang2xxx,vec2xxx, nest2ring,ring2nest.

mk\_pix2xy, mk\_xy2pix routines used in the co

routines used in the conversion between pixel values and "cartesian" coordinates on the Healpix

face.

#### RELATED ROUTINES

This section lists the routines related to pix2xxx,ang2xxx,vec2xxx, nest2ring,ring2nest.

neighbours\_nest find neighbouring pixels.

ang2vec convert  $(\theta, \phi)$  spherical coordinates into (x, y, z)

cartesian coordinates.

vec2ang convert (x, y, z) cartesian coordinates into  $(\theta, \phi)$ 

spherical coordinates.

convert\_inplace in-place conversion between RING and NESTED

for integer/real/double maps.

convert\_nest2ring convert from NESTED to RING scheme using a

temporary array.

# planck\_rng

#### Location in HEALPix directory tree: src/f90/mod/rngmod.f90

The derived type planck\_rng is used by the Random Number Generation routines rand\_init, rand\_uni, rand\_gauss to describe fully the current RNG sequence.

Most users do not need to know about the planck\_rng definition. It may be useful for those wanting to take a snapshot of the RNG sequence they are using (by eg, dumping the latest values of planck\_rng structure on disk) so that the same sequence can be resumed later on from that same point.

The type planck\_rng is a structure defined as

name	type	definition
x, y, z, w	I4B	internal variables of uniform RNG
gset	DP	internal variable for Gaussian RNG
empty	LGT	flag used by Gaussian RNG

## RELATED ROUTINES

This section lists the routines related to **planck\_rng**.

${\rm rand\_gauss}$	function which returns a random normal deviate.
${ m rand}_{ ext{-}}{ m uni}$	function which returns a random uniform deviate.
$\operatorname{rand\_init}$	subroutine to initiate a random number sequence.

# plm\_gen

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine computes the latitude dependent part  $\lambda_{\ell m}$  of the spherical harmonics  $(Y_{\ell m}(\theta,\phi)=\lambda_{\ell m}(\theta)e^{im\phi})$  of spin 0 and 2 (see **HEALPix** primer) used to synthetize or analyze **HEALPix** maps of temperature and polarisation.

## **FORMAT**

call plm\_gen(nsmax, nlmax, nmmax, plm)

## **ARGUMENTS**

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	The $N_{\text{side}}$ value for which to compute the $\lambda_{\ell m}$ .
nlmax	I4B	IN	The maximum multipole order $\ell$ of the generated $\lambda_{lm}$ .
nmmax	I4B	IN	The maximum degree $m$ of the generated $\lambda_{lm}$ .
plm(0:n_plm-1, 1:p)	DP	OUT	The $\lambda_{lm}$ values, either for temperature only $(p=1)$ or temperature and polarisation $(p=3)$ . The number of $\lambda_{\ell m}$ is n-plm = nsmax*(nmmax+1)*(2*nlmax-nmmax+2). They are stored in the order of increasing order $\ell$ , increasing degree $m$ , for all the <b>HEALPix</b> ring colatitudes $\theta$ from North Pole to Equator, ie $\lambda_{00}(\theta_1)$ , $\lambda_{10}(\theta_1)$ , $\lambda_{20}(\theta_1)$ ,, $\lambda_{11}(\theta_1)$ , $\lambda_{21}(\theta_1)$ ;, $\lambda_{00}(\theta_2)$

# **EXAMPLE:**

plm\_gen 145

```
use healpix_types
use alm_tools, only : plm_gen
integer(I4B) :: nside, lmax, mmax, n_plm
real(DP), dimension(:,:), allocatable :: plm
...
nside=256 ; lmax=512 ; mmax=lmax
npix=nside2npix(nside)
n_plm=nside*(mmax+1)*(2*lmax-mmax+2)
allocate(plm(0:n_plm-1,1:3))
...
call plm_gen(nside, lmax, mmax, plm)
```

Computes the spherical harmonics for temperature and polarisation for  $N_{side} = 256$ , up to 512 in  $\ell$  and m.

#### MODULES & ROUTINES

This section lists the modules and routines used by **plm\_gen**.

compute\_lam\_mm, get\_pixel\_layout, gen\_lamfac,gen\_mfac, gen\_normpol, gen\_recfac, init\_rescale, l\_min\_ylm

Ancillary routines used for  $\lambda_{\ell m}$  recursion

misc\_utils module, containing:

assert\_alloc routine to print error message, when an array can

not be allocated properly

#### RELATED ROUTINES

This section lists the routines related to plm\_gen.

alm2map routine generating maps of temperature and po-

larisation from their  $a_{\ell m}$  that can use precom-

puted  $\lambda_{\ell m}$  generated by plm\_gen

map2alm routine analysing maps of temperature and polar-

isation that can use precomputed  $\lambda_{\ell m}$  generated

by plm\_gen

plmgen executable using plm-gen to compute the  $\lambda_{\ell m}$  and

writting them on disc

query\_disc 147

# $query\_disc$

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to find the index of all pixels within an angular distance radius from a defined center. The output indices can be either in the RING or NESTED scheme

#### **FORMAT**

call query\_disc(nside, vector0, radius, listpix, nlist [, nest, inclusive])

#### **ARGUMENTS**

name & dimensional-	kind	in/out	description
ity			
nside	I4B	IN	the $N_{side}$ parameter of the map.
vector 0(3)	DP	IN	cartesian vector pointing at the disc center.
radius	DP	IN	disc radius in radians.
listpix(0:*)	I4B	OUT	the index for all pixels within radius.
- ,			Make sure that the size of the array is big
			enough to contain all pixels.
nlist	I4B	OUT	The number of pixels listed in <i>listpix</i> .
nest (OPTIONAL)	I4B	IN	The pixel indices are in the NESTED num-
,			bering scheme if nest=1, and in RING
			scheme otherwise.
inclusive (OPTIONAL)	I4B	IN	If set to 1, all the pixels overlapping (even
,			partially) with the disc are listed, other-
			wise only those whose center lies within the
			disc are listed.

#### **EXAMPLE:**

call query\_disc(256,(/0,0,1/),pi/2,listpix,nlist,nest=1)

Returns the NESTED pixel index of all pixels north of the equatorial line in a  $N_{side}=256$  map.

#### MODULES & ROUTINES

This section lists the modules and routines used by query\_disc.

in\_ring routine to find the pixels in a certain slice of a

given ring.

ring\_num function to return the ring number corresponding

to the coordinate z

#### RELATED ROUTINES

This section lists the routines related to query\_disc.

pix2ang, ang2pix convert between angle and pixel number.

pix2vec, vec2pix convert between a cartesian vector and pixel num-

ber.

query\_disc, query\_polygon,

query\_strip, query\_triangle render the list of pixels enclosed respectively in a

given disc, polygon, latitude strip and triangle

query\_polygon 149

# query\_polygon

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to find the index of all pixels enclosed in a polygon. The polygon should be convex, or have only one concave vertex. The edges should not intersect each other. The output indices can be either in the RING or NESTED scheme

# FORMAT call query\_polygon(nside, vlist, nv, listpix, nlist [, nest, inclusive])

#### **ARGUMENTS**

name & dimension-	kind	in/out	description	
ality				
nside	I4B	IN	the $N_{side}$ parameter of the map.	
vlist(1:3,0:*)	DP	IN	cartesian vector pointing at polygon respec- tive vertices.	
nv	I4B	IN	number of vertices, should be equal to 3 or larger.	
listpix(0:*)	I4B	OUT	the index for all pixels enclosed in the triangle. Make sure that the size of the array is big enough to contain all pixels.	
nlist	I4B	OUT	The number of pixels listed in <i>listpix</i> .	
nest (OPTIONAL)	I4B	IN	The pixel indices are in the NESTED numbering scheme if nest=1, and in RING scheme otherwise.	
inclusive (OP-TIONAL)	I4B	IN	If set to 1, all the pixels overlapping (even partially) with the polygon are listed, otherwise only those whose center lies within the polygon are listed.	

#### **EXAMPLE:**

real(dp), dimension(1:3,0:9) :: vertices vertices(:,0) = (/0.,0.,1./) ! +z

```
vertices(:,1) = (/1.,0.,0./) ! +x
vertices(:,2) = (/1.,1.,-1./) ! x+y-z
vertices(:,3) = (/0.,1.,0./) ! +y
call query_polygon(256,vertices,4,listpix,nlist,nest=0)
```

Returns the RING pixel index of all pixels in the polygon with vertices of cartesian coordinates (0,0,1), (1,0,0), (1,1,-1) and (0,1,0) in a  $N_{side}=256$  map.

#### MODULES & ROUTINES

This section lists the modules and routines used by query\_polygon.

isort	routine to sort integer number
${\it query\_triangle}$	render the list of pixels enclosed in a given triangle
$surface\_triangle$	computes the surface of a spherical triangle defined by $3$ vertices
$\operatorname{vect\_prod}$	routine to compute the vectorial product of two 3D vectors

#### RELATED ROUTINES

This section lists the routines related to query\_polygon.

pix2ang, ang2pix	convert between angle and pixel number.
pix2vec, vec2pix	convert between a cartesian vector and pixel num-
	ber.
query_disc, query_polygon,	
query_strip, query_triangle	render the list of pixels enclosed respectively in a
	given disc, polygon, latitude strip and triangle

query\_strip 151

# query\_strip

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to find the index of all pixels enclosed in a latitude strip. The output indices can be either in the RING or NESTED scheme

# FORMAT call query\_strip(nside, theta1, theta2, listpix, nlist [, nest, inclusive])

#### **ARGUMENTS**

name&dimensionalitykind		in/out	description	
nside	I4B	IN	the $N_{side}$ parameter of the map.	
theta1	DP	IN	colatitude lower bound in radians measured	
			from North Pole (between 0 and $\pi$ ).	
theta2	DP	IN	colatitude upper bound in radians mea-	
			sured from North Pole (between 0 and	
			$\pi$ ). If theta1< theta2, the pixels lying in	
			[theta1,theta2] are output, otherwise, the	
			pixel lying in [0, theta2] and those lying in	
			[theta1, $\pi$ ] are output.	
listpix(0:*)	I4B	OUT	the index for all pixels enclosed in the strip(s).	
			Make sure that the size of the array is big	
	T.(D)	0.1177	enough to contain all pixels.	
nlist	I4B	OUT	The number of pixels listed in <i>listpix</i> .	
nest (OPTIONAL)	I4B	IN	The pixel indices are in the NESTED num-	
			bering scheme if nest=1, and in RING scheme	
	TAD	T. T.	otherwise.	
inclusive (OP-	I4B	IN	If set to 1, all the pixels overlapping (even	
TIONAL)			partially) with the strip are listed; otherwise	
			only those whose center lies within the strip	
			are listed.	

#### **EXAMPLE:**

call query\_strip(256,0.75\*PI,0.2\*PI,listpix,nlist,nest=1)

Returns the NESTED pixel index of all pixels with colatitude in  $[0,\pi/5]$  and those with colatitude in  $[3\pi/4,\pi]$ 

#### MODULES & ROUTINES

This section lists the modules and routines used by query\_strip.

in_ring	routine to find the pixels in a certain slice of a given ring.
$intrs\_intrv$	routine to compute the intersection of 2 intervals on a circle
${ m ring\_num}$	function to return the ring number corresponding to the coordinate $\boldsymbol{z}$
vect_prod	routine to compute the vectorial product of two 3D vectors

#### RELATED ROUTINES

This section lists the routines related to query\_strip.

pix2ang, ang2pix	convert between angle and pixel number.
pix2vec, vec2pix	convert between a cartesian vector and pixel num-
	ber.
query_disc, query_polygon,	
query_strip, query_triangle	render the list of pixels enclosed respectively in a
	given disc, polygon, latitude strip and triangle
$surface\_triangle$	computes the surface of a spherical triangle de-
	fined by 3 vertices

query\_triangle 153

# query\_triangle

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to find the index of all pixels enclosed in a spherical triangle described by its three vertices. The output indices can be either in the RING or NESTED scheme

# FORMAT call query\_triangle(nside, v1, v2, v3, listpix, nlist [, nest, inclusive])

#### **ARGUMENTS**

name&dimensionality	kind in/out		description		
nside	I4B	IN	the $N_{side}$ parameter of the map.		
v1(3)	DP	IN	cartesian vector pointing at the triangle		
			first vertex.		
v2(3)	DP	IN	cartesian vector pointing at the triangle		
			second vertex.		
v3(3)	DP	IN	cartesian vector pointing at the triangle		
			third vertex.		
listpix(0:*)	I4B	OUT	the index for all pixels enclosed in the tri-		
			angle. Make sure that the size of the array		
			is big enough to contain all pixels.		
$\operatorname{nlist}$	I4B	OUT	The number of pixels listed in $listpix$ .		
nest (OPTIONAL)	I4B	IN	The pixel indices are in the NESTED num-		
			bering scheme if nest=1, and in RING		
			scheme otherwise.		
inclusive (OPTIONAL)	I4B	IN	If set to 1, all the pixels overlapping (even		
			partially) with the triangle are listed, oth-		
			erwise only those whose center lies within		
			the triangle are listed.		

#### **EXAMPLE:**

call query\_triangle(256, (/1,0,0/), (/0,1,0/), (/0,0,1/), listpix, nlist)

Returns the RING pixel index of the (98560) pixels in the octant (x, y, z > 0) in a  $N_{side} = 256$  map.

#### MODULES & ROUTINES

This section lists the modules and routines used by query\_triangle.

in\_ring routine to find the pixels in a certain slice of a given ring. intrs\_intrv routine to compute the intersection of 2 intervals on a circle ring\_num function to return the ring number corresponding to the coordinate zvect\_prod routine to compute the vectorial product of two

3D vectors

#### RELATED ROUTINES

This section lists the routines related to query\_triangle.

pix2ang, ang2pix convert between angle and pixel number. pix2vec, vec2pix convert between a cartesian vector and pixel number. query\_disc, query\_polygon, query\_strip, query\_triangle render the list of pixels enclosed respectively in a given disc, polygon, latitude strip and triangle surface\_triangle computes the surface of a spherical triangle defined by 3 vertices

rand\_gauss 155

# rand\_gauss

#### Location in HEALPix directory tree: src/f90/mod/rngmod.f90

This routine returns a number out of a pseudo-random normal deviate (ie, its probability distribution is a Gaussian of mean 0 and variance 1).

**FORMAT** 

var=rand\_gauss(rng\_handle)

#### ARGUMENTS

name & dimensionality	kind	in/out	description
rng_handle	planck_rng	INOUT	structure of type planck_rng containing on all information
var	DP	OUT	necessary to continue same ran- dom sequence. number belonging to a pseudo- random normal deviate.

#### **EXAMPLE:**

use healpix\_types

use rngmod

type(planck\_rng) :: rng\_handle

real(dp) :: gauss

call rand\_init(rng\_handle, 12345, 6789012)

gauss = rand\_gauss(rng\_handle)

initiates a random sequence with the pair of seeds (12345, 6789012), and generates one number out of the normal deviate.

#### RELATED ROUTINES

This section lists the routines related to  ${\bf rand\_gauss}$ .

planck_rng	derived type describing RNG state
${ m rand}\_{ m uni}$	function which returns a random uniform deviate.
$\operatorname{rand\_init}$	subroutine to initiate a random number sequence.

rand\_init 157

## rand\_init

#### Location in HEALPix directory tree: src/f90/mod/rngmod.f90

This routine initializes, with up to 4 seeds, a randomn number sequence. The generator being primed is an F90 port of an xorshift generator described in Marsaglia, Journal of Statistical Software 2003, vol 8. It has a theoretical period of  $2^{128} - 1 \approx 3.410^{38}$ . Please refer to the "Comment on Random Number Generator" in the Fortran90 facilities guidelines.

#### **FORMAT**

call rand\_init(rng\_handle, [seed1, seed2, seed3, seed4])

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
rng_handle	planck_rng	OUT	structure of type planck_rng containing on output all infor- mation necessary to continue
seed1 (OPTIONAL)	I4B	IN	same random sequence. first seed of the random sequence. Can be of arbitray sign. If set to zero or not provided will be replaced internally by a
seed2 (OPTIONAL)	I4B	IN	non-zero hard coded value. second seed. Same properties as above
seed3 (OPTIONAL) seed4 (OPTIONAL)	I4B I4B	IN IN	third seed. Same as above. fourth seed. Same as above.

#### **EXAMPLE:**

use rngmod

type(planck\_rng) :: rng\_handle

call rand\_init(rng\_handle, 12345, 6789012)

initiates a random sequence with the pair of seeds (12345, 6789012).

#### RELATED ROUTINES

This section lists the routines related to rand\_init.

planck\_rng derived type describing RNG state

rand\_gauss function which returns a random normal deviate.
rand\_uni function which returns a random uniform deviate.

rand\_uni 159

### rand\_uni

#### Location in HEALPix directory tree: src/f90/mod/rngmod.f90

This routine returns a number out of a pseudo-random uniform deviate (ie, its probability distribution is uniform in the range ]0,1[).

**FORMAT** 

var=rand\_uni(rng\_handle)

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
rng_handle	planck_rng	INOUT	structure of type planck_rng containing on all information
var	DP	OUT	necessary to continue same ran- dom sequence. number belonging to a pseudo- random uniform deviate.

#### **EXAMPLE:**

use healpix\_types
use rngmod

type(planck\_rng) :: rng\_handle

real(dp) :: uni

call rand\_init(rng\_handle, 12345, 6789012)
uni = rand\_uni(rng\_handle)

initiates a random sequence with the pair of seeds (12345, 6789012), and generates one number out of the uniform deviate.

#### RELATED ROUTINES

This section lists the routines related to rand\_uni.

planck\_rng rand\_gauss rand\_init derived type describing RNG state function which returns a random normal deviate. subroutine to initiate a random number sequence. read\_asctab\*

# $\underline{read}_asctab^*$

# read\_bintab\*

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads a **HEALPix** map from a binary FITS-file. The routine can read a temperature map or both temperature and polarisation maps (T,Q,U)

#### **FORMAT**

call read\_bintab\*(filename, map, npixtot, nmaps, nullval, anynull [,header, units, extno])

#### **ARGUMENTS**

name &d imensionality	kind	in/ou	tdescription
filename(LEN=filenamelen)	CHR	IN	filename of FITS-file containing the map(s).
npixtot	I4B	IN	Number of pixels to be read from map.
nmap	I4B	IN	number of maps to be read, 1 for temperature only, and 3 for $(T,Q,U)$ .
map(0:npixtot-1,1:nmap)	SP/ DP	OUT	the map read from the FITS-file.
nullval	SP/ DP	OUT	value of missing pixels in the map.
anynull	LGT	OUT	TRUE, if there are missing pixels, and FALSE otherwise.
header(LEN=80)(1:) (OPTIONAL)	CHR	OUT	character string array containing the FITS header read from the file. Its dimension has to be defined prior to calling the routine
units(LEN=*)(1:nmaps) (OPTIONAL)	CHR	OUT	character string array containing the physical units of each map read
extno (OPTIONAL)	I4B	IN	extension number to read the data from (0 based).( <b>default:</b> 0) (the first extension is read)

read\_bintab\*

#### **EXAMPLE:**

call read\_bintab ('map.fits',map,12\*32\*\*2,1,nullval,anynull)

Reads a **HEALPix** temperature map from the file 'map.fits' to the array map(0:12\*32\*\*2-1,1:1). The pixel number 12\*32\*\*2 is the number of pixels in a  $N_{\rm side}=32$  **HEALPix** map. If there are missing pixels in the file, anynull is TRUE and these pixels get the value returned in nullval.

#### MODULES & ROUTINES

This section lists the modules and routines used by read\_bintab\*.

fitstools module, containing:

printerror routine for printing FITS error messages.

**cfitsio** library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to read\_bintab\*.

input\_map Routine which reads a map using read\_bintab\*and

fills missing pixels with a given value.

map2alm Routine which analyse a map and returns the  $a_{lm}$ 

coefficients.

read\_fits\_cut4 Routine to read cut sky **HEALPix** FITS maps

write\_plm, write\_bintab Routines to write **HEALPix** FITS maps

# read\_conbintab\*

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads a FITS file containing  $a_{lm}$  values for constained realisation. The FITS file is supposed to contain one integer column with  $index = \ell^2 + \ell + m + 1$  and 2 or 4 single (or double) precision columns with real/imaginary  $a_{lm}$  values and real/imaginary standard deviation on these  $a_{lm}$ . It is supposed to contain either 1 or 3 extension(s) containing respectively the  $a_{lm}$  for T and if applicable E and B.

#### **FORMAT**

call read\_conbintab\*(filename, alms, nalms [, units, extno])

#### **ARGUMENTS**

name&dimensionality	kind	in/oı	utdescription
filename(LEN=filenamelen) nalms	CHR I4B	IN IN	filename of FITS file containing $a_{lm}$ . Number of $a_{lm}$ values to read from the file.
alms(0:nalms-1,1:6)	SP/ DP	OUT	
units(len=20)(1:) (OPTIONAL)	CHR	OUT	character string containing the units of the $a_{\ell m}$
extno TIONAL)	I <b>4B</b> P-	- IN	extension (0 based) of the FITS file to be read

read\_conbintab\*

#### **EXAMPLE:**

call read\_conbintab ('alms.fits',alms,65\*66/2)

Read 65\*66/2 (the number of  $a_{lm}$  needed to fill the whole range from l=0 to l=64)  $a_{lm}$  values from the file 'alms.fits' into the array alms(0:65\*66/2-1,1:6).

#### MODULES & ROUTINES

This section lists the modules and routines used by **read\_conbintab\***.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to **read\_conbintab\***.

alms2fits, dump\_alms routines to write  $a_{lm}$  to a FITS-file

fits2alms has the same function as read\_conbintab but is

more general.

number\_of\_alms, [getsize\_fits] can be used to find out the number of  $a_{lm}$  avail-

able in the file.

# read\_dbintab

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads a double precision binary array from a FITS-file. It is used by **HEALPix** to read precomputed  $P_{lm}(\theta)$  values and pixel window functions.

FORMAT call read\_dbintab(filename, map, npixtot, nmaps, nullval, anynull, units)

#### **ARGUMENTS**

name & dimensionality	kind	$_{ m in/out}$	$\operatorname{description}$
filename(LEN=filenamelen)	CHR	IN	filename of FITS-file containing the double precision array.
npixtot	I4B	IN	Number of values to be read from the file.
nmaps	I4B	IN	number of 1-dim. arrays, 1 for scalar $P_{lm}$ s and pixel windows, 3 for scalar and tensor $P_{lm}$ s.
map(0:npixtot-1,1:nmaps)	DP	OUT	the array read from the FITS-file.
nullval	DP	OUT	value of missing pixels in the array.
anynull	LGT	OUT	TRUE, if there are missing pixels, and FALSE otherwise.
units(len=20)(1:nmaps)	CHR	OUT	respective physical units of the maps in the FITS file.

read\_dbintab 167

#### **EXAMPLE:**

call read\_dbintab ('plm\_32.fits',plm,65\*66\*32,1,nullval,anynull)

Reads precomputed scalar  $P_{lm}(\theta)$  from the file 'plm\_32.fits'. The values are returned in the array plm(0:65\*66\*32,1:1). The number of values 65\*66\*32 is the number of precomputed  $P_{lm}(\theta)$  for a  $N_{side}=32$ , lmax=64 map. If there are missing values in the file, anynull is TRUE and nullval contains the values of these pixels.

#### MODULES & ROUTINES

This section lists the modules and routines used by read\_dbintab.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to read\_dbintab.

plmgen Executable to create files with precomputed

 $P_{lm}(\theta)$ .

write\_dbintab Routine to create a file to be read by read\_dbintab.

# read\_fits\_cut4

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads a cut sky **HEALPix** map from a FITS file. The format used for the FITS file follows the one used for Boomerang98 and is adapted from COBE/DMR

# FORMAT call read\_fits\_cut4(filename, np, pixel, [signal, n\_obs, serror, header, units, extno])

#### **ARGUMENTS**

name&dimensionality	kind	in/outdescription		
filename(LEN=filenamelen)CHR		IN	FITS file to be read from, containing a cut sky map	
np	I4B	IN	number of pixels to be read from the file	
pixel(0:np-1)	I4B	OUT	index of observed (or valid) pixels	
signal(0:np-1)	SP	OUT	value of signal in each observed pixel	
(OPTIONAL)				
$n_{-}obs(0:np-1)$	I4B	OUT	number of observation per pixel	
(OPTIONAL)				
serror(0:np-1)	SP	OUT	rms of signal in pixel. (For white noise, this	
(OPTIONAL)			would be $\propto 1/\sqrt{\text{n_obs}}$	
header(LEN=80)(1:)	CHR	OUT	FITS extension header	
(OPTIONAL)				
units(LEN=20)	CHR	OUT	maps units (applies only to Signal and Serror,	
(OPTIONAL)			which are assumed to have the same units)	
extno (OPTIONAL)	I4B	IN	extension number (0 based) for which map is	
			read. Default $= 0$ (first extension).	

read\_fits\_cut4

#### MODULES & ROUTINES

This section lists the modules and routines used by read\_fits\_cut4.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to read\_fits\_cut4.

anafast executable that reads a **HEALPix** map and anal-

yses it.

synfast executable that generate full sky **HEALPix** maps

getsize\_fits routine to know the size of a FITS file and its type

(eg, full sky vs cut sky)

input\_map all purpose routine to input a map of any kind

from a FITS file

output\_map subroutine to write a FITS file from a **HEALPix** 

map

write\_fits\_cut4 subroutine to write a cut sky map into a FITS file

## read\_par

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine reads the 'NSIDE', 'TFIELDS', 'MAX-LPOL', and optionally 'MAX-MPOL' keywords from a FITS-file. These keywords desribe  $N_{side}$ , number of datasets (maps) and maximum multipole  $\ell$  (order) and m (degree) value for the file. If a keyword is not found in the FITS file, a value of -1 is returned instead. The file could eg. be a **HEALPix** map, or a set of  $a_{lm}$  or precomputed  $P_{lm}(\theta)$ 

#### **FORMAT**

call read\_par( filename, nside, lmax, tfields [, mmax] )

#### **ARGUMENTS**

name & dimensionality	kind	in/oı	in/outdescription		
filename(LEN=filenamelen)	CHR	IN	filename of the FITS file.		
nside	I4B	OUT	'NSIDE' keyword value from the FITS		
			header.		
lmax	I4B	OUT	'MAX-LPOL' keyword value from the		
			FITS header.		
tfields	I4B	OUT	'TFIELDS' keyword value from the FITS		
			header.		
mmax (OPTIONAL)	I4B	OUT	'MAX-MPOL' keyword value from the		
,			FITS header.		

#### **EXAMPLE:**

call read\_par('plm\_128p.fits', nside, lmax, nhar)

Checks the  $N_{side}$  and maximum  $\ell$  value used for the precomputed  $P_{\ell m}(\theta)$  that are stored in the file 'plm\_128p.fits'. If the file also contains tensor harmonics, nhar is returned with the value 3, otherwise it is 1.

read\_par 171

#### MODULES & ROUTINES

This section lists the modules and routines used by **read\_par**.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to  ${\bf read\_par}.$ 

synfast, plmgen executables that produce FITS-files with key-

words relevant to this routine.

### $real_{fft}$

#### Location in HEALPix directory tree: src/f90/mod/healpix\_fft.F90

This routine performs a forward or backward Fast Fourier Transformation on its argument data.

FORMAT call real\_fft(data, backward)

#### **ARGUMENTS**

name & dimensionality	kind in/out	description
data(:)	XXX INOUT	array containing the input and output data. Can be of type real(sp) or real(dp)
backward	LGT IN	Optional argument. If present and true, perform backward transformation, else forward

#### **EXAMPLE:**

use healpix\_fft
call real\_fft (data, backward=.true.)

Performs a backward FFT on data.

#### RELATED ROUTINES

This section lists the routines related to real\_fft.

complex\_fft routine for FFT of complex data

remove\_dipole\*

# remove\_dipole\*

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

This routine provides a means to fit and remove the dipole and monopole from a **HEALPix** map. The fit is obtained by solving the linear system

$$\sum_{j=0}^{d^2-1} A_{ij} f_j = b_i \tag{15}$$

with, d = 1 or 2, and

$$b_i = \sum_{p \in \mathcal{P}} s_i(p)w(p)m(p), \tag{16}$$

$$A_{ij} = \sum_{p \in \mathcal{P}} s_i(p)w(p)s_j(p), \tag{17}$$

where  $\mathcal{P}$  is the set of valid, unmasked pixels, m is the input map, w is pixel weighting, while  $s_0(p) = 1$  and  $s_1(p) = x$ ,  $s_2(p) = y$ ,  $s_3(p) = z$  are respectively the monopole and dipole templates. The output map is then

$$m'(p) = m(p) - \sum_{i=0}^{d^2 - 1} f_i s_i(p).$$
 (18)

#### **FORMAT**

call remove\_dipole\*(nside, map, ordering, degree, multipoles, zbounds [, fmissval, mask, weights])

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
nside	I4B	IN	value of $N_{\text{side}}$ resolution parameter for in-
map(0:12*nside*nside-1)	SP/ DP	INOUT	put map  HEALPix map from which the monopole and dipole will be removed.  Those are removed from all unflagged pixels, even those excluded by the cut zounds or the mask.
ordering	I4B	IN	HEALPix scheme 1:RING, 2: NESTED
degree	I4B	IN	multipoles to fit and remove. It is either 0 (nothing done), 1 (monopole only) or 2 (monopole and dipole).
$\frac{\text{multipoles}(0:\text{degree*degree-}}{1)}$	DP	OUT	values of best fit monopole and dipole. The monopole is described as a scalar in the same units as the input map, the dipole as a 3D cartesian vector, in the same units.
zbounds(1:2)	DP	IN	section of the map on which to perform the fit, expressed in terms of $z = \sin(\operatorname{latitude}) = \cos(\theta)$ . If $z = \sin(1) < z = \cos(\theta)$ . If $z = \sin(1) < z = \cos(\theta)$ , the fit is performed on the strip $z = \cos(\theta) < z < z = \sin(1) < \cos(\theta)$ , the fit is performed outside of the strip $z = \sin(1) < \cos(\theta)$ .
fmissval (OPTIONAL)	SP/ DP	IN	value used to flag bad pixel on input (default: -1.6375e30). Pixels with that value are ignored during the fit, and left unchanged on output.
mask(0:12*nside*nside-1) (OPTIONAL)	SP/ DP	IN	mask of valid pixels. Pixels with $ \text{mask}  < 10^{-10}$ are not used for fit. Note: the map is <i>not</i> multiplied by the mask.
weights(0:12*nside*nside-1) (OPTIONAL)	SP/ DP	IN	weight to be given to each map pixel before doing the fit. By default pixels are given a uniform weight of 1. Note: the output map is <i>not</i> multiplied by the weights.

remove\_dipole\*

#### **EXAMPLE:**

```
s = sin(15.0_dp * PI / 180.0_dp)
call remove_dipole*(128, map, 1, 2, multipoles, (\ s, -s \) )
```

Will compute and remove the best fit monopole and dipole from a map with  $N_{\rm side} = 128$  in RING ordering scheme. The fit is performed on pixels with  $|b| > 15^{\circ}$ .

#### MODULES & ROUTINES

This section lists the modules and routines used by **remove\_dipole\***.

pix\_tools module, containing:

#### RELATED ROUTINES

This section lists the routines related to **remove\_dipole\***.

add\_dipole

routine to add a dipole and monopole to a map.

# ring\_analysis

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This subroutine computes the Fast Fourier Transform of a single ring of pixels and extends the computed coefficients up to the maximum m of the transform.

FORMAT	call	ring_analysis(nsmax,	nlmax,	nmmax,
	data	in, nph, dataout, kphi0)		

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
nsmax	I4B	IN	$N_{\rm side}$ of the map.
nlmax	I4B	IN	Maximum $\ell$ of the analysis.
nmmax	I4B	IN	Maximum $m$ of the analysis.
nph	I4B	IN	The number of points on the
			ring.
datain(0:nph-1)	DP	IN	Function values on the ring.
dataout(0:nmmax)	DPC	OUT	Fourier components, replicated
			to Nmmax.
kphi0	I4B	IN	0 if the first pixel on the ring is
_			at $\phi = 0$ ; 1 otherwise.

#### **EXAMPLE:**

call ring\_analysis(64,128,128,datain,8,dataout,0)

Returns the periodically extended complex Fourier Transform of data in in dataout. They are returned in the following order: 0 1 2 3 4 5 6 7 6 5 4 3 2 1 0.... The value kphi0=0 specifies that no phase factor needed to be applied, because the ring starts at  $\phi=0$ . ring\_analysis 177

#### MODULES & ROUTINES

This section lists the modules and routines used by ring\_analysis.

healpix\_fft module.

#### RELATED ROUTINES

This section lists the routines related to ring\_analysis.

ring\_synthesis Inverse transform (complex-to-real), used in

alm2map, alm2map\_der and synfast

### ring\_num

Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

This function returns the ring number for a z coordinate.

FORMAT var=ring\_num(nside, z)

#### **ARGUMENTS**

name&dimensionality	kind	in/out	description
nside z	I4B DP	IN IN	the $N_{side}$ parameter of the map. the z coordinate to find the ring number for.

#### **EXAMPLE:**

print\*,ring\_num(256, 0.5)

Prints the ring number of the ring at position z = 0.5.

#### MODULES & ROUTINES

This section lists the modules and routines used by ring\_num.

None

ring\_num 179

### RELATED ROUTINES

This section lists the routines related to  ${\bf ring\_num}.$ 

in\_ring Returns the pixels in a slice on a given ring.

# $\underline{\mathbf{ring\_syn}}$ thesis

Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

FORMAT	call ring_synthesis(nsmax,	nlmax,	nmmax,
	datain, nph, dataout, kphi0	))	

#### **ARGUMENTS**

kind	in/out	description
I4B	IN	$N_{\rm side}$ of the map.
I4B	IN	Maximum $\ell$ of the analysis.
I4B	IN	Maximum $m$ of the analysis.
I4B	IN	The number of points on the
		ring.
DPC	IN	Fourier components as com-
		puted from the $a_{lm}$ .
DP	OUT	Synthesized function values on
		the ring.
I4B	IN	0 if the first pixel on the ring is
		at $\phi = 0$ ; 1 otherwise.
	I4B I4B I4B I4B DPC	I4B IN I4B IN I4B IN DPC IN DP OUT

#### **EXAMPLE:**

call ring\_synthesis(64,128,128,datain,8,dataout,1)

This computes the inverse (complex-to-real) Fast Fourier Transform for the second ring from the pole, containing 8 pixels, for a map resolution of  $N_{\rm side}=64$ . 128 complex Fourier components contribute to these 8 pixels. The value kphi0=1 specifies that a phase factor needed to be applied to correctly rotate the ring into position on the **HEALPix** grid.

ring\_synthesis 181

#### MODULES & ROUTINES

This section lists the modules and routines used by **ring\_synthesis**.

healpix\_fft module.

#### RELATED ROUTINES

This section lists the routines related to ring\_synthesis.

ring\_analysis Forward transform, used in map2alm and anafast

## $rotate\_alm*$

#### Location in HEALPix directory tree: src/f90/mod/alm\_tools.f90

This routine transform the scalar (and tensor)  $a_{\ell m}$  coefficients to emulate the effect of an arbitrary rotation of the underlying map. The rotation is done directly on the  $a_{\ell m}$  using the Wigner rotation matrices, computed by recursion. To rotate the  $a_{\ell m}$  for  $\ell \leq \ell_{\rm max}$  the number of operations scales like  $\ell_{\rm max}^3$ .

# FORMAT call rotate\_alm\*(lmax, alm\_TGC, psi, theta, phi)

name & dimensionality	kind	in/out	description
nlmax alm_TGC(1:p,0:nlmax,0:nlmax)	I4B SPC/ DPC	IN INOUT	maximum $\ell$ value for the $a_{\ell m}$ . complex $a_{\ell m}$ values before and after rotation of the coordinate system. The first index here runs from 1:1 for temperature only, and 1:3 for po- larisation. In the latter case, 1=T, 2=E, 3=B.
psi	DP	IN	first rotation: angle $\psi$ about the z-axis. All angles are in radians and should lie in $[-2\pi,2\pi]$ , the rotations are active and the referential system is assumed to be right handed, the routine coordsys2euler_zyz can be used to generate the Euler angles $\psi, \theta, \varphi$ for rotation between standard astronomical coordinate systems;
theta	DP	IN	second rotation: angle $\theta$ about the original (unrotated) y-axis;
phi	DP	IN	third rotation: angle $\varphi$ about the original (unrotated) z-axis;

rotate\_alm\* 183

#### **EXAMPLE:**

```
use alm_tools, only: rotate_alm
...
call rotate_alm(64, alm_TGC, PI/3., 0.5_dp, 0.0_dp)
```

Transforms scalar and tensor  $a_{lm}$  for  $\ell_{max} = m_{max} = 64$  to emulate a rotation of the underlying map by  $(\psi = \pi/3, \theta = 0.5, \varphi = 0)$ .

#### **EXAMPLE:**

```
use coord_v_convert, only: coordsys2euler_zyz
use alm_tools, only: rotate_alm
...
call coordsys2euler_zyz(2000.0_dp, 2000.0_dp, 'E', 'G', psi, theta, phi)
call rotate_alm(64, alm_TGC, psi, theta, phi)
```

Rotate the  $a_{lm}$  from Ecliptic to Galactic coordinates.

#### RELATED ROUTINES

This section lists the routines related to **rotate\_alm\***.

coordsys2euler_zyz	can be used to generate the Euler angles $\psi, \theta, \varphi$ for rotation between standard astronomical coordinate systems
$create\_alm$	Routine to create $a_{\ell m}$ coefficients.
$alter\_alm$	Routine to modify $a_{\ell m}$ coefficients to apply or remove the effect of an instrumental beam.
m map2alm	Routines to analyze a <b>HEALPix</b> sky map into its $a_{\ell m}$ coefficients.
alm2map	Routines to synthetize a <b>HEALPix</b> sky map from its $a_{\ell m}$ coefficients.
$alms2 fits,  dump\_alms$	Routines to save a set of $a_{lm}$ in a FITS file.
$xcc\_v\_convert$	rotates a 3D coordinate vector from one astronom-

ical coordinate system to another.

## same\_shape\_pixels\_nest, same\_shape\_pixels\_ring

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

These routines provide the ordered list of all **HEALPix** pixels having the same shape as a given template, for a resolution parameter  $N_{\text{side}}$ . Depending on the template considered the number of such pixels is either 8, 16,  $4N_{\text{side}}$  or  $8N_{\text{side}}$ .

The template pixels are all located in the Northern Hemisphere, or on the Equator. They are chosen to have their center located at

$$\begin{split} z &= \cos(\theta) \geq 2/3, \qquad 0 < \phi \leq \pi/2, \\ 2/3 > z \geq 0, \qquad \phi = 0, \quad \text{or} \quad \phi = \frac{\pi}{4N_{\text{side}}}. \end{split}$$

They are numbered continuously from 0, starting at the North Pole, with the index increasing in  $\phi$ , and then increasing for decreasing z.

FORMAT	call same_shape_pixels_nest( nside,	template
	[, list, reflexion, nrep])	
	11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1

FORMAT call same\_shape\_pixels\_ring( nside, template [, list, reflexion, nrep])

name & dimensional-	kind	in/out	description
ity			
nside	I4B I4B	IN OUT	the <b>HEALPix</b> $N_{\text{side}}$ parameter.
template	14D	001	identification number(s) of the template matching in shape the pixel(s) provided (the numbering scheme of the pixel tem- plates is the same for both routines).
list(0:nrep-1)	I4B	OUT	pointer containing the ordered list of
OPTIONAL			NESTED/RING scheme identification numbers (in $\{0.12N_{\text{side}}^2 - 1\}$ ) of all pixels having the same shape as the template provided. The routines will allocate the list array if it is not allocated upon calling.
reflexion(0:nrep-1) OPTIONAL	I4B	OUT	pointer containing the transformation(s) (in {0, 3}) to apply to each of the returned pixels to match exactly in shape and position its respective template. 0: rotation around the polar axis only, 1: rotation + East-West swap (ie, reflexion around meridian), 2: rotation + North-South swap (ie, reflexion around Equator), 3: rotation + East-West and North-South swaps. The routines will allocate the list array if it is not allocated upon calling.
nrep OPTIONAL	I4B	OUT	number of pixels having the same template (either 8, 16, $4N_{\text{side}}$ or $8N_{\text{side}}$ ).

#### **EXAMPLE:**

call same\_shape\_pixels\_ring(256, 1234, list, reflexion, np)

Returns in list the RING-scheme index of the all the pixels having the same shape as the template #1234 for  $N_{\rm side}=256$ . Upon return reflexion will contain the rotation/reflexions to apply to each pixel returned to match the template, and np will contain the number of pixels having that same shape (16 in that case).

#### RELATED ROUTINES

This section lists the routines related to **same\_shape\_pixels\_ring**.

nside2templates returns the number of template pixel shapes avail-

able for a given  $N_{\text{side}}$ .

template\_pixel\_ring

template\_pixel\_nest return the template shape matching the pixel pro-

vided

## scan\_directories

Location in HEALPix directory tree: src/f90/mod/paramfile\_io.F90 Function to scan a set of directories for a given file

FORMAT var=scan\_directories(directories, filename, full-path)

#### **ARGUMENTS**

name&dimensionality	kind	in/out	description
directories	CHR	IN	contains the set of directories (up to 20), separated by an ASCII character of value < 32 (see concatn1). During the search, it is assumed that the given directories and filename can be separated by noth-
filename fullpath	CHR CHR		ing, a / (slash) or a \ (backslash) the file to be found. returns the full path to the first occur- rence of the file among the directories
var	LGT	OUT	provided. Empty if the file is not found. The search is not recursive. set to true if the file is found, to false otherwise.

#### **EXAMPLE:**

```
use paramfile_io
character(len=filenamelen) :: dirs, full
logical(lgt) :: found
dirs = concatnl('dir1','/dir2','/dir2/subdir1/') ! build directories
list.
found = scan_directories(dirs, 'myfile', full) ! do the search
if (found) print*,trim(full)
```

scan\_directories 189

Search for 'myfile' in the directories 'dir1', '/dir2', '/dir2/subdir1/'

#### RELATED ROUTINES

This section lists the routines related to scan\_directories.

parse\_xxx parse an ASCII file for parameters definition concatnl concatenates a set of substrings into one string,

interspaced with LineFeed character

# string, strlowcase, strupcase

Location in HEALPix directory tree: src/f90/mod/misc\_utils.F90

The Fortran90 module misc\_utils contains three functions to create or manipulate character strings.

#### **ARGUMENTS**

name & dimensionality	kind in/out	description
Tty		
number	LGT/ IN	number or boolean flag to be turned into
	I4B/	a character string.
	SP/	
	DP	
instring	CHR IN	arbitrary character string.
outstring	CHR —	output character string.
format	CHR IN	character string describing Fortran format
OPTIONAL		of output.
		-

#### **FUNCTIONS:**

outstring = string(number [,format])

returns in outstring its argument number converted to a character string. If format is provided it is used to format the output, if not, the fortran default format matching number's type is used.

outstring = strlowcase(instring)

returns in outstring its argument instring converted to lowercase. ASCII characters in the [A-Z] range are mapped to [a-z], while all others remain unchanged.

outstring = strupcase(instring)

returns in outstring its argument instring converted to uppercase. ASCII characters in the [a-z] range are mapped to [A-Z], while all others remain unchanged.

#### **EXAMPLE:**

```
use misc_utils
character(len=24) :: s1
s1 = string(123,'(i5.5)')
print*, trim(s1)
print*,trim(strupcase('*aBcD-123'))
print*,trim(strlowcase('*aBcD-123'))
```

Will printout 00123, \*ABCD-123 and \*abcd-123.

## surface\_triangle

Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Returns the surface in steradians of the spherical triangle described by its three vertices

**FORMAT** 

call surface\_triangle(v1, v2, v3, surface)

#### **ARGUMENTS**

name&dimensionalityki	nd in/out	description
v1(3) D	P IN	cartesian vector pointing at the triangle first vertex.
v2(3) D	P IN	cartesian vector pointing at the triangle second vertex.
v3(3) D.	P IN	cartesian vector pointing at the triangle third
surface D	P OUT	vertex. surface of the triangle in steradians.

#### **EXAMPLE:**

use healpix\_types

use pix\_tools, only : surface\_triangle

real(DP) :: surface, one =  $1.0_dp$ 

call  $surface_triangle((/1,0,0/)*one, (/0,1,0/)*one, (/0,0,1/)*one,$ 

surface)

print\*, surface

Returns the surface in steradians of the triangle defined by the octant (x, y, z > 0): 1.5707963267948966

#### RELATED ROUTINES

This section lists the routines related to **surface\_triangle**.

surface\_triangle 193

pix2ang, ang2pix pix2vec, vec2pix convert between angle and pixel number. convert between a cartesian vector and pixel number.

query\_disc, query\_polygon, query\_strip, query\_triangle

render the list of pixels enclosed respectively in a given disc, polygon, latitude strip and triangle

## template\_pixel\_nest, template\_pixel\_ring

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routines to provide the index of the template pixel associated with a given **HEALPix** pixel, for a resolution parameter  $N_{\text{side}}$ .

Any pixel can be *matched in shape* to a single of these templates by a combination of a rotation around the polar axis with reflexion(s) around a meridian and/or the equator.

The template pixels are all located in the Northern Hemisphere, or on the Equator. They are chosen to have their center located at

$$\begin{split} z &= \cos(\theta) \geq 2/3, \qquad 0 < \phi \leq \pi/2, \\ 2/3 > z \geq 0, \qquad \phi = 0, \quad \text{or} \quad \phi = \frac{\pi}{4N_{\text{side}}}. \end{split}$$

They are numbered continuously from 0, starting at the North Pole, with the index increasing in  $\phi$ , and then increasing for decreasing z.

FORMAT	call template_pixel_nest(nside, pixel_nest, template, reflexion)
FORMAT	call template_pixel_ring(nside, pixel_ring, template, reflexion)

name & dimensionality	kind	in/out	description
		·	
nside	I4B	IN	the <b>HEALPix</b> $N_{\text{side}}$ parameter.
pixel_nest	I4B	IN	NESTED scheme pixel identification number over the range $\{0.12N_{\text{side}}^2 - 1\}$ .
pixel_ring	I4B	IN	RING scheme pixel identification number over the range $\{0,12N_{\text{side}}^2 - 1\}$ .
template	I4B	OUT	identification number(s) of the template matching in shape the pixel(s) provided (the numbering scheme of the pixel tem-
reflexion	I4B	OUT	plates is the same for both routines). in {0, 3} encodes the transformation(s) to apply to each pixel provided to match exactly in shape and position its respective template. 0: rotation around the polar axis only, 1: rotation + East-West swap (ie, reflexion around meridian), 2: rotation + North-South swap (ie, reflexion around Equator), 3: rotation + East-West and North-South swaps

#### **EXAMPLE:**

call template\_pixel\_ring(256, 500000, template, reflexion)

Returns in template the index of the template pixel (16663) whose shape matches that of the pixel #500000 for  $N_{\rm side} = 256$ . Upon return reflexion will contain 2, meaning that the template must be reflected around a meridian and around the equator (and then rotated around the polar axis) in order to match the pixel.

#### RELATED ROUTINES

This section lists the routines related to template\_pixel\_ring.

nside2templates	returns the number of template pixel shapes avail-
	able for a given $N_{\text{side}}$ .
$same\_shape\_pixels\_ring$	
$same\_shape\_pixels\_nest$	return the ordered list of pixels having the same
	shape as a given pixel template

udgrade\_nest\*

# $udgrade_nest*$

#### Location in HEALPix directory tree: src/f90/mod/udgrade\_nr.f90

Routine to degrade or prograde the pixel size of a **HEALPix** map indexed with the NESTED scheme. The degradation/progradation is done assuming an intensive quantity (like temperature) that does NOT scale with surface area.

In case of degradation, a big pixel that contains one or several bad pixels will take the average of the valid small pixels, unless a 'pessimistic' behavior is assumed in which case the big pixel will take the bad pixel sentinel value. In case of progradation, a bad pixel only spawns bad pixels.

The routine accepts both mono and bi-dimensional maps.

#### **FORMAT**

call udgrade\_nest\*(map\_in, nside\_in, map\_out, nside\_out [, fmissval, pessimistic])

name & dimensionality	kind	in/out	description
name & unnensionality	KIIIU	m/out	description
map_in(0:12*nside_in**2-1)	SP/ DP	IN	mono-dimensional full sky map to be prograded or degraded.
map_in(0:12*nside_in**2-1,1:nd)	SP/ DP	IN	bi-dimensional full sky map to be prograded or degraded. The routine finds the second dimension (nd) by itself.
nside_in	I4B	IN	the $N_{side}$ resolution parameter of the input map. Must be a power of 2.
map_out(0:12*nside_out**2- 1)	SP/ DP	OUT	mono-dimensional full sky map after degradation or progradation.
map_out(0:12*nside_out**2-1,1:nd)	SP/ DP	OUT	bi-dimensional full sky map after degradation or progradation. The second dimension (nd) should match that of the input map.
nside_out	I4B	IN	the $N_{side}$ resolution parameter of the output map. Must be a power of 2. If nside_out > nside_in, the map is prograded (ie, more and smaller pixels) with each pixel having the same value as its parent; otherwise, the map in degraded (ie, fewer larger pixels), with each pixel being the average of its (nside_in/nside_out) <sup>2</sup> components.
fmissval (OPTIONAL)	SP/ DP	IN	sentinel value given to bad pixels in input and output maps. ( <b>default:</b> $-1.6375 \ 10^{30}$ )
pessimistic (OPTIONAL)	LGT	IN	if set to .true., during a degradation, a big pixel containing at least a small bad pixel will be returned as bad as well, instead of taking the average of the remaing valid pixels. (default: .false.)

#### **EXAMPLE:**

call udgrade\_nest(map\_hi, 256, map\_low, 64)

Degrades a NESTED ordered map with  $N_{side}=256$  into a NESTED map with  $N_{side}=64$ 

#### RELATED ROUTINES

udgrade\_nest\*

This section lists the routines related to  $\mathbf{udgrade\_nest*}$ .

udgrade\_ring

prograde or degrade a RING ordered map.

# udgrade\_ring\*

#### Location in HEALPix directory tree: src/f90/mod/udgrade\_nr.f90

Routine to degrade or prograde the pixel size of a **HEALPix** map indexed with the RING scheme. The degradation/progradation is done assuming an intensive quantity (like temperature) that does NOT scale with surface area.

In case of degradation, a big pixel that contains one or several bad pixels will take the average of the valid small pixels, unless a 'pessimistic' behavior is assumed in which case the big pixel will take the bad pixel sentinel value. In case of progradation, a bad pixel only spawns bad pixels.

The routine accepts both mono and bi-dimensional maps.

#### **FORMAT**

call udgrade\_ring\*(map\_in, nside\_in, map\_out, nside\_out [, fmissval, pessimistic])

udgrade\_ring\* 201

name & dimensionality	kind	in/out	description
map_in(0:12*nside_in**2- 1)	SP/ DP	INOUT	mono-dimensional full sky map to be prograded or degraded. The routine finds the second dimension (nd) by itself. Note that the map is modified on output
map_in(0:12*nside_in**2-1,1:nd)	SP/ DP	INOUT	(reordered into NESTED scheme). bi-dimensional full sky map to be prograded or degraded. Note that the map is modified on output (reordered into NESTED scheme).
nside_in	I4B	IN	the $N_{side}$ resolution parameter of the input map. Must be a power of 2.
map_out(0:12*nside_out**2-1)	SP/ DP	OUT	mono-dimensional full sky map after degradation or progradation.
map_out(0:12*nside_out**2-1,1:nd)		OUT	bi-dimensional full sky map after degradation or progradation. The second dimension (nd) should match that of the input map.
$nside\_out$	I4B	IN	the $N_{side}$ resolution parameter of the output map. Must be a power of 2. If nside_out > nside_in, the map is prograded (ie, more and smaller pixels) with each pixel having the same value as its parent; otherwise, the map in degraded (ie, fewer larger pixels), with each pixel being the average of its (nside_in/nside_out) <sup>2</sup> components.
fmissval (OPTIONAL)	SP/ DP	IN	sentinel value given to bad pixels in input and output maps. ( <b>default:</b> $-1.6375 \ 10^{30}$ )
pessimistic (OPTIONAL)	LGT	IN	if set to .true., during a degradation, a big pixel containing at least a small bad pixel will be returned as bad as well, instead of taking the average of the remaing valid pixels. (default: .false.)

#### **EXAMPLE:**

call udgrade\_ring(map\_hi, 256, map\_low, 64)

Degrades a RING ordered map with  $N_{side}=256$  into a RING map with  $N_{side}=64$ 

#### RELATED ROUTINES

This section lists the routines related to  $\mathbf{udgrade\_ring*}$ .

 $udgrade\_nest$ 

prograde or degrade a NESTED ordered map.

vec2ang 203

# vec2ang

#### Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90

Routine to convert the 3D position vector (x, y, z) of point into its position angles  $(\theta, \phi)$  on the sphere with  $x = \sin \theta \cos \phi$ ,  $y = \sin \theta \sin \phi$ ,  $z = \cos \theta$ .

**FORMAT** 

call vec2ang(vector, theta, phi)

#### **ARGUMENTS**

name&dimensionality	kind	in/out	description
vector(3)	DP	IN	three dimensional cartesian position vector $(x, y, z)$ . The
theta	DP	OUT	north pole is $(0,0,1)$ colatitude in radians measured southward from north pole (in
phi	DP	OUT	$[0,\pi]$ ). longitude in radians measured eastward (in $[0, 2\pi]$ ).

#### RELATED ROUTINES

This section lists the routines related to **vec2ang**.

ang2vec

converts the position angles of a point on the sphere into its 3D position vector.

## $\mathbf{vect}_{\mathbf{prod}}$

Location in HEALPix directory tree: src/f90/mod/pix\_tools.f90 Returns the vectorial product of two vectors.

**FORMAT** 

call vect\_prod(v1, v2, v3)

#### **ARGUMENTS**

name&dimensionalitykind	in/out	description
v1(3) DP v2(3) DP v3(3) DP	IN IN OUT	cartesian vector $\mathbf{v}_1$ . cartesian vector $\mathbf{v}_2$ . cartesian vector $\mathbf{v}_3 = \mathbf{v}_1 \times \mathbf{v}_2$

#### **EXAMPLE:**

use healpix\_types

use pix\_tools, only : vect\_prod
real(DP), dimension(3) :: vec

 $real(DP) :: one = 1.0_dp$ 

call  $vect_prod((/2,0,0/)*one, (/0,1,0/)*one, vec)$ 

print\*, vec

will return: 0.00E+000 0.00E+000 2.00

#### RELATED ROUTINES

This section lists the routines related to **vect\_prod**.

angdist

computes the angular distance between 2 vectors

write\_asctab\*

## write\_asctab\*

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine stores a power spectrum in an ascii FITS-file. The routine can store temperature coeffecients  $C_l^T$  or both temperature and polarisation coeffecients  $C_l^T$ ,  $C_l^B$ ,  $C_l^B$ ,  $C_l^{T \times E}$ .

#### **FORMAT**

call write\_asctab\*(clout, lmax, ncl, header, nl-header, filename)

#### ARGUMENTS

name & dimensionality	kind	in/out	description
$\overline{\text{filename}(\text{LEN=filenamelen})}$	CHR	IN	the FITS file to which the power spectrum is written.
lmax	I4B	IN	Maximum $\ell$ value to be written.
ncl	I4B	IN	1 for temperature coeffecients
clout(0:lmax,1:ncl)	SP/ I	IN	only, 4 for polarisation. the powerspectrum to be saved in the file.
nlheader	I4B	IN	number of header lines to write
header(LEN=80) (1:nlheader)	CHR	IN	to the file. the header to the FITS-file.

#### **EXAMPLE:**

call write\_asctab (cl,64,1,header,80,'cl.fits')

Writes a powerspectrum in the array cl(0:64,1:1) to a FITS-file called 'cl.fits'. The cl array contains the temperature power-spectrum  $C_l^T$  up to an  $\ell$  value of 64. 80 header lines are written to the file from the array header(1:80).

#### MODULES & ROUTINES

This section lists the modules and routines used by write\_asctab\*.

fitstools module, containing:

printerror routine for printing FITS error messages.

**cfitsio** library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to write\_asctab\*.

alm2cl Routine computing the power spectrum from

spherical harmonics coefficients  $a_{\ell m}$ 

fits2cl Routine to read a FITS file created by

 $write\_asctab.$ 

write\_minimal\_header routine to write minimal FITS header

write\_bintab\*

## write\_bintab\*

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine creates a binary FITS-file from a **HEALPix** map. The routine can save a temperature map or both temperature and polarisation maps (T,Q,U) to the file.

# FORMAT call write\_bintab\*(map, npix, nmap, header, nl-header, filename [, extno])

Arguments appearing in *italic* are optional.

#### **ARGUMENTS**

name & dimensionality	kind	in/out	description
map(0:npix-1,1:nmap)	SP/	IN	the map to write to the FITS-file.
•	DP 14D	INI	NI la d'alla de la la la de la companya de la compa
npix	I4B	IN	Number of pixels in the map.
nmap	I4B	IN	number of maps to be written, 1 for temper-
			ature only, and 3 for $(T,Q,U)$ .
header(LEN=80) (1:nl-	CHR	IN	The header for the FITS-file.
header)			
nlheader	I4B	IN	number of header lines to write to the file.
filename(LEN=8)	CHR	IN	the map(s) is (are) written to a FITS-file
			with this filename.
extno	I4B	IN	extension number in which to write the data
			(0 based). ( <b>default:</b> 0)

#### **EXAMPLE:**

call write\_bintab (map,12\*32\*\*2,3,header,120,'map.fits')

Makes a binary FITS-file called 'map.fits' from the **HEALPix** maps (T,Q,U) in the array map(0:12\*32\*\*2-1,1:3). The number of pixels 12\*32\*\*2 corresponds to the number of pixels in a  $N_{side} = 32$  **HEALPix** map. The header for the FITS-file is given in the string array header and the number of lines in the header is 120.

#### MODULES & ROUTINES

This section lists the modules and routines used by write\_bintab\*.

fitstools module, containing:

printerror routine for printing FITS error messages.

**cfitsio** library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to write\_bintab\*.

input\_map, read\_bintab routines which read a file created by

write\_bintab\*.

map2alm subroutine which analyse a map and returns the

 $a_{lm}$  coeffecients.

output\_map subroutine which calls write\_bintab\*

write\_bintabh subroutine to write a large array into a FITS file

piece by piece

input\_tod\* subroutine to read an arbitrary subsection of a

large binary table

write\_minimal\_header routine to write minimal FITS header

write\_bintabh 209

## write\_bintabh

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine is designed to write large (or huge) arrays into a binary table extension of a FITS file. The user can choose to write the array piece by piece. This is designed to deal with Time Ordered Data set (tod).

#### **FORMAT**

call write\_bintabh(tod, npix, ntod, header, nl-header, filename, [extno, firstpix, repeat])

Arguments appearing in *italic* are optional.

name & dimensionality	kind	in/out	description
tod(0:npix-1,1:ntod)	SP	IN	the map or tod to write to the FITS-file. It will be written in the file at the location corresponding to pixels (or time samples) firstpix to firtpix + npix -1.
npix	I8B	IN	Number of pixels or time samples in the map or TOD. See Note below.
ntod	I4B	IN	number of maps or tods to be written.
header(LEN=80) (1:nlheader)	CHR	IN	The header for the FITS-file.
nlheader	I4B	IN	number of header lines to write to the file.
filename(LEN = filenamelen)	CHR	IN	the array is written into a FITS-file with this filename.
extno	I4B	IN	extension number in which to write the data (0 based). ( <b>default:</b> 0)
firstpix	I8B	IN	0 location in the FITS file of the first pixel (or time sample) to be written (0 based). ( <b>default:</b> 0). See Note below.
repeat	I4B	IN	length of the element vector used in the binary table. ( <b>default:</b> 1024) if npix $\propto 1024$ ; 12000 if npix $> 12000$ and 1 otherwise. Choosing a large repeat for multi-column tables (ntod $> 1$ ) generally speeds up the I/O. It also helps bringing the number of rows of the table under $2^{31}$ , which is a hard limit of cfitsio.

**Note:** Indices and number of data elements larger than  $2^{31}$  are only accessible in FITS files on computers with 64 bit enabled compilers and with some specific compilation options of cfitsio (see cfitsio documentation).

#### **EXAMPLE:**

```
use healpix_types
use fitstools, only : write_bintabh
character(len=80), dimension(1:128) :: hdr
real(SP), dimension(0:49,1) :: tod
hdr(:) = ' '
tod(:,1) = 1.
call write_bintabh(tod, 50_i8b, 1, header, 128, 'tod.fits', firstpix=0_i8b, repeat=10)
```

write\_bintabh 211

```
tod = tod * 3.
call write_bintabh(tod, 20_i8b, 1, header, 128, 'tod.fits',
firstpix=40_i8b)
```

Writes into the FITS file 'tod.fits' a 1 column binary table, where the first 40 data samples have the value 1. and the next 20 have the value 3. (Note that in this example the second call to write\_bintabh overwrites some of the pixels written by the first call). The samples will be written in element vectors of length 10. The header for the FITS-file is given in the string array hdr and the number of lines in the header is 128.

#### MODULES & ROUTINES

This section lists the modules and routines used by write\_bintabh.

fitstools module, containing:

printerror routine for printing FITS error messages.

**cfitsio** library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to write\_bintabh.

input\_tod\* routine that reads a file created by write\_bintabh.

input\_map, read\_bintab routines to read **HEALPix** sky map, write\_minimal\_header routine to write minimal FITS header

# $write\_dbintab$

Location in HEALPix directory tree: src/f90/mod/fitstools.f90 This routine is obsolete. Use write\_plm instead.

write\_fits\_cut4 213

## write\_fits\_cut4

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine writes a cut sky **HEALPix** map into a FITS file. The format used for the FITS file follows the one used for Boomerang98 and is adapted from COBE/DMR. This routine can be used to store polarized maps, where the information relative to the Stokes parameters I, Q and U are placed in extension 0, 1 and 2 respectively by successive invocation of the routine.

#### **FORMAT**

call write\_fits\_cut4(filename, np, pixel, signal, n\_obs, serror[, header, coord, nside, order, units, extno, polarisation])

name&dimensionality	kind	in/oı	ıtdescription
filename(LEN=filenamelen	n)CHR	IN	FITS file to be read from, containing a cut sky map
np	I4B	IN	number of pixels to be written in the file
pixel(0:np-1)	I4B	IN	index of observed (or valid) pixels
signal(0:np-1)	SP	IN	value of signal in each observed pixel
$n_{-}obs(0:np-1)$	I4B	IN	number of observation per pixel
serror(0:np-1)	SP	IN	rms of signal in pixel, for white noise, this is $\propto 1/\sqrt{\text{n}_{-}\text{obs}}$ .
header(LEN=80)(1:) (OPTIONAL)	CHR	IN	FITS extension header
coord(LEN=1) (OPTIONAL)	CHR	IN	astrophysical coordinates ('C' or 'Q' Celestial/eQuatorial, 'G' for Galactic, 'E' for Ecliptic)
nside (OPTIONAL)	I4B	IN	HEALPix resolution parameter of data set
order (OPTIONAL)	I4B	IN	<b>HEALPix</b> ordering scheme, 1: RING, 2: NESTED
header(LEN=80) (OPTIONAL)	CHR	IN	FITS header to be included in the FITS file
units(LEN=20)	CHR	IN	maps units (applies only to Signal and Serror)
(OPTIONAL) extension (OPTIONAL)  polarisaton (OPTIONAL)	I4B	IN	(0 based) extension number in which to write data. (default: 0). If set to 0 (or not set) a new file is written from scratch. If set to a value larger than 1, the corresponding extension is added or updated, as long as all previous extensions already exist. All extensions of the same file should use the same Nside, Order and Coord if set to a non zero value, specifies that file will contain the I, Q and U polarisation Stokes parameter in extensions 0, 1 and 2 respectively, and sets the FITS header keywords accordingly. If not set, the keywords found in header will prevail.  Note: the information relative to Nside, Order and Coord has to be given, either thru these keyword or via the FITS Header.

write\_fits\_cut4 215

#### MODULES & ROUTINES

This section lists the modules and routines used by write\_fits\_cut4.

fitstools module, containing:

printerror routine for printing FITS error messages.

**cfitsio** library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to write\_fits\_cut4.

anafast executable that reads a **HEALPix** map and anal-

yses it.

synfast executable that generate full sky **HEALPix** maps

getsize\_fits routine to know the size of a FITS file and its type

(eg, full sky vs cut sky)

input\_map all purpose routine to input a map of any kind

from a FITS file

output\_map subroutine to write a FITS file from a **HEALPix** 

map

read\_fits\_cut4 subroutine to read a **HEALPix** cut sky map from

a FITS file

write\_minimal\_header routine to write minimal FITS header

### write\_minimal\_header

#### Location in HEALPix directory tree: src/f90/mod/head\_fits.F90

This routine writes the baseline FITS header for the most common **HEALPix** data sets: (cut sky or full sky) map, C(l) power spectra and  $a_{lm}$  coefficients.

#### **FORMAT**

call write\_minimal\_header(header, dtype, [append, nside, order, ordering, coordsys, creator, version, randseed, beam\_leg, fwhm\_degree, units, nlmax, polar, nmmax, bcross, deriv])

Arguments appearing in *italic* are optional.

write\_minimal\_header 217

name & dimensionality	kind	in/out	description
header(LEN=80) DIMENSION(:)	CHR	INOUT	The FITS header to fill in.
dtype(LEN=*)	CHR	IN	data to be put in the FITS file, must be one of 'ALM', 'CL', 'MAP', 'CUTMAP' (case un-sensitive).
append	LGT	IN	if set to TRUE, the keywords will be appended to the content of header instead of written from scrath
nside	I4B	IN	map resolution parameter; required for dtype='MAP' and dtype='CUTMAP'
order	I4B	IN	map ordering, either 1 (=ring) or 2 (=nested); see ordering
ordering(LEN=*)	CHR	IN	map ordering, either 'RING' or 'NESTED' (case un-sensitive); either order or ordering is required for dtype='MAP' and dtype='CUTMAP'
coordsys(LEN=*)	CHR	IN	map coordinate system; Valid choices are 'G' = Galactic, 'E' = Ecliptic, 'C'/'Q' = Celestial = eQuatorial
creator(LEN=*)	CHR	IN	name of software generating the data set
version(LEN=*)	CHR	IN	version of creator software
randseed	I4B	IN	random number generator seed used to generate the data
$beam\_leg(LEN=*)$	CHR	IN	File containing Legendre transform of symmetric beam
$fwhm\_degree$	DP	IN	FWHM in degrees of gaussian symmetric beam (FITS keyword: FWHM)
units(LEN=*)	CHR	IN	physical units of the data set (FITS keyword: TUNIT*)
nlmax	I4B	IN	maximum multipole order $l$ of the data set (FITS keyword: MAX-LPOL)
polar	LGT	IN	if set to .TRUE., the file to be written contains polarized data
nmmax	I4B	IN	maximum degree $m$ of data set (FITS keyword: MAX-MPOL)
bcross	LGT	IN	if set to .TRUE., the magnetic cross terms power spectra (TB and EB) are included; only applies to dtype='CL'
deriv	I4B	IN	order of derivatives to included in FITS file (0, 1 or 2); only applies to dtype='MAP'

#### **EXAMPLE:**

use head\_fits
character(len=80), dimension(1:60) :: header
call write\_minimal\_header(header, 'MAP', nside=256, ordering='Nested')
call add\_card(header, 'HISTORY', 'Dummy map')

Writes in header a **HEALPix** compliant FITS header for a  $N_{\text{side}} = 256$  map with NESTED ordering. Further HISTORY information is added with add\_card

#### MODULES & ROUTINES

This section lists the modules and routines used by write\_minimal\_header.

write\_hl more general routine for adding a keyword to a

header.

**cfitsio** library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to write\_minimal\_header.

add\_card general purpose routine to write/edit an arbitrary

keyword into a FITS file header.

get\_card general purpose routine to read any keywords

from a header in a FITS file.

del\_card routine to discard a keyword from a FITS header

read\_par, number\_of\_alms routines to read specific keywords from a header

in a FITS file.

getsize\_fits function returning the size of the data set in a fits

file and reading some other useful FITS keywords

merge\_headers routine to merge two FITS headers

write\_plm 219

## $write_plm$

#### Location in HEALPix directory tree: src/f90/mod/fitstools.f90

This routine creates a double precision binary FITS-file from a given array. The routine is used by the **HEALPix** facility plungen to store precomputed  $P_{lm}(\theta)$ .

# FORMAT call write\_plm(plm, nplm, nhar, header, nl-header, filename, nsmax, nlmax)

name&dimensionality	kind	in/o	utdescription
1 (0 1 1 1 1 )	DD	TNI	
plm(0:nplm-1,1:nhar)	DP	IN	the array with the precomputed $P_{lm}(\theta)$ values.
nplm	I4B	IN	Number of $P_{lm}$ values to store.
nhar	I4B	IN	1 for scalar $P_{lm}$ only and 3 for tensor
			harmonics.
header(LEN=80) (1:nlheader)	CHR	IN	The header for the FITS-file.
nlheader	I4B	IN	number of header lines to write to
			the file.
filename(LEN = filenamelen)	CHR	IN	the precomputed $P_{lm}(\theta)$ values are written to this file.
nsmax	I4B	IN	$N_{side}$ for the precomputed $P_{lm}$ s.
nlmax	I4B	IN	maximum $\ell$ value for the precom-
			puted $P_{lm}$ s.

#### **EXAMPLE:**

call write\_plm (plm, 65\*66\*32, 1, header, 120, 'plm\_32.fits', 32, 64)

Makes a double precision binary FITS-file called 'plm\_32.fits' from the precomputed  $P_{lm}(\theta)$  in the array plm(0:65\*66\*32-1,1:1). The number 65\*66\*32 corresponds to the number of precomputed  $P_{lm}$ s needed for a  $N_{side} = 32$  **HEALPix** map synthesis/analysis. The header for the FITS-file is given in the string array header and the number of lines in the header is 120.

#### MODULES & ROUTINES

This section lists the modules and routines used by write\_plm.

fitstools module, containing:

printerror routine for printing FITS error messages.

cfitsio library for FITS file handling.

#### RELATED ROUTINES

This section lists the routines related to write\_plm.

read\_dbintab, read\_bintab routines which reads a file created by write\_plm.

map2alm, alm2map routines using precomputed  $P_{lm}(\theta)$ .

xcc\_v\_convert 221

### $xcc_v_convert$

 $Location \ in \ HEALPix \ directory \ tree: \ src/f90/mod/coord\_v\_convert.f90$ 

This routine rotates a 3D coordinate vector from one astronomical coordinate system to another.

FORMAT call xcc\_v\_convert(ivector, iepoch, oepoch, isys, osys, ovector)

#### **ARGUMENTS**

name & dimension-	kind in	out description
ality		
ivector(1:3)	DP IN	3D coordinate vector of one astronomical ob-
, ,		ject, in the input coordinate system.
iepoch	DP IN	epoch of the input astronomical coordinate system.
oepoch	DP IN	epoch of the output astronomical coordinate
isys(len=*)	CHR IN	system.  input coordinate system, should be one of 'E'=Ecliptic, 'G'=Galactic, 'C'/'Q'=Celestial/eQuatorial.
osys(len=*)	CHR IN	output coordinate system, same choice as above.
ovector(1:3)	DP IN	

#### **EXAMPLE:**

```
use healpix_types
use coord_v_convert, only: xcc_v_convert
real(dp) :: vecin(1:3), vecout(1:3)
vecin = (/ 0_dp, 0_dp, 1_dp /)
call xcc_v_convert(vecin, 2000.0_dp, 2000.0_dp, 'g', 'c', vecout)
```

Will produce in vecout the location in Celestial coordinates (2000 epoch) of the North Galactic Pole (defined in vecin)

#### RELATED ROUTINES

This section lists the routines related to xcc\_v\_convert.

coordsys2euler\_zyz produces the Euler angles  $\psi, \theta, \varphi$  in (Z,Y,Z) con-

vention for rotation between standard astronomi-

cal coordinate systems.

ang2vec, vec2ang Routine to convert spherical coordinates (co-

latitude and longitude) into 3D vector coordinates

and vice-versa.